

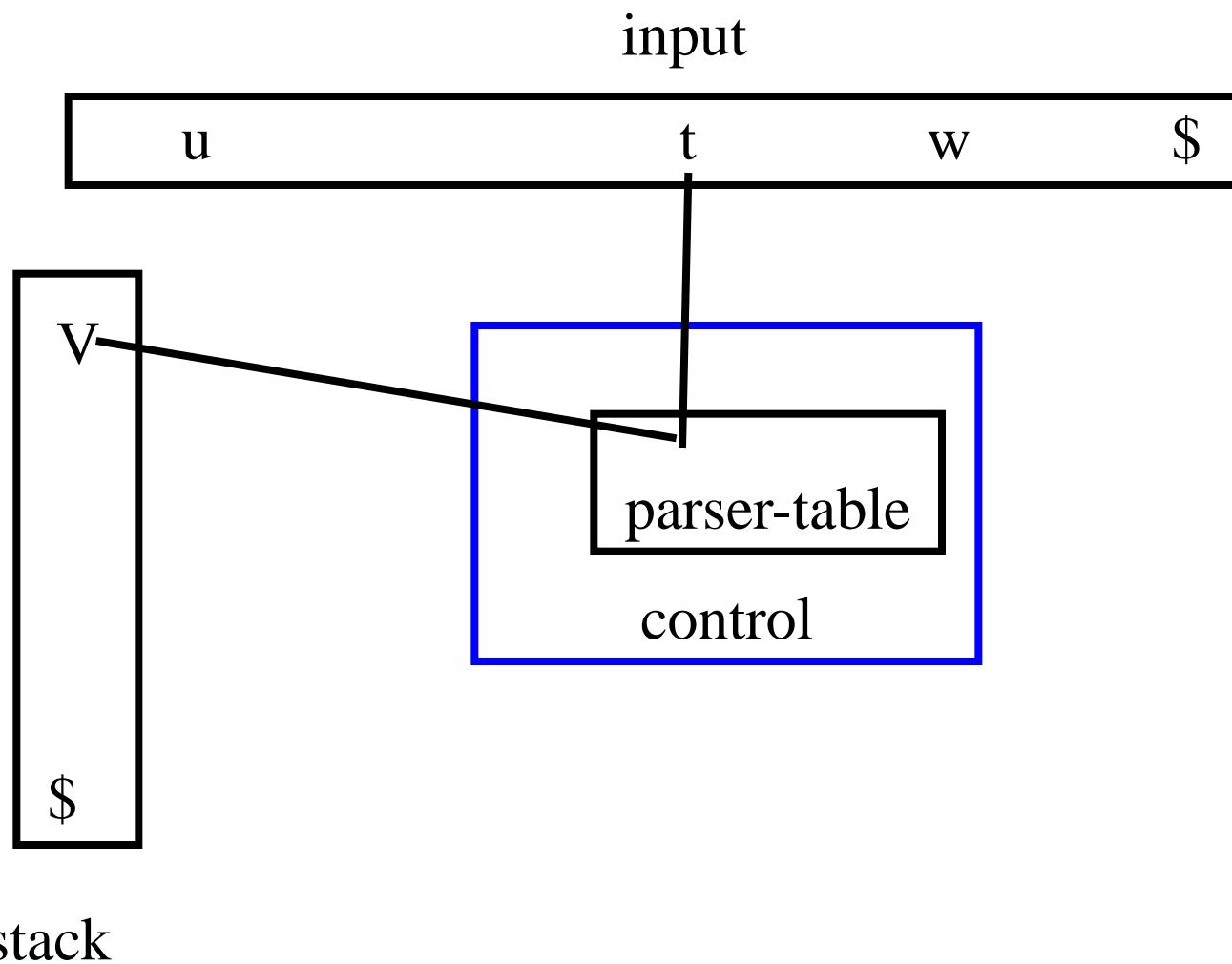
# Syntax Analysis

## Mooly Sagiv

<http://www.cs.tau.ac.il/~msagiv/courses/wcc13.html>

Textbook:Modern Compiler Design  
Chapter 2.2 (Partial)

# Pushdown Automaton



# A motivating example

- Create a desk calculator
- Challenges
  - Non trivial syntax
  - Recursive expressions (semantics)
    - Operator precedence

# Solution (lexical analysis)

```
import java_cup.runtime.*;
%%
%cup
%eofval{
    return sym.EOF;
}
NUMBER=[0-9] +
%%
"+"
{ return new Symbol(sym.PLUS); }

"-"
{ return new Symbol(sym_MINUS); }

"**"
{ return new Symbol(sym.MULT); }

"/"
{ return new Symbol(sym.DIV); }

"("
{ return new Symbol(sym.LPAREN); }

")"
{ return new Symbol(sym.RPAREN); }

{NUMBER} {
    return new Symbol(sym.NUMBER, new Integer(yytext()));
}

\n { }
. { }
```

- Parser gets terminals from the Lexer

```

terminal Integer NUMBER;
terminal PLUS,MINUS,MULT,DIV;
terminal LPAREN, RPAREN;
terminal UMINUS;
non terminal Integer expr;
precedence left PLUS, MINUS;
precedence left DIV, MULT;
Precedence left UMINUS;
%%

expr ::= expr:e1 PLUS expr:e2
      { : RESULT = new Integer(e1.intValue() + e2.intValue()); : }
      | expr:e1 MINUS expr:e2
      { : RESULT = new Integer(e1.intValue() - e2.intValue()); : }
      | expr:e1 MULT expr:e2
      { : RESULT = new Integer(e1.intValue() * e2.intValue()); : }
      | expr:e1 DIV expr:e2
      { : RESULT = new Integer(e1.intValue() / e2.intValue()); : }
      | MINUS expr:e1 %prec UMINUS
      { : RESULT = new Integer(0 - e1.intValue()); : }
      | LPAREN expr:e1 RPAREN
      { : RESULT = e1; : }
      | NUMBER:n
      { : RESULT = n; : }

```

# Solution (syntax analysis)

```
// input  
7 + 5 * 3
```

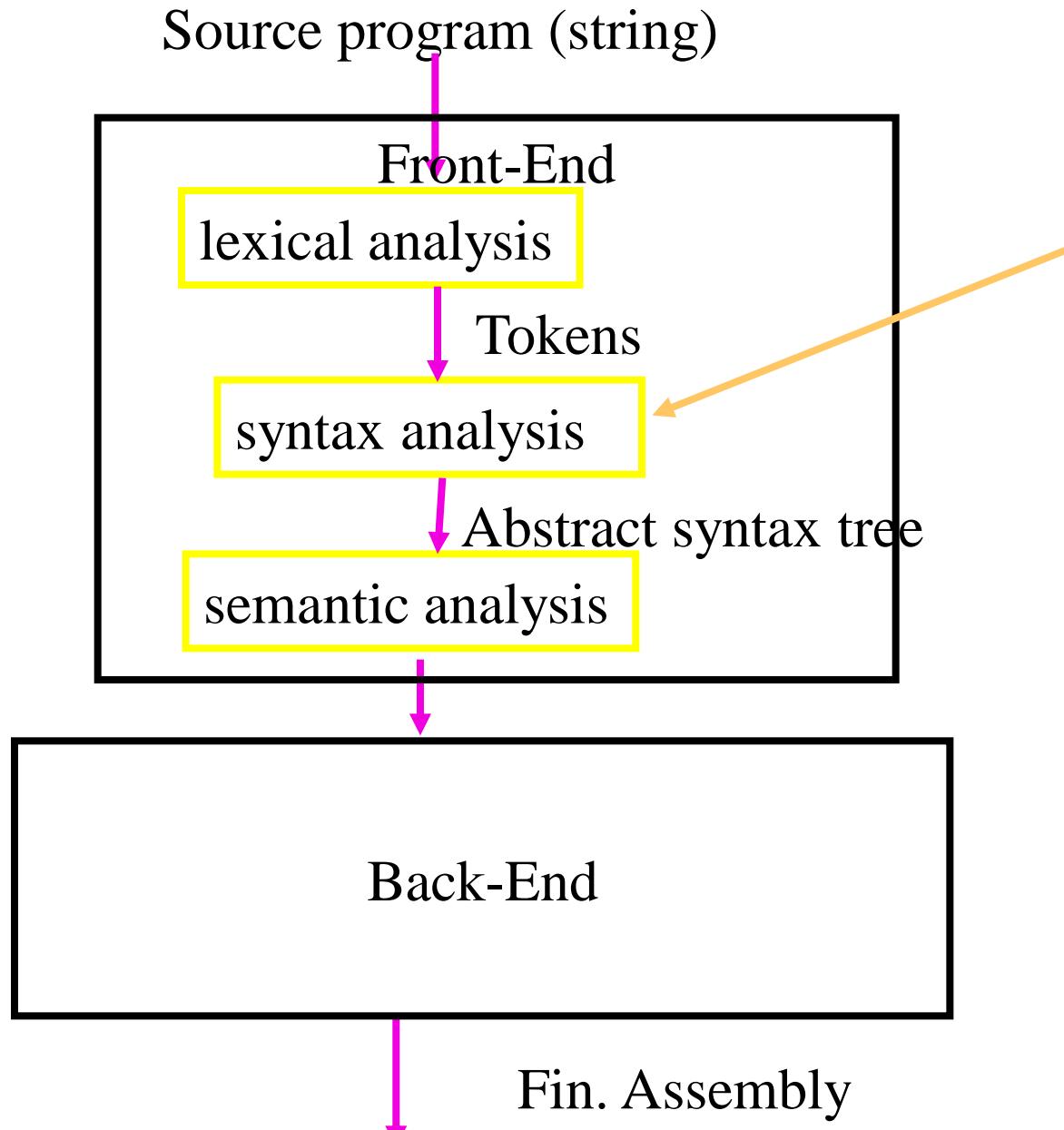
calc <input

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# Subjects

- The task of syntax analysis
- Automatic generation
- Error handling
- Context Free Grammars
- Ambiguous Grammars
- Top-Down vs. Bottom-Up parsing
- Simple Top-Down Parsing
- Bottom-Up Parsing (next lesson)

# Basic Compiler Phases



# Syntax Analysis (Parsing)

- input
  - Sequence of tokens
- output
  - Abstract Syntax Tree
- Report syntax errors
  - unbalanced parenthesizes
- [Create “symbol-table” ]
- [Create pretty-printed version of the program]
- In some cases the tree need not be generated  
(one-pass compilers)

# Handling Syntax Errors

- Report and locate the error
- Diagnose the error
- Correct the error
- Recover from the error in order to discover more errors
  - without reporting too many “strange” errors

# Example

```
a := a * ( b + c * d ;
```

# The Valid Prefix Property

- For every prefix tokens
  - $t_1, t_2, \dots, t_i$  that the parser identifies as legal:
    - there exists tokens  $t_{i+1}, t_{i+2}, \dots, t_n$  such that  $t_1, t_2, \dots, t_n$  is a syntactically valid program
- If every token is considered as single character:
  - For every prefix word u that the parser identifies as legal:
    - there exists w such that
      - $u.w$  is a valid program

# Error Diagnosis

- Line number
  - may be far from the actual error
- The current token
- The expected tokens
- Parser configuration

# Error Recovery

- Becomes less important in interactive environments
- Example heuristics:
  - Search for a semi-column and ignore the statement
  - Try to “replace” tokens for common errors
  - Refrain from reporting 3 subsequent errors
- Globally optimal solutions
  - For every input  $w$ , find a valid program  $w'$  with a “minimal-distance” from  $w$

# Why use context free grammars for defining PL syntax?

- Captures program structure (hierarchy)
- Employ formal theory results
- Automatically create “efficient” parsers

# Context Free Grammar (Review)

- What is a grammar
- Derivations and Parsing Trees
- Ambiguous grammars
- Resolving ambiguity

# Context Free Grammars

- Non-terminals
  - Start non-terminal
- Terminals (tokens)
- Context Free Rules  
 $<\text{Non-Terminal}> \rightarrow \text{Symbol Symbol} \dots \text{Symbol}$

# Example Context Free Grammar

- 1  $S \rightarrow S ; S$
- 2  $S \rightarrow id := E$
- 3  $S \rightarrow \text{print} (L)$
- 4  $E \rightarrow id$
- 5  $E \rightarrow \text{num}$
- 6  $E \rightarrow E + E$
- 7  $E \rightarrow (S, E)$
- 8  $L \rightarrow E$
- 9  $L \rightarrow L, E$

# Derivations

- Show that a sentence is in the grammar (valid program)
  - Start with the start symbol
  - Repeatedly replace one of the non-terminals by a right-hand side of a production
  - Stop when the sentence contains terminals only
- Rightmost derivation
- Leftmost derivation

# Example Derivations

1  $S \rightarrow S ; S$

2  $S \rightarrow id := E$

3  $S \rightarrow \text{print}(L)$

4  $E \rightarrow id$

5  $E \rightarrow \text{num}$

6  $E \rightarrow E + E$

7  $E \rightarrow (S, E)$

8  $L \rightarrow E$

9  $L \rightarrow L, E$

S

S ; S

S ; id := E

id := E ; id := E

id := num ; id := E

id := num ; id := E + E

id := num ; id := E + num

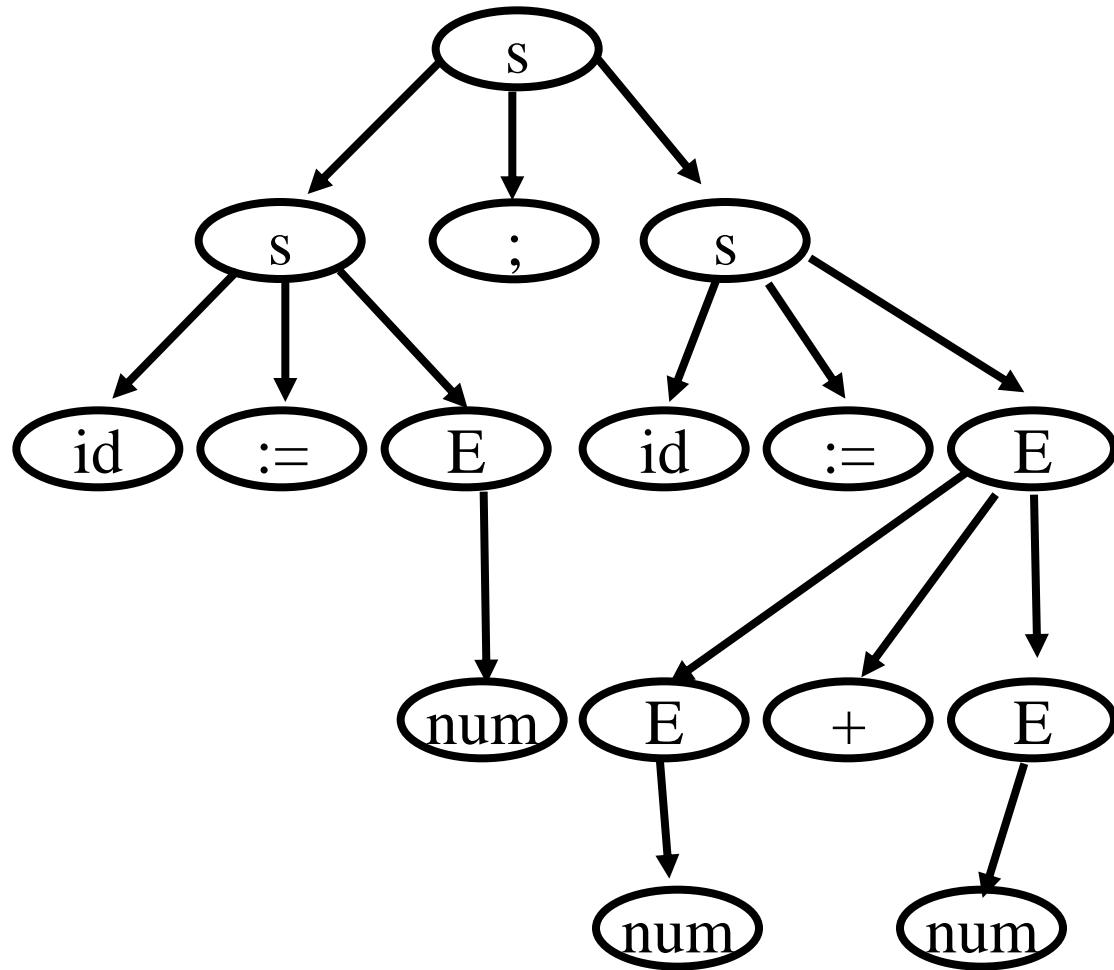
id := num ; id := num + num

# Parse Trees

- The trace of a derivation
- Every internal node is labeled by a non-terminal
- Each symbol is connected to the deriving non-terminal

# Example Parse Tree

S  
S ; S  
S ; id := E  
id := E ; id := E  
id := num ; id := E  
id := num ; id := E + E  
id := num ; id := E + num  
id := num ; id := num + num



# Ambiguous Grammars

- Two leftmost derivations
- Two rightmost derivations
- Two parse trees

# A Grammar for Arithmetic Expressions

1  $E \rightarrow E + E$

2  $E \rightarrow E * E$

3  $E \rightarrow id$

4  $E \rightarrow (E)$

# Drawbacks of Ambiguous Grammars

- Ambiguous semantics
- Parsing complexity
- May affect other phases

# Non Ambiguous Grammar for Arithmetic Expressions

Ambiguous grammar

- 1  $E \rightarrow E + E$
- 2  $E \rightarrow E * E$
- 3  $E \rightarrow id$
- 4  $E \rightarrow (E)$

- 1  $E \rightarrow E + T$
- 2  $E \rightarrow T$
- 3  $T \rightarrow T * F$
- 4  $T \rightarrow F$
- 5  $F \rightarrow id$
- 6  $F \rightarrow (E)$

# Non Ambiguous Grammars for Arithmetic Expressions

Ambiguous grammar

$$1 \quad E \rightarrow E + E$$

$$2 \quad E \rightarrow E * E$$

$$3 \quad E \rightarrow id$$

$$4 \quad E \rightarrow (E)$$

$$1 \quad E \rightarrow E + T$$

$$2 \quad E \rightarrow T$$

$$3 \quad T \rightarrow T * F$$

$$4 \quad T \rightarrow F$$

$$5 \quad F \rightarrow id$$

$$6 \quad F \rightarrow (E)$$

$$1 \quad E \rightarrow E * T$$

$$2 \quad E \rightarrow T$$

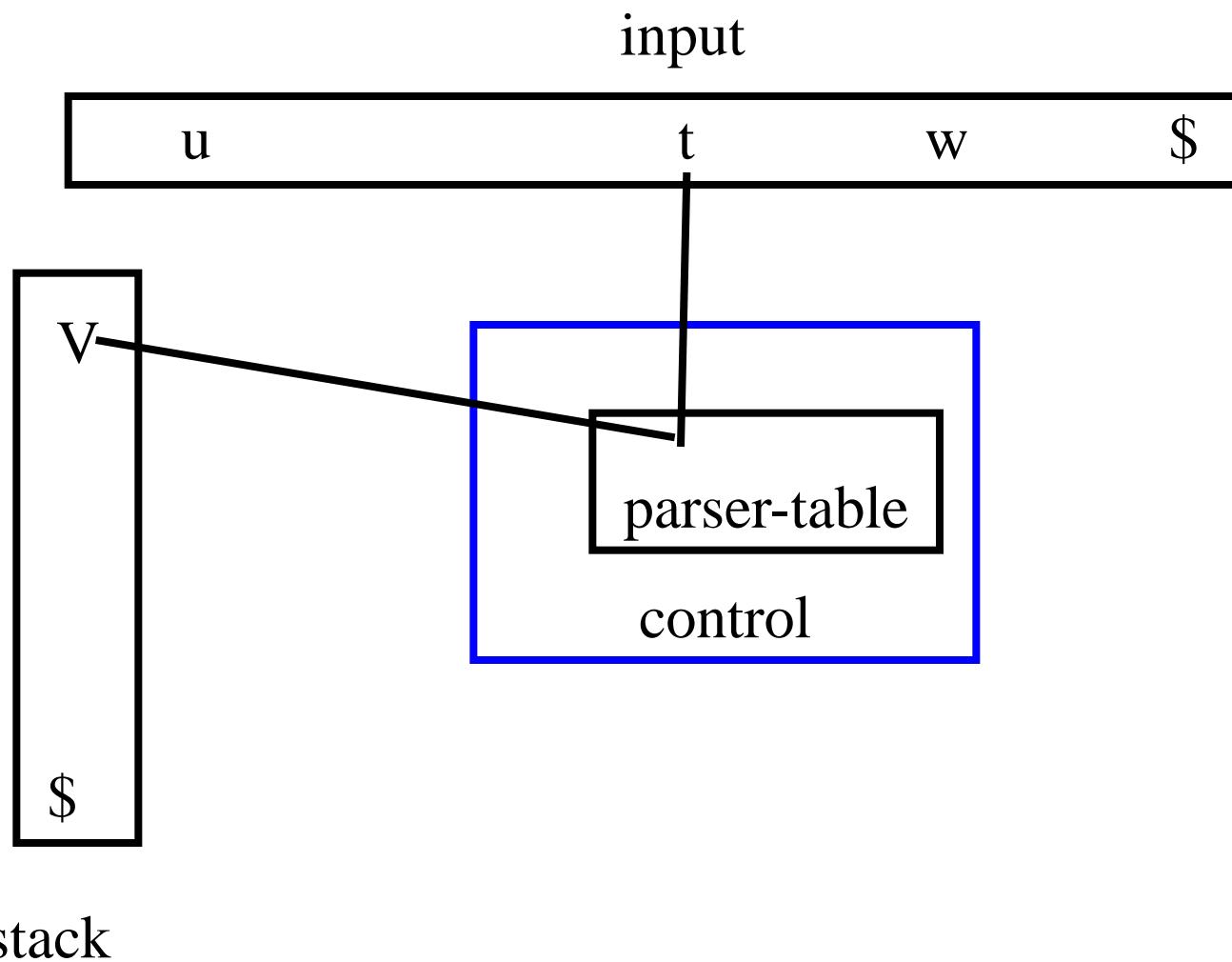
$$3 \quad T \rightarrow F + T$$

$$4 \quad T \rightarrow F$$

$$5 \quad F \rightarrow id$$

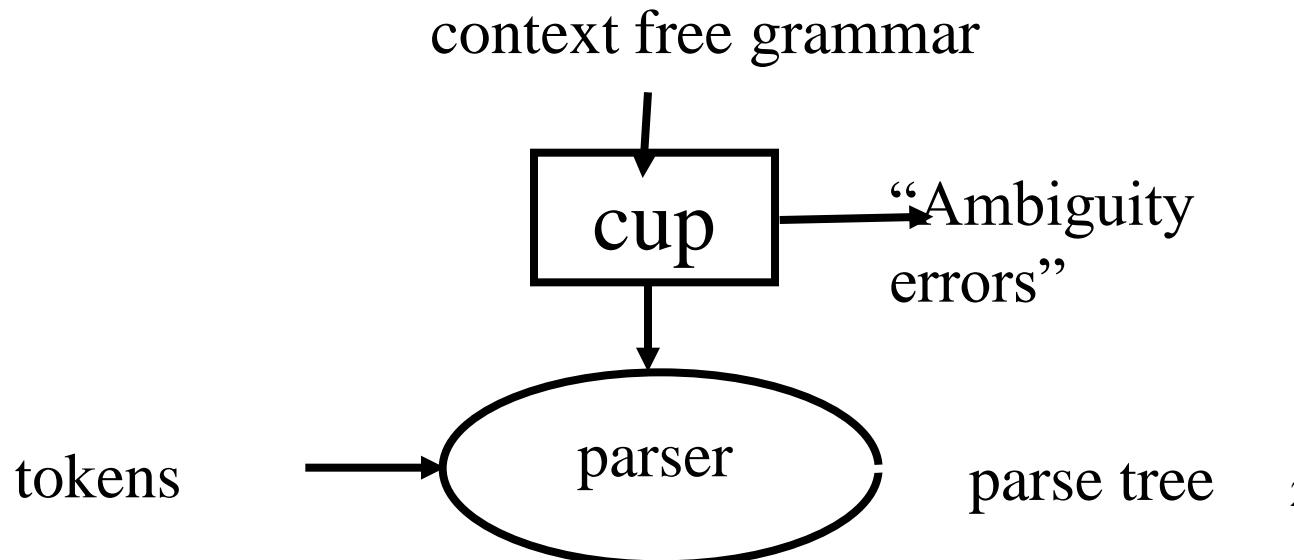
$$6 \quad F \rightarrow (E)$$

# Pushdown Automaton

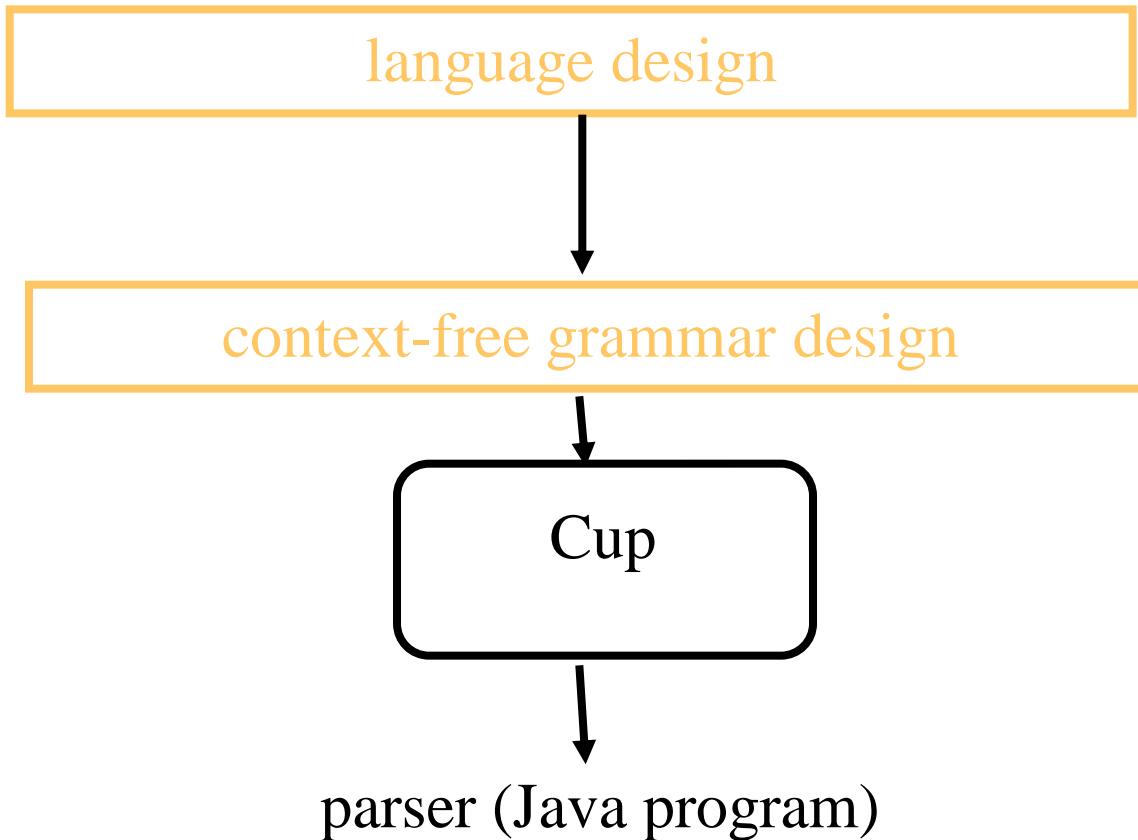


# Efficient Parsers

- Pushdown automata
- Deterministic
- Report an error as soon as the input is not a prefix of a valid program
- Not usable for all context free grammars



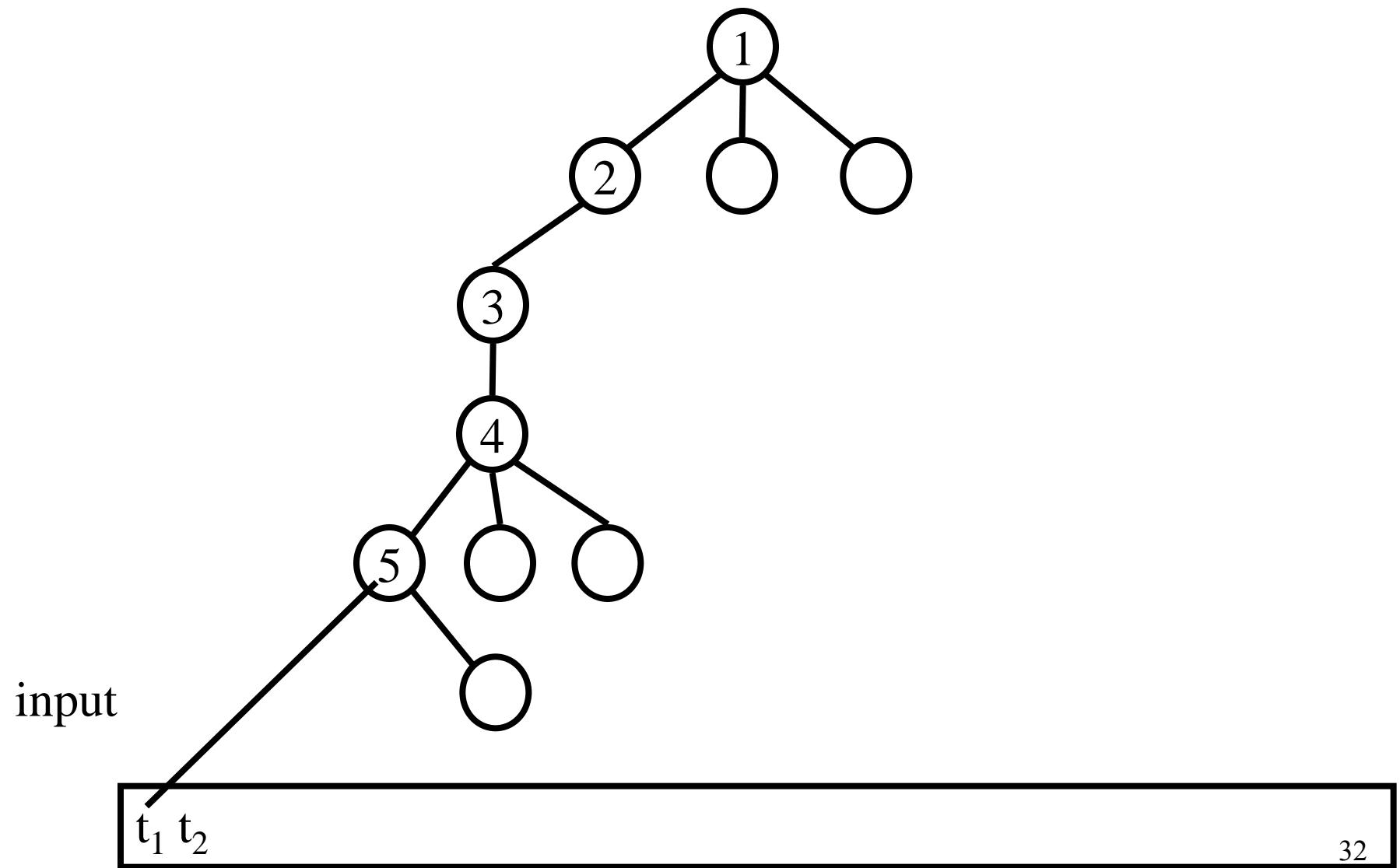
# Designing a parser



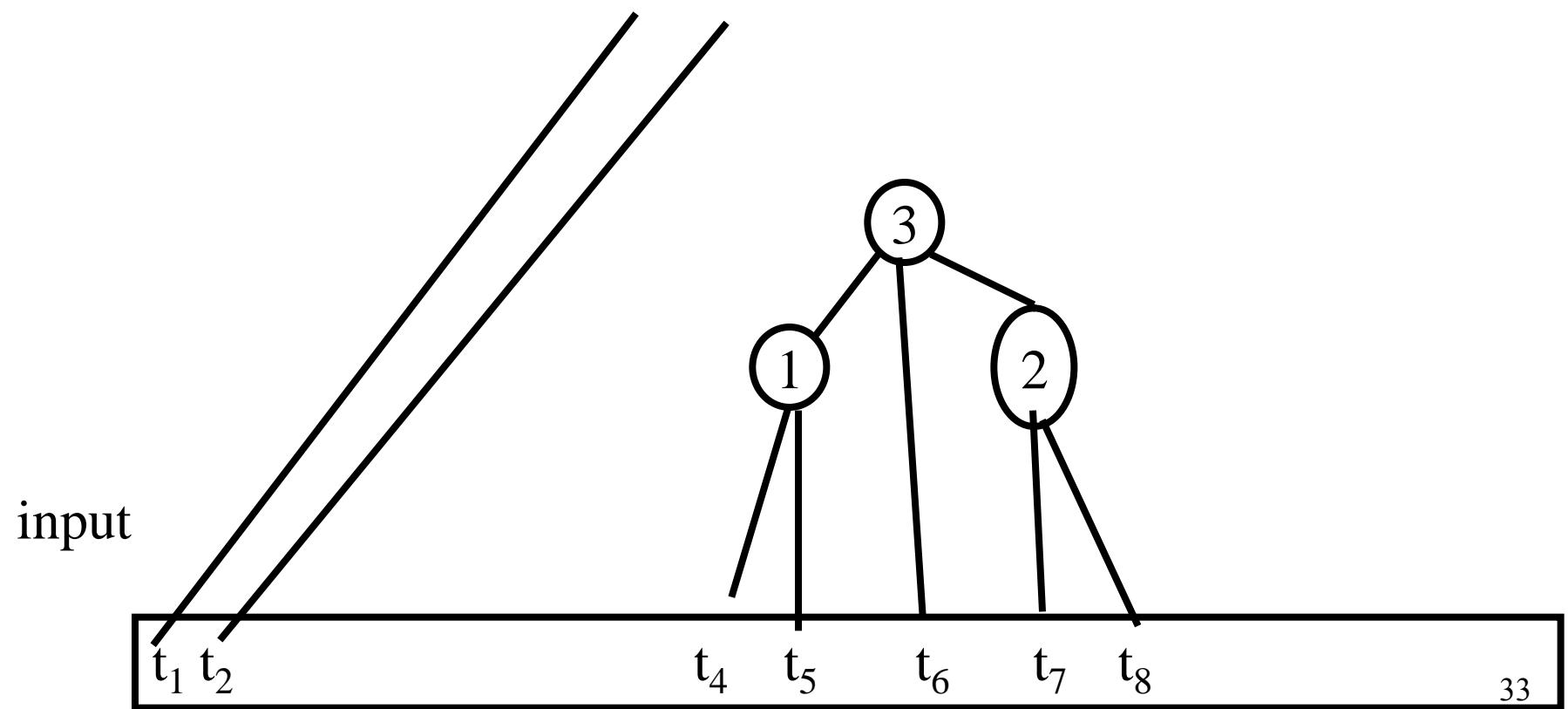
# Kinds of Parsers

- Top-Down (Predictive Parsing) LL
  - Construct parse tree in a top-down manner
  - Find the leftmost derivation
  - For every non-terminal and token **predict** the next production
  - Preorder tree traversal
- Bottom-Up LR
  - Construct parse tree in a bottom-up manner
  - Find the rightmost derivation in a reverse order
  - For every potential right hand side and token decide when a production is found
  - Postorder tree traversal

# Top-Down Parsing



# Bottom-Up Parsing



# Example Grammar for Predictive LL Top-Down Parsing

expression → digit | ‘(‘ expression operator expression ‘)’

operator → ‘+’ | ‘\*’

digit → ‘0’ | ‘1’ | ‘2’ | ‘3’ | ‘4’ | ‘5’ | ‘6’ | ‘7’ | ‘8’ | ‘9’

```
static int Parse_Expression(Expression **expr_p) {  
    Expression *expr = *expr_p = new_expression();  
    /* try to parse a digit */  
    if (Token.class == DIGIT) {  
        expr->type='D'; expr->value=Token.repr-'0'; get_next_token();  
        return 1;    }  
    /* try parse parenthesized expression */  
    if (Token.class == '(') {  
        expr->type='P'; get_next_token();  
        if (!Parse_Expression(&expr->left)) Error("missing expression");  
        if (!Parse_Operator(&expr->oper)) Error("missing operator");  
        if (Token.class != ')') Error("missing )");  
        get_next_token();  
        return 1;    }  
    return 0;  
}
```

# Parsing Expressions

- Try every alternative production
  - For  $P \rightarrow A_1 A_2 \dots A_n | B_1 B_2 \dots B_m$
  - If  $A_1$  succeeds
    - Call  $A_2$
    - If  $A_2$  succeeds
      - Call  $A_3$
    - If  $A_2$  fails report an error
  - Otherwise try  $B_1$
- Recursive descent parsing
- Can be applied for certain grammars
- Generalization: LL1 parsing

```

int P(...) {
    /* try parse the alternative P → A1 A2 ... An */
    if (A1(...)) {
        if (!A2()) Error("Missing A2");
        if (!A3()) Error("Missing A3");
        ..
        if (!An()) Error(Missing An);
    }
    return 1;
}

/* try parse the alternative P → B1 B2 ... Bm */
if (B1(...)) {
    if (!B2()) Error("Missing B2");
    if (!B3()) Error("Missing B3");
    ..
    if (!Bm()) Error(Missing Bm);
}
return 1;
}
return 0;

```

# Bad Example for Top-Down Parsing

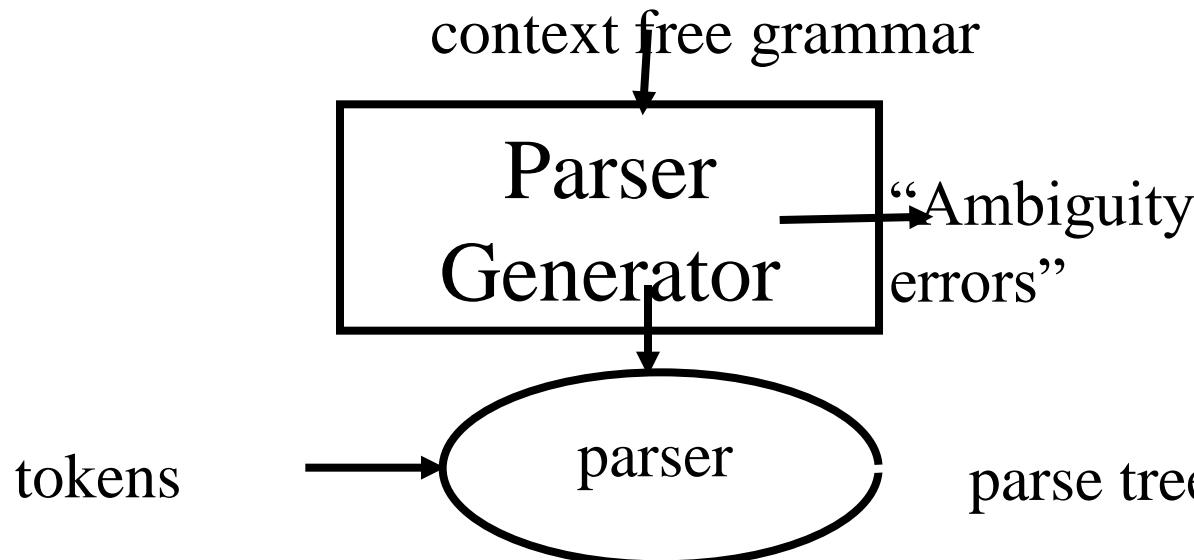
$S \rightarrow A\ c \mid B\ d$

$A \rightarrow a$

$B \rightarrow a$

# Efficient Top-Down Parsers

- Pushdown automata/Recursive descent
- Deterministic
- Report an error as soon as the input is not a prefix of a valid program
- Not usable for all context free grammars



# Top-Down Parser Generation

- First assume that all non-terminals are not nullable
  - No possibility for  $A \rightarrow^* \epsilon$
- Define for every string of grammar symbols  $\alpha$ 
  - $\text{First}(\alpha) = \{ t \mid \exists \beta: \alpha \rightarrow^* t\beta \}$
- The grammar is LL(1) if for every two grammar rules  $A \rightarrow \alpha$  and  $A \rightarrow \beta$ 
  - $\text{First}(\alpha) \cap \text{First}(\beta) = \emptyset$

# Bad Example for Top-Down Parsing

$S \rightarrow A\ c \mid B\ d$

$A \rightarrow a$

$B \rightarrow a$

$\alpha$	First( $\alpha$ )
a	{a}
c	{c}
d	{d}
A	{a}
B	{a}
S	{a}
Ac	{a}
Bd	{a}

# Computing First Sets

- For tokens  $t$ , define  $\text{First}(t) = \{t\}$
- For Non-terminals  $A$ , defines  $\text{First}(A)$  inductively
  - If  $A \rightarrow V\alpha$  then  $\text{First}(V) \subseteq \text{First}(A)$
- Can be computed iteratively
- For  $\alpha = V \beta$  define
$$\text{First}(\alpha) = \text{First}(V)$$

# Computing First Iteratively

For each token  $t$ ,  $\text{First}(t) := \{t\}$

For each non-terminal  $A$ ,  $\text{First}(A) := \{ \}$

while changes occur do

    if there exists a non-terminal  $A$  and

        a rule  $A \rightarrow V\alpha$  and

        a token  $t \in \text{First}(V)$  and

$t \notin \text{First}(A)$

    add  $t$  to  $\text{First}(A)$

# A Simple Example

$$E \rightarrow ( E ) \mid ID$$

# Constructing Top-Down Parser

- Construct First sets
- If the grammar is not LL(1) report an error
- Otherwise construct a predictive parser
  - A procedure for every non-terminals
  - For tokens  $t \in \text{First}(\alpha)$  apply the rule  $A \rightarrow \alpha$ 
    - Otherwise report an error

# Handling Nullable Non-Terminals

- Which tokens predicate empty derivations?
- For a non-terminal A define
  - $\text{Follow}(A) = \{ t \mid \exists \beta: S \xrightarrow{*} At\beta \}$
- Follow can be computed iteratively
- First need to be updated too

# Handling Nullable Non-Terminals

- For a non-terminal  $A$  define
  - $\text{Follow}(A) = \{ t \mid \exists \beta: S \xrightarrow{*} At\beta \}$
- For a rule  $A \rightarrow \alpha$ 
  - If  $\alpha$  is nullable then
$$\text{select}(A \rightarrow \alpha) = \text{First}(\alpha) \cup \text{Follow}(A)$$
    - Otherwise  $\text{select}(A \rightarrow \alpha) = \text{First}(\alpha)$
- The grammar is LL(1) if for every two grammar rules  $A \rightarrow \alpha$  and  $A \rightarrow \beta$ 
  - $\text{Select}(A \rightarrow \alpha) \cap \text{Select}(A \rightarrow \beta) = \emptyset$

# Computing First For Nullable Non-Terminals

For each token  $t$ ,  $\text{First}(t) := \{t\}$

For each non-terminal  $A$ ,  $\text{First}(A) = \{ \}$

while changes occur do

    if there exists a non-terminal  $A$  and

        a rule  $A \rightarrow V_1 V_2 \dots V_n \alpha$  and

$V_1, V_2, \dots, V_{n-1}$  are nullable

        a token  $t \in \text{First}(V_n)$  and

$t \notin \text{First}(A)$

    add  $t$  to  $\text{First}(A)$

# An Imperative View

- Create a table with  
 $\# \text{Non-Terminals} \times \# \text{Tokens}$   
Entries
- If  $t \in \text{select}(A \rightarrow \alpha)$  apply the rule “apply  
the rule  $A \rightarrow \alpha$ ”
- Empty entries correspond to syntax errors

# A Simple Example

$$E \rightarrow ( E ) \mid ID$$

	(	)	ID	\$
E	$E \rightarrow (E)$		$E \rightarrow id$	

# Left Recursion

- Left recursive grammar is never LL(1)
  - $A \rightarrow Aa \mid b$
- Convert into a right-recursive grammar
- Can be done for a general grammar
- The resulting grammar may or may not be LL(1)

# Predictive Parser for Arithmetic Expressions

- Grammar
  - 1  $E \rightarrow E + T$
  - 2  $E \rightarrow T$
  - 3  $T \rightarrow T * F$
  - 4  $T \rightarrow F$
  - 5  $F \rightarrow id$
  - 6  $F \rightarrow (E)$
- C-code?

# Computing First Sets for Expression Grammar

- Grammar
  - 1  $E \rightarrow E + T$
  - 2  $E \rightarrow T$
  - 3  $T \rightarrow T * F$
  - 4  $T \rightarrow F$
  - 5  $F \rightarrow id$
  - 6  $F \rightarrow (E)$

Modified First Sets	Rule	Select
$First(F) = \{id\}$	1	{id, ()}
$First(F) = \{id, ()\}$	2	{id, ()}
$First(T) = \{id, ()\}$	3	{id, ()}
$First(E) = \{id, ()\}$	4	{id, ()}
$First(E+T) = \{id, ()\}$	5	id
$First(T^*F) = \{id, ()\}$	6	(

# Select sets for modified expression grammar

- 1  $E \rightarrow T E'$
- 2  $E' \rightarrow \epsilon$
- 3  $E' \rightarrow + T E'$
- 4  $T \rightarrow F T'$
- 5  $T' \rightarrow \epsilon$
- 6  $T' \rightarrow * F T'$
- 7  $F \rightarrow id$
- 8  $F \rightarrow (E)$

	First Sets	Follow Sets	Rule	Select
1	$\text{First}(F) = \{\text{id}, ()\}$	$\text{Follow}(E) = \{\$, )\}$	1	$\{\text{id}, ()\}$
2	$\text{First}(T) = \{\text{id}, ()\}$	$\text{Follow}(E') = \{\$, )\}$	2	$\{\$\}, )\}$
3	$\text{First}(E) = \{\text{id}, ()\}$	$\text{Follow}(T) = \{+, ), \$\}$	3	$\{+\}$
4	$\text{First}(E') = \{+\}$	$\text{Follow}(T') = \{+, ), \$\}$	4	$\{\text{id}, ()\}$
5	$\text{First}(T') = \{* \}$	$\text{Follow}(F) = \{* , +, ), \$\}$	5	$\{*, +, (), \$\}$
6	$\text{First}(T E') = \{\text{id}, ()\}$		6	$\{* \}$
7	$\text{First}(\epsilon) = \{\}$		7	$\{\text{id}\}$
8	$\text{First}(+ T E') = \{+\}$		8	$\{()\}$
	$\text{First}(F T) = \{\text{id}, ( )\}$			
	$\text{First}(* F T') = \{* \}$			
	$\text{First}(id) = \{\text{id}\}$			
	$\text{First}(( E )) = \{()\}$			

# Summary

- Context free grammars provide a natural way to define the syntax of programming languages
- Ambiguity may be resolved
- Predictive parsing is natural
  - Good error messages
  - Natural error recovery
  - But not expressive enough
- Bottom-up parsing is more expressive