Problem #100

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Summary: Design new termination methods based on the gap-embedding theorems of Friedman and Kriz.

Harvey Friedman [Sim85] modified Kruskal's Tree Theorem to restrict labels that appear along the path between the images of adjacent nodes to what is called *gap embedding*. Whereas Friedman's result applied only to labellings with the natural numbers, Igor Kříž [Kš9] extended it to arbitrary ordinal labellings. See also [Gor90]. The question is whether new and useful termination methods can be based on these gap-embedding theorems. One step in this directions is [Oga95].

This problem is related to Problem #73.

Bibliography

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