

Homework 0

*Lecturer: Ronitt Rubinfeld**Due Date: November 10, 2014*

Homework guidelines: The following problems are for your understanding. Do not turn it in, but make sure you can solve it.

1. Show that given any algorithm A that runs in time $T(n)$ on inputs of size n with probability of error $1/4$, one can convert it into a new algorithm B that runs in time $O(T(n) \log 1/\beta)$ with probability of error at most β . (Hint: run A $O(\log 1/\beta)$ times and take the majority answer. Use Chernoff bounds.)
2. You are given an approximation scheme \mathcal{A} for f such that $\Pr[\frac{f(x)}{1+\epsilon} \leq \mathcal{A}(x) \leq f(x)(1+\epsilon)] \geq 3/4$, and \mathcal{A} runs in time polynomial in $1/\epsilon, |x|$. Construct an approximation scheme \mathcal{B} for f such that $\Pr[\frac{f(x)}{1+\epsilon} \leq \mathcal{B}(x) \leq f(x)(1+\epsilon)] \geq 1 - \delta$, and \mathcal{B} runs in time polynomial in $\frac{1}{\epsilon}, |x|, \log \frac{1}{\delta}$.
3. (Coupon Collector Problem). Given a die with n sides. What is the expected number of times you need to roll the die in order to see each of the n sides? (Hint: Given that you saw i sides, how many times do you need to roll the die to see the $(i + 1)^{st}$ side? Then use linearity of expectation.)