

# Compiling Functional Programs

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Chapter 7

<http://www.cs.tau.ac.il/~msagiv/courses/wcc10.html>

# Main features of Haskell

- No side effects
  - Referential Transparency
- List comprehension
- Pattern matching
- Higher order functions
  - Curried notions
- Polymorphic typing
- Lazy evaluation

# Factorial in Haskell vs. C

```
fac 0 = 1  
fac n = n * fac (n - 1)
```

```
int fac(int n) {  
    int product = 1;  
    while (n > 0) {  
        product *= n ;  
        n --;  
    }  
    return product;  
}
```

# Function Application

- Concise syntax
- No argument parentheses
  - $f\ 11\ 13$
- Function application is left associative and has higher precedence than any operator
  - $g\ g\ n = (g\ g)\ n$
  - $g\ n + 1 = (g\ n) + 1$

# Offside rule

- Layout characters matter to parsing
  - divide  $x \ 0 = \text{inf}$
  - divide  $x \ y = x / y$
- Everything below and right of  $=$  in equations defines a new scope
- Applied recursively
  - fac  $n = \text{if } (n == 0) \text{ then } 1 \text{ else prod } n \ (n-1)$
  - where
    - prod  $\text{acc } n = \text{if } (n == 0) \text{ then } \text{acc}$
    - else  $\text{prod } (\text{acc} * n) \ (n - 1)$
- Lexical analyzer maintains a stack

# Lists

- Part of all functional programs since Lisp
- Empty list [] = Nil
- [1]
- [1, 2, 3, 4]
- [4, 3, 7, 7, 1]
- ["red", "yellow", "green"]
- [1 .. 10]
- Can be constructed using ":" infix operator
  - $[1, 2, 3] = (1 : (2 : (3 : [])))$
  - $\text{range } n \ m = \text{if } n > m \text{ then } []$   
   $\text{else } (n : \text{range } (n+1) \ m)$

# List Comprehension

- Inspired by set comprehension

$$S = \{n^2 \mid n \in \{1, \dots, 100\} \wedge \text{odd } n\}$$

- Haskell code

```
s = [n^2 | n <- [1..100], odd n]
```

“n square such that n is an element of [1..100] and n is odd”

- Qsort in Haskell

```
qsort [] = []
```

```
qsort (x: xs) = qsort [y | y <- xs, y < x]
```

```
    ++ [x]
```

```
    ++ qsort[y | y <- xs, y >= x]
```

# Pattern Matching

- Convenient way to define recursive functions

- A simple example

fac 0 = 1

fac n = n \* fac (n-1)

- Equivalent code

fac n = if (n == 0) then 1

    else n \* fac (n -1)

- Another example

length [] = 0

length (x: xs) = 1 + length xs

- Equivalent code

length list = if (list == []) then 0

    else let

        x = head list

        xs = tail list

    in 1 + length xs



# Polymorphic Typing

- **Polymorphic** expression has many types
- Benefits:
  - Code reuse
  - Guarantee consistency
- The compiler infers that in  
length [] = 0  
length (x: xs) = 1 + length xs
  - length has the type [a] -> int  
length :: [a] -> int
- Example expressions
  - length [1, 2, 3] + length ["red", "yellow", "green"]
  - length [1, 2, "green"] // invalid list
- The user can optionally declare types
- Every expression has the **most general type**
- “boxed” implementations

# Referential Transparency

- Expressions in Haskell have no side effects
- Usually requires more space  
 $\text{add\_one []} = []$   
 $\text{add\_one (x xs)} = x + 1 : \text{add\_one xs}$
- Can be tolerated by garbage collection and smart compilers
- Input/Output operations can be also be defined using Monads

# Higher Order Functions

- Functions are first class objects
  - Passed as parameters
  - Returned as results

# Example Higher Order Function

- The differential operator

$$Df = f' \text{ where } f'(x) = \lim_{h \downarrow 0} (f(x+h)-f(x))/h$$

- In Haskell

`diff f = f_`

where

$$f_ x = (f (x +h) - f x) / h$$

$$h = 0.0001$$

- `diff :: (float -> float) -> (float -> float)`
- `(diff square) 0 = 0.0001`
- `(diff square) 0.0001 = 0.0003`
- `(diff (diff square)) 0 = 2`

# Currying

- Functions can be created by partially applying a function to some of its arguments
- $\text{deriv } f \ x = (f \ (x + h) - f \ x) / h$   
where  $h = 0.0001$
- $\text{deriv } f \ x == (\text{diff } f) \ x$
- Non semantic difference by Unary and n-ary functions
- $f \ e_1 \ e_2 \ \dots \ e_n = ({}^n((f \ e_1) \ e_2) \ \dots \ e_n)$
- Complicates compilation

# Lazy vs. Eager Evaluation

- When to evaluate expressions
- A simple example  
let const c x = c in const 1 (2 + 3)
- In eager evaluation  
const 1 (2 + 3)  $\infty$  const 1 5 = 1
- In lazy Evaluation (Haskel)  
const 1 (2 + 3)  $\infty$  1
- Another example  
let const c x = c in const 1 (2 / 0)

# Benefits of Lazy Evaluation

- Define streams  
main = take 100 [1 .. ]
- $\text{deriv } f \ x = \lim [(f (x + h) - f x) / h \mid h \leftarrow [1/2^n \mid n \leftarrow [1..]]]$   
where  $\text{lim } (a: b: \text{lst}) = \text{if } \text{abs}(a/b - 1) < \text{eps} \text{ then } b$   
else  $\text{lim } (b: \text{lst})$   
 $\text{eps} = 1.0 \text{ e-}6$
- Lower asymptotic complexity
- Language extensibility
  - Domain specific languages
- But some costs

# Functional Programming Languages

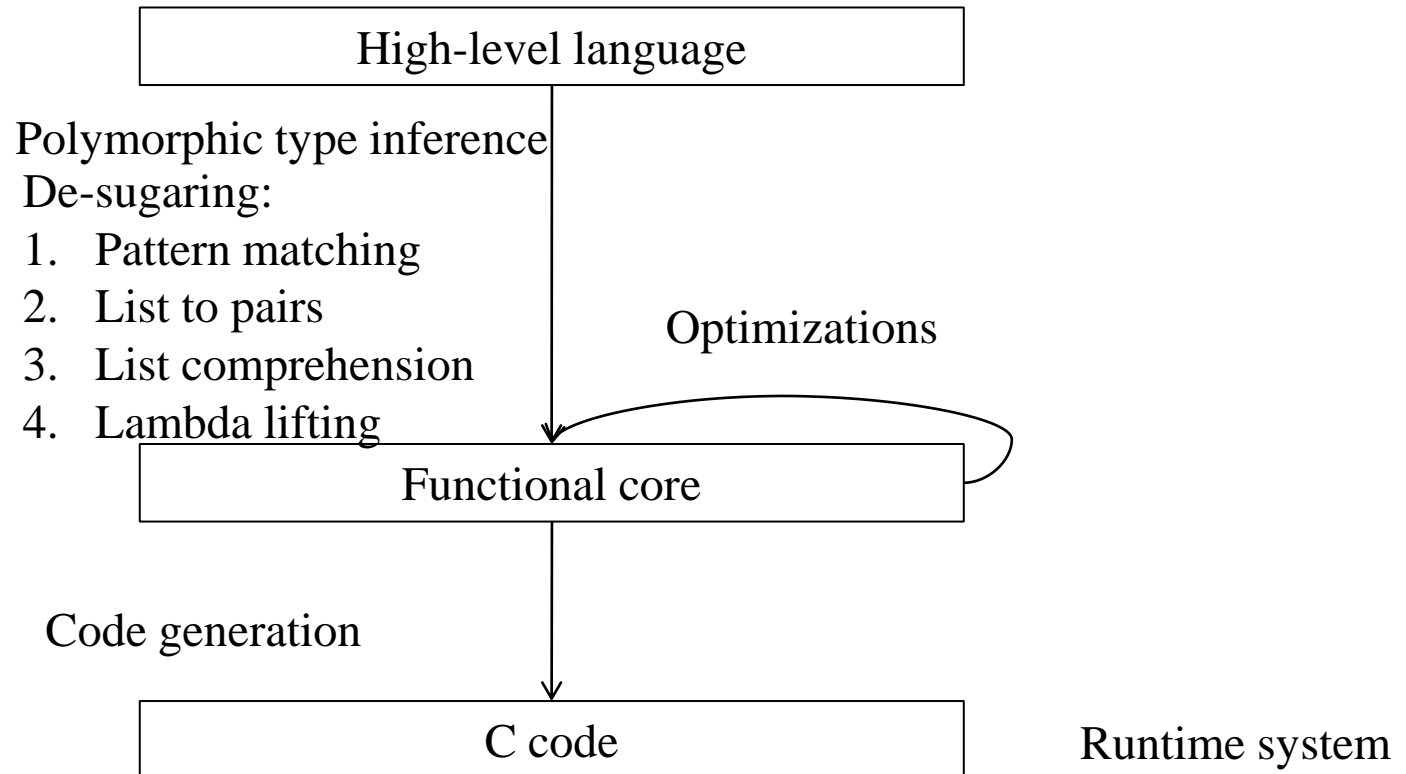
PL	types	evaluation	Side-effect
scheme	Weakly typed	Eager	yes
ML OCAML F#	Polymorphic strongly typed	Eager	References
Haskel	Polymorphic strongly typed	Lazy	None



# Compiling Functional Programs

Compiler Phase	Language Aspect
Lexical Analyzer	Offside rule
Parser	List notation List comprehension Pattern matching
Context Handling	Polymorphic type checking
Run-time system	Referential transparency Higher order functions Lazy evaluation

# Structure of a functional compiler

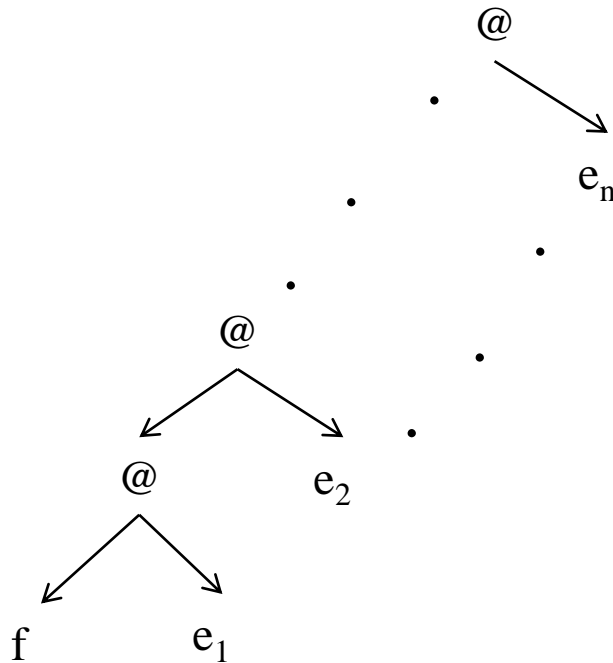


# Graph Reduction

- The runtime state of a lazy functional program can be represented as a direct graph
  - Nodes represent arguments in expressions
  - Edges between functions and argument
- An execution is simulated with a graph reduction
- Supports laziness and higher order functions

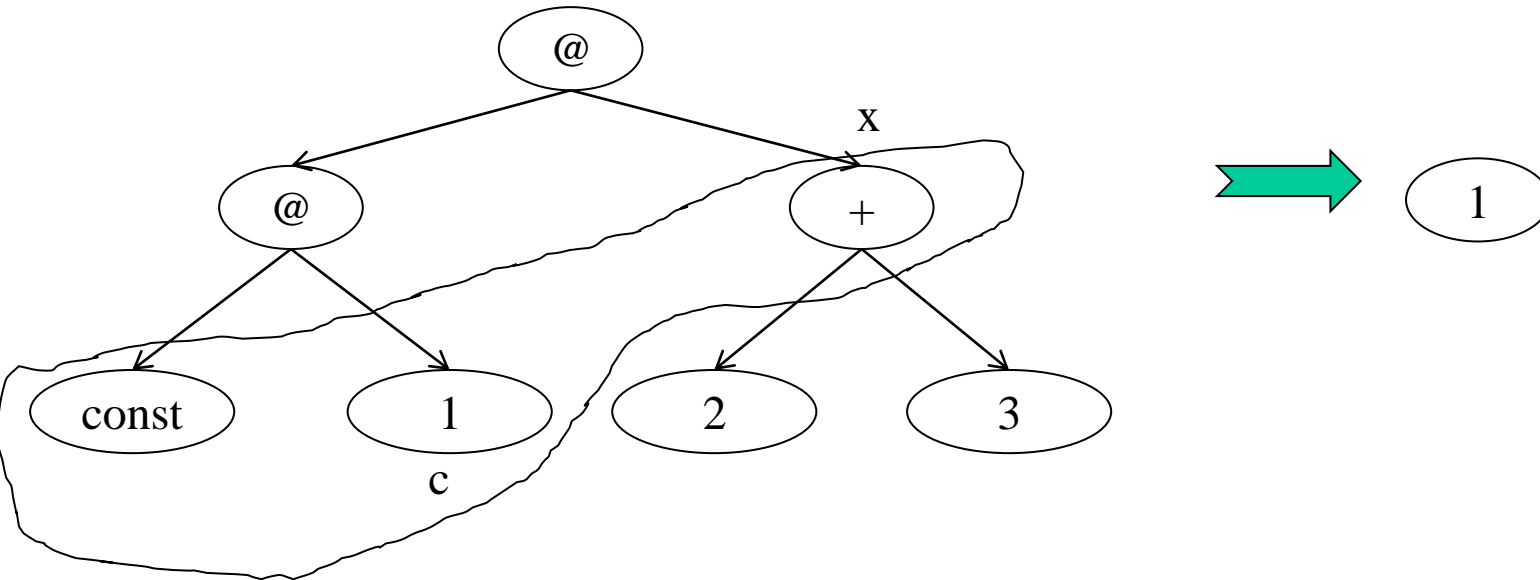
# Function Application

- $f e_1 e_2 \dots e_n = ({}^n((f e_1) e_2) \dots e_n)$   
 $= ({}^n((f @ e_1) @ e_2) \dots e_n)$



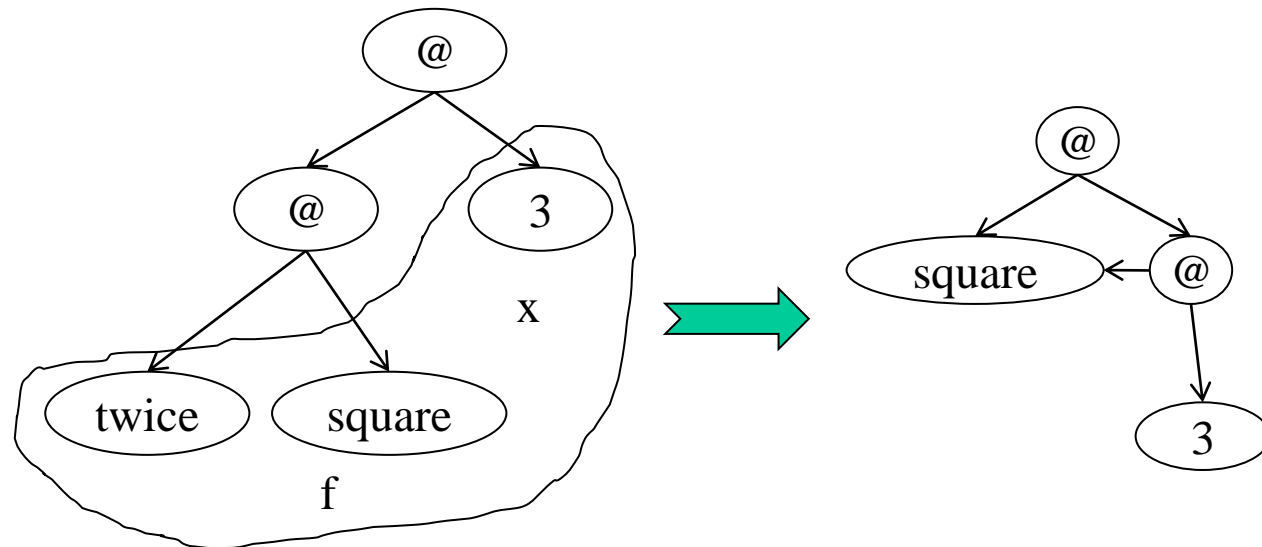
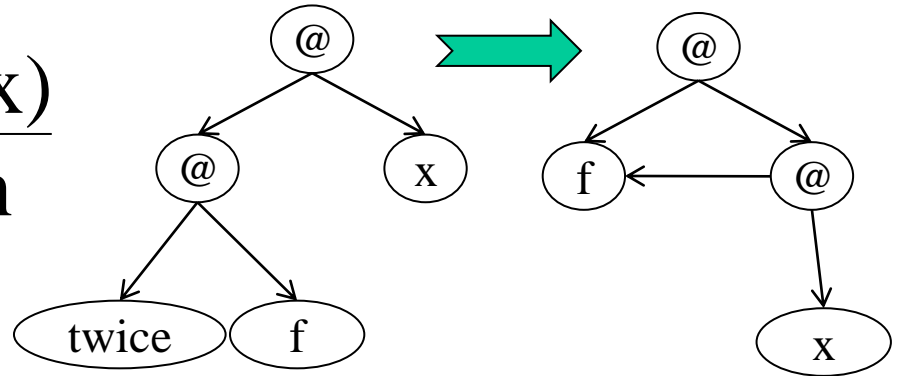
# A Simple Example

- `let const c x = c in const 1 (2 + 3)`



# Another Example

- let twice f x = f (f x)  
square n = n \* n  
in  
twice square 3



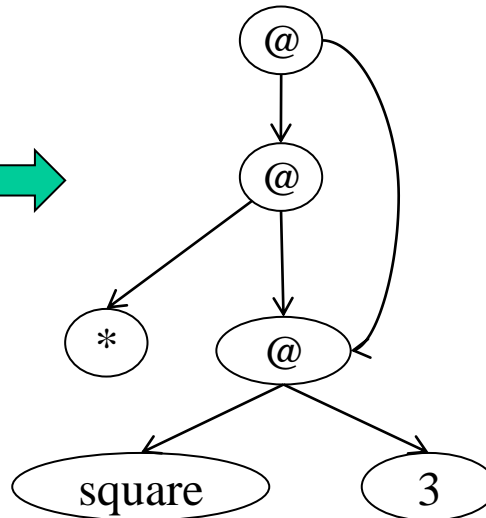
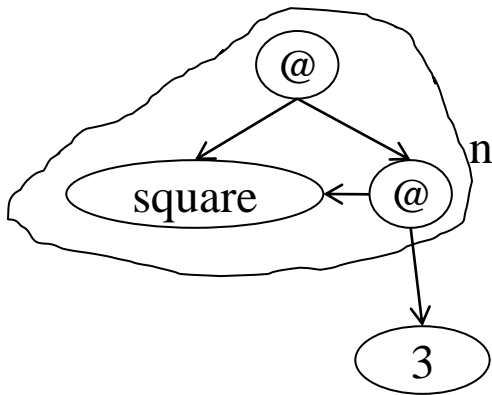
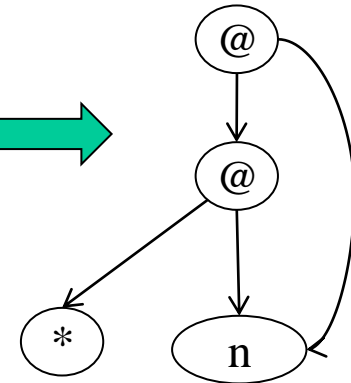
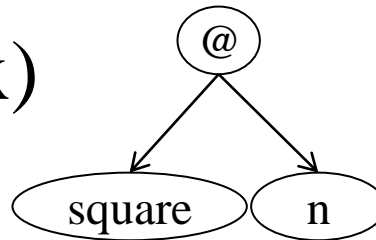
# Another Example (cont1)

- let  $\text{twice } f \ x = f (f \ x)$

$$\underline{\text{square } n = n * n}$$

in

twice square 3



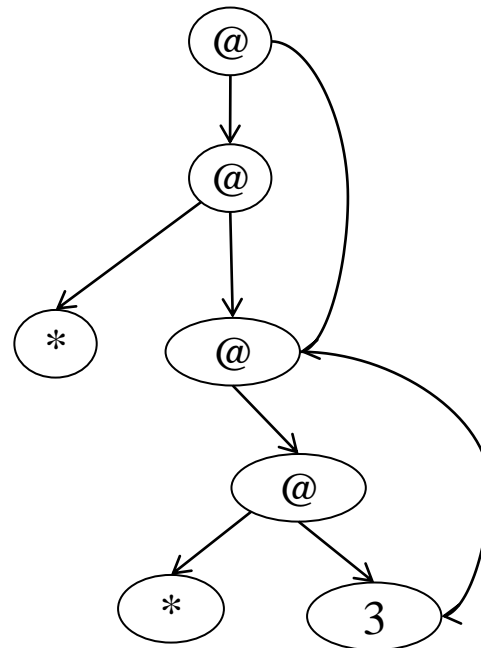
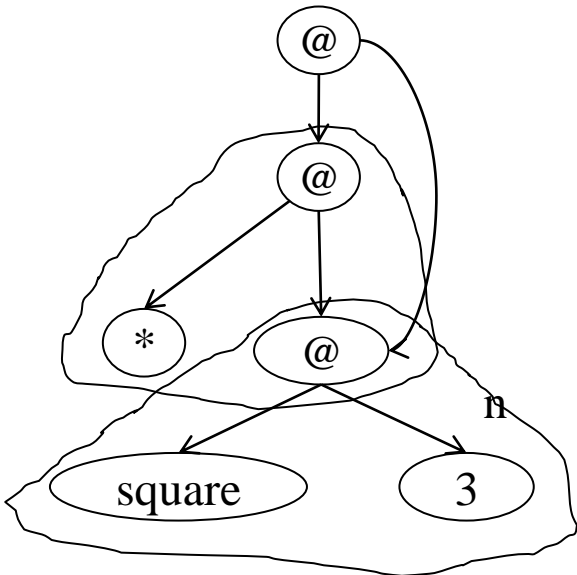
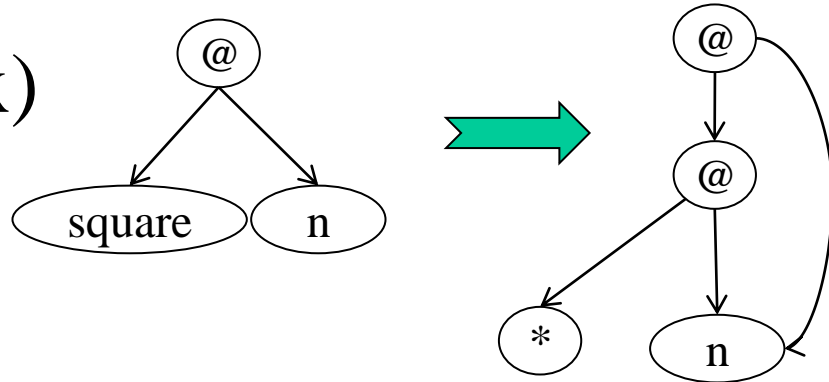
# Another Example (cont2)

- let twice f x = f (f x)

$$\underline{\text{square } n = n * n}$$

in

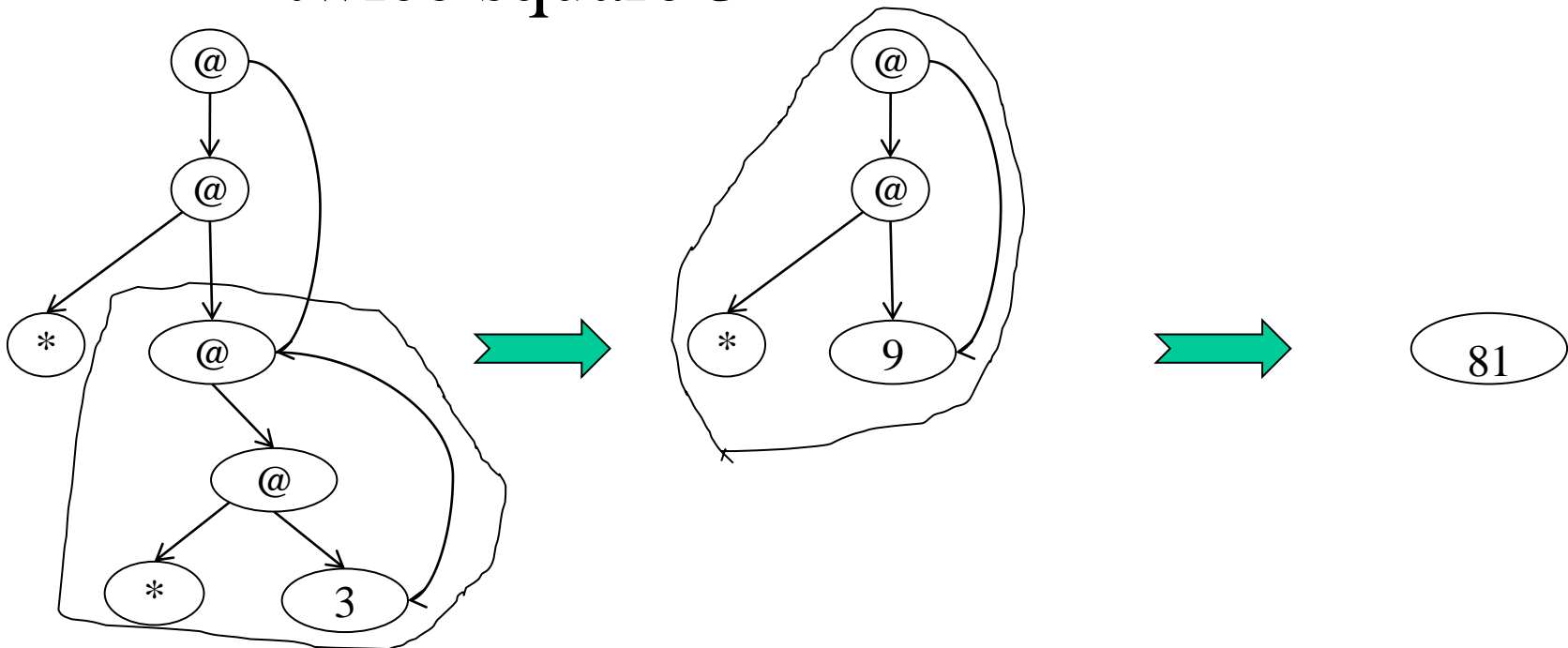
twice square 3





# Another Example (cont3)

- let twice f x = f (f x)  
square n = n \* n  
in  
twice square 3



# Reduction Order

- At every point in execution redexes can be selected
- Start at the root
- If the root is not application node print the result
- If the root is an application node  $\rightarrow$  its value is needed
  - Traverse the application spine to the left to find the function, say  $f$
  - Check if the application spine contains all the arguments for  $f$ 
    - No a Curried function is detected
    - Yes search and apply the redex

# The reduction Engine

- Usually implemented in C
- Apply redexes
- Use a stack to match arguments
- Use Eval to apply redexes using function pointers
- Built in functions are part of the runtime system
- User defined functions are mapped into C in a straightforward way using Eval function
- Significant runtime overhead

# C Header file

```
typedef enum {FUNC, NUM, NIL, CONS, APPL} node_type
typedef struct node *Pnode
typedef Pnode (*unary) (Pnode *arg)
struct function_descriptor {
    int arity;
    const char * name;
    unary code ;
};
struct node_type {
    node_type tag;
    union {
        struct function_descriptor func;
        int num;
        struct {Pnode hd, Pnode tl ;} cons
        struct {Pnode fun; Pnode arg;} appl;
    } nd;
}
extern Pnode Func(int arity, const char *name, unary code);
extern Pnode Nil(int num);
...
```

# Reducing the cost of graph reduction

- Shortcut reductions
- Detect lazy expressions which are always executed
  - Strict

# Optimizing the functional core

- Boxing analysis
- Tail call elimination
- Accumulator translation
- Strictness analysis

# Strictness Analysis

- A function is **strict** in an argument  $a$  if it needs the value of  $a$  in all executions
- Example  $\text{safe\_div } a \ b = \text{if } (b == 0) \text{ then } 0 \text{ else } a / b$ 
  - strict in  $b$
- Can be computed using dataflow equations

# Limitations

- Usually the generated C code can be reasonably efficient
- Current strictness analysis works poorly for user-defined data structures and higher order functions



# Summary

- Functional programs provide concise coding
- Compiled code compares with C code
- Successfully used in some commercial applications
  - F#, ERLANG
- Ideas used in imperative programs
- Less popular than imperative programs