

# Sequence-to-Sequence Self Calibration

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## Abstract

*We present a linear method for self-calibration of a moving rig when no correspondences are available between the cameras. Such a scenario occurs, for example, when the cameras have different viewing angles, different zoom factors or different spectral range. It is assumed that during the motion of the rig, the relative viewing angle between the cameras remains fixed and is known. Except for the fixed relative viewing angle, any of the internal parameters and any of the other external parameters of the cameras may vary freely. The calibration is done by linearly computing multilinear invariants, expressing the relations between the optical axes of the cameras during the motion. A solution is then extracted from these invariants. Given the affine calibration, the metric calibration is known to be achieved linearly (e.g. by assuming zero skew).*

*Thus an automatic solution is presented for self calibration of a class of moving rigs with varying internal parameters. This solution is achieved without using any correspondences between the cameras, and requires only solving linear equations.*

**Keywords:** *Self-Calibration, Multi-View Invariants.*

## 1 Introduction

The projective framework of Structure from Motion (SFM) is supported by a relatively large body of literature on the techniques for taking matching image features (points and lines) across multiple views and producing a projective representation of the three-dimensional (3D) positions of the features in space.

For many tasks such as computer graphics, projective representation is not sufficient, and an Affine/Metric representation is required. In recent years there has been much progress in the theory and algorithms of Self/Auto-Calibration, the upgrading of a projective structure to an Affine/Metric one, without using knowledge of the viewed scene. These algorithms must make assumptions about the parameters of the camera to achieve a unique solution (For a review see [6]).

There are roughly two approaches to self-calibration: The non-stratified approach solves directly for metric upgrade. This can be done for example by solving Kruppa's equations [4], or by solving for the absolute quadric [11]. In both cases the solution of a set of non-linear equations is required. The stratified approach first upgrades the projective representation to an affine representation by solving for the homographies through the plane at infinity and then upgrades the affine representation to a metric one [3, 8]. It was pointed by several authors (e.g. [6, 7]) that the first stage, the affine calibration, is the most challenging in stratified methods.

By using a stereo rig, a stable solution for both affine and metric calibration can be computed linearly from two or more images from each camera ([7], following [12]). This method assumes that the rig structure and the Zoom/Focus are fixed. Another approach for rig calibration achieves a linear solution by assuming known relative orientations of the cameras, but allowing the Zoom/Focus and the relative displacements to vary [13]. Both methods require correspondences between the cameras.

In this paper we focus on a self-calibration scenario which is of interest on both practical and theoretical fronts. We consider a rig of two or more video cameras, each capturing an image sequence, where there is no or little spatial overlap between the fields of view of the cameras (such as when the cameras have different zoom settings or pointing to largely different directions). While in motion, each camera may change its internal parameters and zoom factor.

Applying conventional self calibration algorithms for each camera separately is always challenging with varying internal parameters, especially the affine calibration stage. Applying one of the existing rig algorithms [7, 13], on the other hand, is not possible since no correspondences are available between the cameras.

Therefore, we seek to solve for the calibration of the cameras, while exploiting the *rigidity constraints between them*. We refer to this problem as "Sequence to Sequence Self-Calibration", since every sequence requires a different calibration, and only the relations between the sequences can be exploited to recover these calibrations. A similar scenario, of exploiting the rigidity between multiple cameras, was presented recently in the context of image alignment [1].

A previous approach for handling self calibration without correspondences between the cameras [2] assumed highly constrained conditions: In addition to

knowing one degree of freedom about the rotation between the cameras, that solution also assumed fixed internal parameters, where only two of which were unknown. It also required the solution of highly non-linear equations over a large set of variables. The work presented in this paper solves for affine calibration linearly, without using any assumption but one known d.o.f. of the relative rotation between the cameras.

In order to solve for the calibration, we use assumptions about the relative orientations of the cameras in the rig. We divide the problem to three different cases:

- Two cameras with parallel image planes. The cameras may view the same direction, or the opposite directions (Back to back).
- Two cameras with non-parallel image planes, with the special case of orthogonal image planes.
- Three cameras with varying orientations, each rotating about its  $Y$  axis. Their  $Y$  axes are assumed to be parallel.

In the following sections we present a linear solution for affine self-calibration for each of the cases above, assuming the cameras are synchronized. Later in Section. 5 we show how such synchronization can be achieved automatically. The calibration is done by computing multilinear tensorial invariants, expressing the relations between the axes of the cameras during the motion. A solution is then extracted from these tensors. Having solved for the challenging stage of affine calibration, the metric calibration can be achieved linearly by imposing further constraints, e.g. zero skew (see [6]). In case the cameras view the same/opposite directions, they share the same affine ambiguity. Thus metric constraints on both cameras can be simultaneously used for calibrating both of the cameras.

### 1.1 Formal Statement of the Problem

A pinhole camera projects a point  $P$  in 3-D projective space  $\mathcal{P}^3$  to a point  $p$  in the 2-D projective plane  $\mathcal{P}^2$ . The projection can be written as a  $3 \times 4$  homogeneous matrix  $M$ :

$$p \cong MP$$

where  $\cong$  marks equality up to a scale factor. When the camera is calibrated, it can be factored (by QR decomposition):

$$M = K[R;T]$$

where  $R$  and  $T$  are the rotation and translation of the camera respectively, and  $K$  is a  $3 \times 3$  upper diagonal matrix containing the internal parameters of the camera. The most general form of the internal parameters matrix  $K$  is:

$$K = \begin{pmatrix} f & \gamma & u_0 \\ 0 & \alpha f & v_0 \\ 0 & 0 & 1 \end{pmatrix} \tag{1}$$

where  $f$  is the *focal length*,  $\alpha$  is the *aspect ratio*,  $(u_0, v_0)$  is the *principle point* and  $\gamma$  is the *skew*. It is practical to model  $K$  by a reduced set of internal parameters, for example assume zero skew.

Generally, given projections of  $m$  3-D points  $\{P_j\}_{j=1}^m$  to  $n$  images, it is possible to estimate the location of the 3-D points and the camera matrices  $\{M\}_{i=1}^n$  up to a projective transformation (collineation) represented by a  $4 \times 4$  matrix  $H$ :

$$p \cong MH^{-1}HP \quad (2)$$

The matrices  $\{C_i = M_iH^{-1}\}_{i=1}^n$  are called the projective camera matrices. The points  $HP$  are the points in the projective coordinate system. We refer to the matrix  $H^{-1}$  as the projective to Euclidean matrix.

When the internal parameters of the cameras  $\{K_i\}_{i=1}^n$  are known, then  $H$  can be recovered up to a 3-D similarity transformation. The goal of (internal) calibration is to recover  $\{K_i\}_{i=1}^n$ , or equivalently recover the  $4 \times 4$  collineation  $H$  up to a similarity transformation.

In all following sections it is assumed that the projective camera matrices  $\{C\}_{i=1}^n$  were already computed for each one of the sequences, using for example point correspondences between the different frames. This can be done in various ways (for a review see [6]).

## 2 Parallel optical axes

We first analyze the case of two cameras attached in a rig, viewing the same direction, or the opposite directions (back-to-back). In addition, each camera may rotate freely about its  $Z$  axis. Note that there are no constraining assumption about neither the internal parameters of the cameras, nor the relative displacements of the centers of projections.

The first Euclidean camera matrix is given by:

$$M_i^1 = K_i^1[R_i; t_i^1]$$

and the second Euclidean camera is given by:

$$M_i^2 = K_i^2[R_0 * R_i; t_i^2]$$

Where  $R_0$  is the relative rotation between the cameras, and the third row of  $R_0$  equals  $[0, 0, 1]$  up to sign.

Given projective cameras  $C_i^1, C_i^2$ , we seek for two projective transformations  $H_1, H_2$  mapping the projective cameras to the Euclidean ones (up to similarity transformation).

Let  $r_i$  be the third row of  $R_i$ , and let  $c_i^j$  be the third row of  $C_i^j$ . Let  $\hat{H}_j, j = 1..2$  be the  $4 \times 3$  matrices composed from the first 3 columns of the matrices  $H_j$ .

The internal parameters matrices  $K_i^j$  are upper triangular matrices and so  $\hat{H}_1^T c_i^1 \cong r_i$ . Having also the special structure of the third row of  $R_0$  :  $\hat{H}_2^T c_i^2 \cong r_i$ . Thus for every  $i$ :

$$\hat{H}_1^T c_i^1 \cong \hat{H}_2^T c_i^2 \cong r_i \quad (3)$$

The constraint above holds also for  $D\hat{H}_1, D\hat{H}_2$  for every  $3 \times 3$  matrix  $D$ . This results in an ambiguity that would later on express itself as an affine ambiguity on the cameras, the same affine ambiguity for both cameras (up to similarity).

The above Eqns. 3 have a form we call “equivalence after projection”. In the next section we present the solution for such equations.

Given the solution to these equations, the homographies through the plane at infinity can be recovered for each sequence and between the sequences. A point  $[a^T, 0]^T$  on the plane at infinity is projected to  $C_i^j \hat{H}_j a$  in the  $i$ th frame of the  $j$ th camera. Hence the homography at infinity  $H_{ijkl}^\infty$  between frame  $i$  of camera  $j$  and frame  $k$  of camera  $l$  is given by

$$H_{ijkl}^\infty = C_k^l \hat{H}_l (C_i^j \hat{H}_j)^{-1}$$

The solutions to Eqn. 3 are up to a common  $3 \times 3$  matrix  $D$  which cancels out, and so:

$$H_{ijkl}^\infty = C_k^l \hat{H}_l (C_i^j \hat{H}_j)^{-1} = C_k^l \hat{H}_l D (C_i^j \hat{H}_j D)^{-1}$$

Similarly, the coordinates of the plane at infinity  $L_j$  in the projective representations of camera  $j$  can be recovered. Since  $L_j$  satisfies  $L_j^\top \hat{H}_j a = 0$  for every  $a$ , then  $L_j$  is the null space of  $\hat{H}_j^\top$ , which is also the null space of  $D\hat{H}_j^\top$ .

## 2.1 The “Equivalence after Projection” problem

We define the equivalence after projection problem as follows: Given two sets of points in  $P^3$   $\{P_i\}_{i=1}^n, \{Q_i\}_{i=1}^n$ , determine whether there exist two  $3 \times 4$  projection matrices  $A, B$  such that for every  $i$ :

$$AP_i \cong BQ_i$$

If such  $A$  and  $B$  exist solve for them up to a multiplication on the left by a  $3 \times 3$  matrix. We next show a solution for this problem which requires only solving linear systems of equations.

Let  $C_B$  be the center of the projection matrix  $B$ , i.e  $C_B$  is the null space of  $B$ . Let  $B^+$  be a pseudo-inverse of  $B$ , i.e. a mapping from the image plane of  $B$  to a plane in  $P^3$  such that  $BB^+p \cong p$ .

The points  $C_B, B^+AP_i$  are incident with the line of sight of the projection matrix  $B$  associated with the image point  $AP_i$ . Since  $AP_i \cong BQ_i$ ,  $Q_i$  is also on this line. This defines a constraint on the projection of these points by an arbitrary projection matrix  $O$ : Let  $e_O = OC_B$ . Then the point  $OQ_i$  resides on the line  $e_O \times OB^+AP_i$ . Therefore:

$$(OQ_i)^T ([e_O]_x OB^+A) P_i = 0 \tag{4}$$

By choosing an arbitrary camera matrix  $O$ , the  $3 \times 4$  matrix  $F_O = ([e_O]_x OB^+A)$  can be recovered linearly from the pairs of points  $\{OQ_i, P_i\}_{i=1}^n$ . The introduction of  $O$  enables to extract a unique bi-linear invariant with a minimal number of parameters. There exists a set of invariants described by  $4 \times 4$  matrices  $G$ ,

satisfying:  $(Q_i)^T(G)P_i = 0$ . These matrices span a linear space of dimension 4. By using the matrix  $O$ , we get a unique invariant with 12 elements.

For each  $O$ , the image  $e_O$  of  $C_B$  can be recovered as the null space of  $F_O^T$ . Using two such projection matrices  $O$ , the 3D position of  $C_B$  can be recovered by triangulation.

$A, B$  can be recovered up to some  $3 \times 3$  matrix  $D$ . All cameras of the form  $DB$  share the same center of projection. Thus  $B$  can be chosen as any  $3 \times 4$  matrix whose left null space is the recovered  $C_B$ . In order to solve for  $A$ ,  $\{BQ_i\}_{i=1}^n$  are first computed. Since for all  $i$ ,  $AP_i \cong BQ_i$  and  $BQ_i, P_i$  are known,  $A$  can be recovered. This can be done by any method for recovering a camera from the projections of known 3D points [6].

### 3 Non-Parallel optical axes

In the previous section, we studied the case of two cameras viewing the same or opposite directions. In this section, it is assumed that the two cameras have a known constant angle between their optical axes.

The directions of the optical axes of the cameras are given by  $c_i^{jT} \hat{H}_j$ , and the angle between the axes of the two cameras  $\alpha$  satisfies:

$$\cos^2 \alpha = \frac{(c_i^{1T} \hat{H}_1 \hat{H}_2^T c_i^2)^2}{(c_i^{1T} \hat{H}_1 \hat{H}_1^T c_i^1)(c_i^{2T} \hat{H}_2 \hat{H}_2^T c_i^2)} \quad (5)$$

This defines a nonlinear metric constraint on  $\hat{H}_1, \hat{H}_2$ .

We solve for the case of orthogonal optical axes, where  $\cos^2 \alpha = 0$ , i.e. by Eqn. 5:

$$c_i^{1T} \hat{H}_1 \hat{H}_2^T c_i^2 = 0$$

Each image pair provides one constraint on the matrix  $F = \hat{H}_1 \hat{H}_2^T$ . From the matrix  $F$ , one can extract using SVD the matrices  $\hat{H}_1 D$  and  $\hat{H}_2 D^{-T}$  for some unknown  $3 \times 3$  matrix  $D$ .

The planes at infinity of the two projective reconstructions are the null spaces of  $\hat{H}_1^T, \hat{H}_2^T$ , as in the previous section. The homography through the plane at infinity between frames  $i, k$  of the same sequence  $j$  can be computed similarly to previous case by  $C_k^j \hat{H}_j (C_i^j \hat{H}_j)^{-1}$ . Since the two matrices  $\hat{H}_1, \hat{H}_2$  do not have the same ambiguity, the homography through the plane at infinity between frames of different sequences cannot be computed.

### 4 Non-fixed parallel rotation axes

In previous sections we analyzed self calibration for rigs in which the angle between the optical axes of the cameras remains fixed. In some cases it is useful to enable the cameras to rotate. For example, they may need to be reoriented such that the object of interest appears in the image.

In this section we explore another type of constraints for self calibration of rigs without correspondences between the cameras. It is assumed that there are three cameras in the rig, each may rotate arbitrarily about its  $Y$  axis (or similarly about its  $X$  axis). It is further assumed that their  $Y$  axes are parallel. The rig as a whole can rotate and translate freely in space, and the internal parameters of the cameras may vary freely.

Since the  $Y$  axes of the cameras at time  $i$  are parallel to each other, they intersect in a point on the plane at infinity. Let  $\sigma_i^j$  be the plane defined by the  $X, Y$  axes of this camera. Then in every time instance  $i$ , all planes  $\{\sigma_i^j\}_{j=1,2,3}$  intersect in a point on the plane at infinity. We next show how to express this constraint as a multilinear equation in the projective camera matrices.

Let  $G_j$  be the transformations mapping the projective coordinate systems of camera  $j$  to a common affine reconstruction in which the plane at infinity is given by  $L = [0, 0, 0, 1]$ . Let  $\{\pi^j\}_{j=1,2,3}$  be three planes, where  $\pi^j$  is given in the coordinate system of the  $j$ -th camera. Then if these planes intersect in a point at infinity, the determinant of the following matrix vanishes:

$$\begin{bmatrix} G_1^{-T} \pi^1 \\ G_2^{-T} \pi^2 \\ G_3^{-T} \pi^3 \\ L \end{bmatrix} \quad (6)$$

This determinant can be written using a  $4 \times 4 \times 4$  tensor  $J^{abc}$ , as

$$\pi_a^1 \pi_b^2 \pi_c^3 J^{abc} = 0$$

The reader is assumed to be familiar with tensor notations. See for example in [9]

The tensor  $J^{abc}$  can now be used to express the calibration constraints. In each time  $i$  all planes  $\{\sigma_i^j\}_{j=1,2,3}$  intersect in a point on the plane at infinity. As  $\sigma_i^j$  is given by  $[0, 0, 1]C_i^j$ , this is expressed by:

$$([0, 0, 1]C_i^1)_a ([0, 0, 1]C_i^2)_b ([0, 0, 1]C_i^3)_c J^{abc} = 0$$

Given the projective camera matrices  $C_i^j$ , every time instance provides a linear constraint on  $J^{abc}$ . Thus  $J^{abc}$  can be computed linearly from the projection matrices.

In order to extract the homographies through the plane at infinity between different images, We identify points at infinity in each coordinate frame. Let  $Y_i^3$  be a double contraction of the form  $Y_i^3 = ([0, 0, 1]C_i^1)_a ([0, 0, 1]^T C_i^2)_b J^{abc}$ . Let  $N$  be any plane in the third coordinate system intersecting  $\sigma_i^1, \sigma_i^2$  in a point on the plane at infinity. Then:

$$([0, 0, 1]C_i^1)_a ([0, 0, 1]^T C_i^2)_b N_c J^{abc} = N^T Y_i^3 = 0$$

Hence  $Y_i^3$  is the point of intersection of  $\{\sigma_i^j\}_{j=1,2,3}$  in the coordinate frame of the third camera. Similarly this point can be extracted in the two other coordinate systems:  $Y_i^1, Y_i^2$ .

The set of points  $\{Y_i^j\}_{i=1..n}$  are sufficient to determine the plane at infinity at the  $j$ th coordinate system. We can use these matching points on the plane at infinity to compute the homography at infinity between all frames: The homography at infinity  $H_{stuv}^\infty$  between frames  $s$  and  $u$  of cameras  $t$  and  $v$  can be computed using the pairs of matching points  $\{(C_s^t Y_i^t, C_u^v Y_i^v)\}_{i=1..n}$ .

## 5 Sequences Synchronization

In the previous sections it was assumed that the sequences are synchronized. This enabled to compute the multilinear constraints:  $F_O$  of section 2.1,  $F$  of section 3 and  $J^{abc}$  of Section 4. However the existence of these constraints may be used to establish the synchronization between the sequences.

Consider for example the case of the orthogonal optical axes presented in section 3. The existence of a matrix  $F$  such that for every frame  $i$ :  $c_i^1 \top F c_i^2 = 0$  is not guaranteed if the two sequences are not temporally aligned. Let  $A$  be the estimation matrix of  $F$ , i.e  $A$  is the matrix whose  $i$ th row is composed from the Kronecker product of  $c_i^1$  and  $c_i^2$ . If such an  $F$  exists then the rank of the matrix  $A$  is not more than 8 and the vector composed from the elements of  $F$  lies in the null space of  $A$ . In practice due to noise  $A$  is always of full rank, and we use a least squares solution, choosing  $F$  to be composed out of the elements of the eigenvector of  $AA^\top$  with the smallest eigenvalue. Let  $f$  be this eigenvector. We define the magnitude of  $Af$  as the algebraic error of the estimation of  $F$ . When the sequences are synchronized this magnitude is expected to be small.

In order to synchronize the sequences this algebraic error is measured for each temporal shift between the sequences. The shift which produces the minimal algebraic error is chosen as the solution. This measure is not optimal for a number of reasons. First it has no real geometrical meaning. Second it depends on the number of the frames which can bias in short sequences toward the ends of the sequence. Third, changing the coordinates of  $c_i^j$  changes the measure. However in practice we find minimizing the algebraic error to work well on our sequences.

## 6 Experiments

We have conducted several experiments for testing the quality of the affine self-calibration and the sequence synchronization. In all our experiments we have used an object modeling framework: The cameras were static, and an object to be modeled was rotating in the scene. Points lying on this object were tracked, and the virtual camera motion with respect to the object was estimated. Since no calibration was available, the cameras and points had a projective ambiguity to be recovered in the experiments. Then the proposed algorithm was used, estimating an Affine representation of the structure and motion.

In the first experiment we tested the sequence synchronization application. The algorithm was applied for several temporal shifts, and the sequences were temporally aligned by finding the shift with the minimal residual error, as described in Section. 5. Figures 1-a,b present the results of this experiment for



opposite and orthogonal directions respectively. The true shift was estimated using hand waving in front of the camera. Note that this is an integer estimation for the non-integer temporal shift of the sequences, and thus it is accurate up to 0.5 a frame. In the experiments we tested 10 frames shifts in each temporal direction on sequences containing 40 frames. Indeed a shift close to the estimated by no more than 1 frame yielded the minimal estimation error.

One way to verify the accuracy of affine calibration is to test the accuracy of the homographies through the plane at infinity. In the second experiment we tested the accuracy of the homography through the plane at infinity by mapping vanishing points between the images. We have marked points lying on parallel lines, and tracked them along the sequences. The vanishing points at each frame were computed as the intersections of the parallel lines defined by the tracked points. We then mapped the vanishing points from the input images to a common coordinate system. The quality of the homographies was measured by the proximity of the mapped vanishing points. We have conducted this test for two scenarios: One for cameras viewing opposite directions (Section. 2), and one for cameras viewing orthogonal directions (Section. 3). Figure 2 shows the results of these experiments. Errors in these results are combined from errors in the Affine calibration, errors in the projective camera matrices (the input to our algorithm), and errors in the estimations of the vanishing points in the images due to drifts in the points tracking. However it is visible that the algorithm does indeed align the vanishing points.

Finally, the quality of the homographies can also be tested visually. Warping a sequence of images of a moving camera to a common reference by the homographies through the plane at infinity cancels the rotations of the cameras, as well as the variations in the internal parameters. The result is a sequence in which the camera virtually moves in pure translation and constant internal parameters. Figure. 3 shows the results of applying the computed homographies through the plane at infinity to several images. Note that while the original motion included a rotation, the homographies through the plane at infinity canceled the rotations, leaving only a translational component.

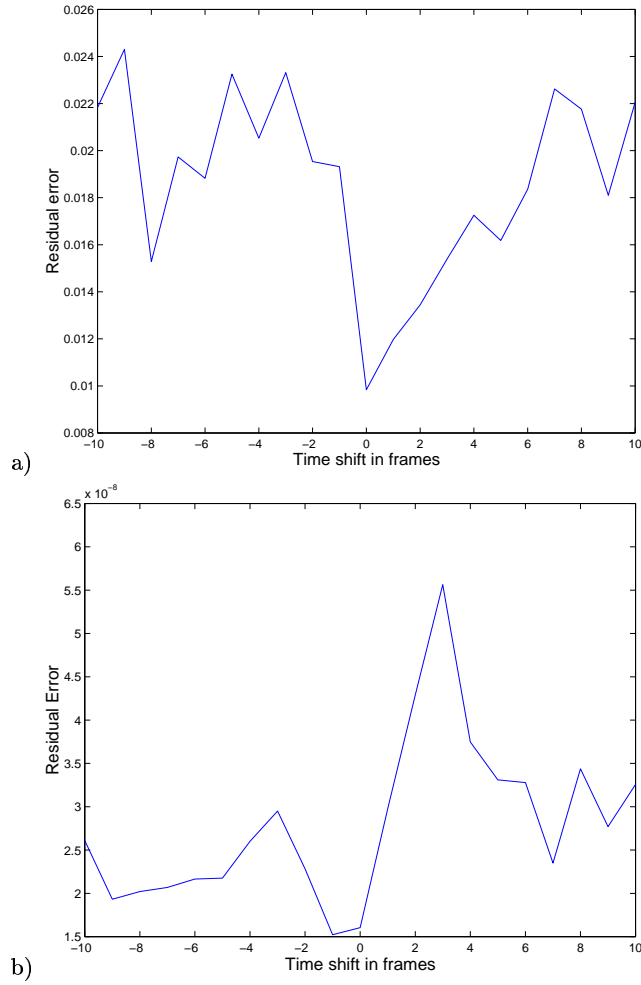
## 7 Summary and Future Work

We have analyzed self calibration of rigs with varying internal parameters, when no correspondences are available between the cameras. The only assumption used for the affine calibration, was that the angle between the viewing directions of the cameras is known.

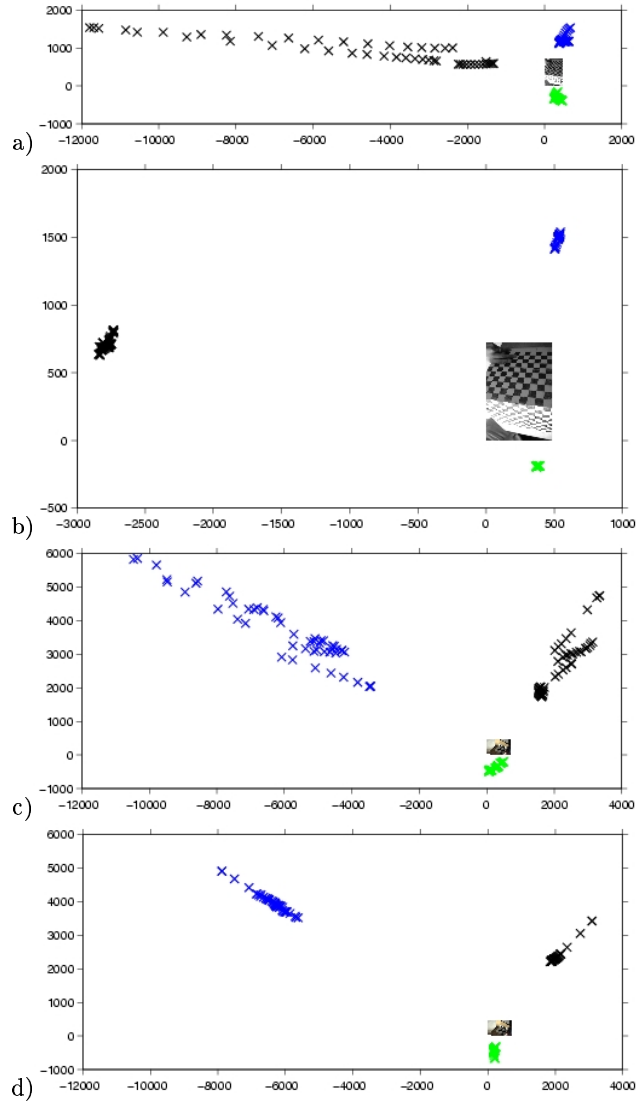
We presented constraints for general angles, and solved specific cases of parallel, opposite and orthogonal angles by extracting affine invariants.

Future work can be solving similar cases by deriving metric invariants, e.g.:

- Solving the case of arbitrary angles, with or without knowing the angle.
- Assuming that the distances between the centers of projections of the cameras remain fixed during the motion.



**Fig. 1.** Sequences synchronization for cameras viewing opposite directions (Fig. 1-a) and for cameras viewing orthogonal directions (Fig. 1-b). The residual error of the estimation matrix is presented as a function of the temporal shift between the sequences, where 0 shift corresponds to the manual integer estimation of the real shift. The residual error for the orthogonal case is averaged over four random choices of the camera matrix  $O$ .



**Fig. 2.** Mapping vanishing points by the homographies through the plane at infinity extracted by the proposed algorithm. a) The original vanishing points, opposite viewing directions. b) The mapped vanishing points, opposite viewing directions. c) The original vanishing points, orthogonal viewing directions. d) The mapped vanishing points, orthogonal viewing directions. The size of the images in illustrations a,b and c,d visualize the scale differences between the coordinate axes.



a1)



a2)



b1)



b2)



c1)



c2)

**Fig. 3.** Using the computed homographies through the planes at infinity to generate a virtual motion of pure translation. Figures b1,b2 contain the same image, to which the input images were warped. Figures a1,c1 to the left are the original input images. Figures a2,c2 to the right are the results of warping a1,c1 by the respective homographies through the plane at infinity.

We hope that even if such invariants are not compact, they may find use in some application such as cameras synchronization.

We plan to implement such algorithms for self calibration on “domes” containing cameras with fixed orientations and varying Zoom/Focus.

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