

# Storage Management for Programming Languages

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# High level Programs vs. Executable Programs

Abstractions for productive programming

First order order functions

Higher order functions

Polymorphism

Abstract Data Types

Algebraic Data Types

Modules

Control abstractions

## Executable Code

```
00000000 <code_00000000>
00000000: push    rbp
00000001: mov     rbp, rsp
00000002: and    rsp, 0xffffffff
00000003: push   rdi
00000004: push   rsi
00000005: mov    rsi, rdi
00000006: call   sub_00000000
00000007: mov    rdi, ptr [rsi+0], offset 0x10000000
00000008: mov    rdi, ptr [rsi+0], 0
00000009: call   sub_00000000
0000000a:
0000000b:
0000000c:
0000000d:
0000000e:
0000000f:
00000010: <code_00000010>
00000010: jmp     rdi
00000011:
00000012:
00000013:
00000014:
00000015:
00000016:
00000017:
00000018:
00000019:
0000001a:
0000001b:
0000001c:
0000001d:
0000001e:
0000001f:
00000020: <code_00000020>
00000020: jmp     rdi
00000021:
00000022:
00000023:
00000024:
00000025:
00000026:
00000027:
00000028:
00000029:
0000002a:
0000002b:
0000002c:
0000002d:
0000002e:
0000002f:
00000030: <code_00000030>
00000030: mov    rdi, ptr [rdi+0], <code_00000030>
00000031: mov    rdi, ptr [rdi+0], <code_00000030>
00000032: mov    rdi, rdi
00000033: jmp     rdi
00000034:
00000035:
00000036:
00000037:
00000038:
00000039:
0000003a:
0000003b:
0000003c:
0000003d:
0000003e:
0000003f:
00000040: <code_00000040>
00000040: jmp     rdi
```

# Topics

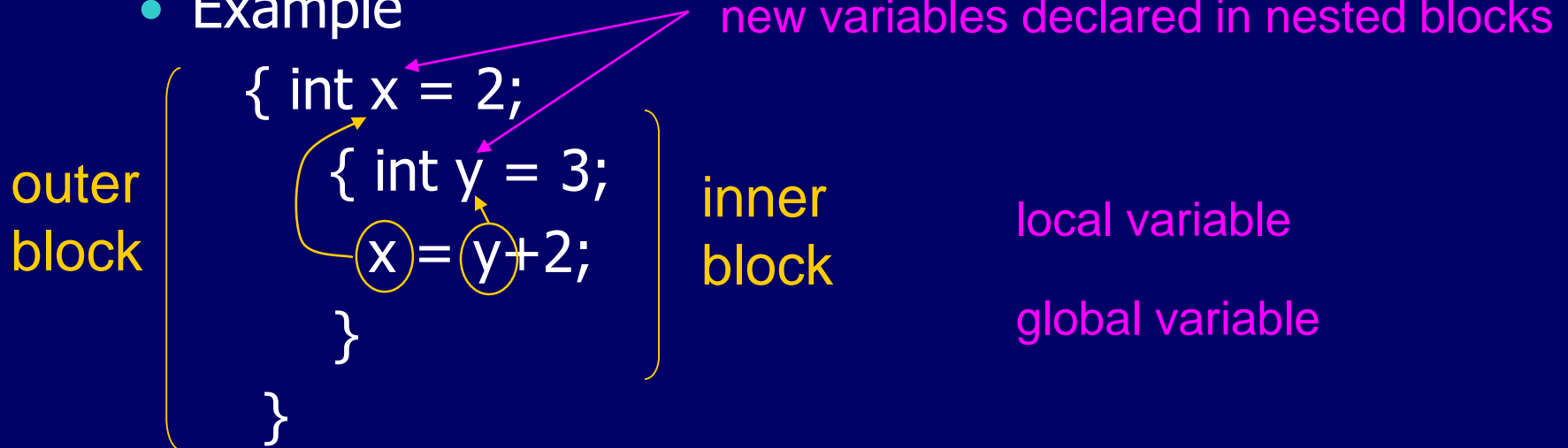
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- ◆ Block-structured languages and stack storage
- ◆ In-line Blocks
  - activation records
  - storage for local, global variables
- ◆ First-order functions
  - parameter passing
  - tail recursion and iteration
- ◆ Higher-order functions
  - deviations from stack discipline
  - language expressiveness => implementation complexity
- ◆ Garbage Collection

# Block-Structured Languages

## ◆ Nested blocks, local variables

- Example



- Storage management

- Enter block: allocate space for variables
- Exits block: some or all space may be deallocated

# Examples

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## ◆ Blocks in common languages

- C, ~~JavaScript~~ \* { ... }
- Algol begin ... end
- ML let ... in ...

## ◆ Two forms of blocks

- In-line blocks
- Blocks associated with functions or procedures

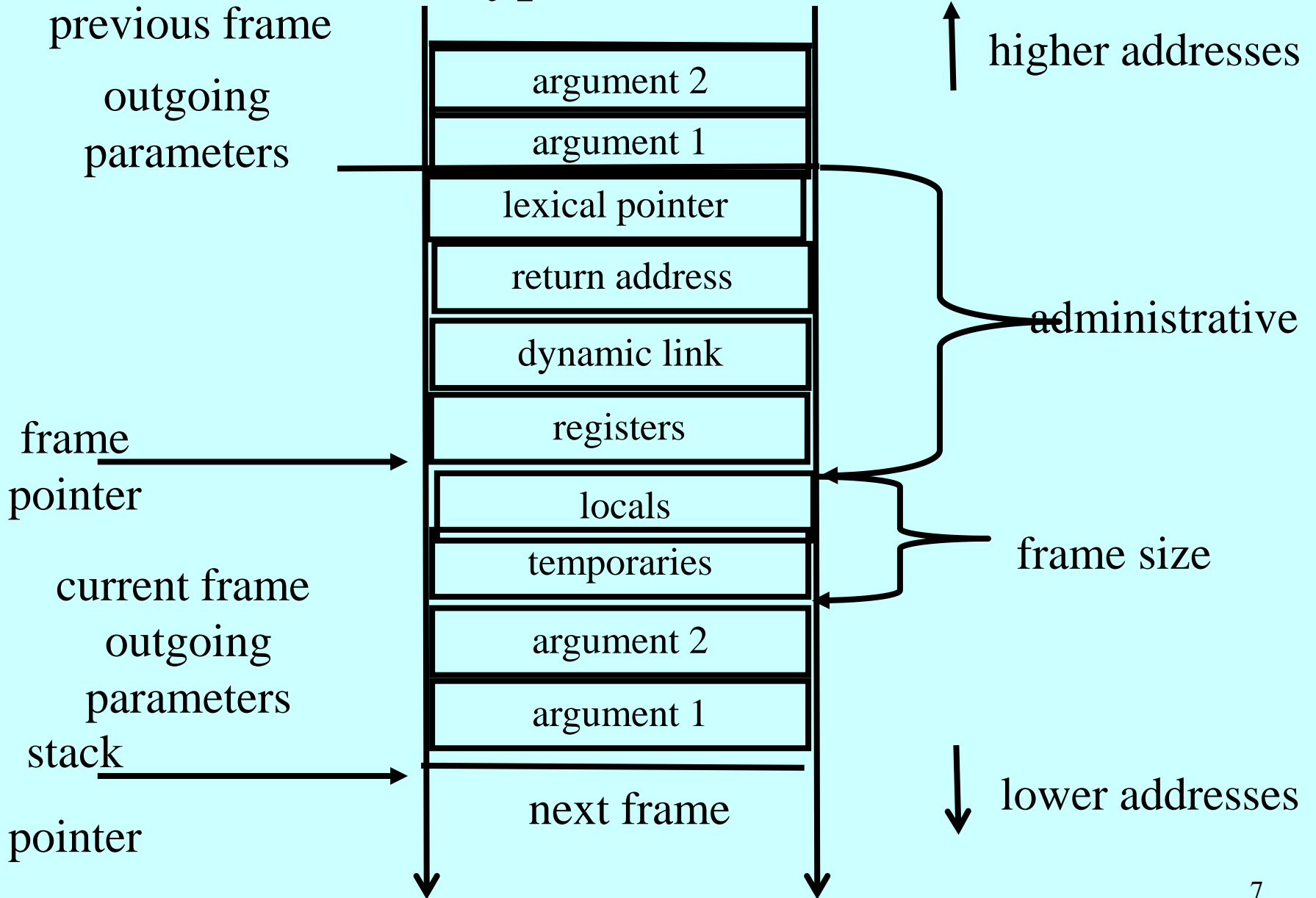
## ◆ Topic: block-based memory management, access to local variables, parameters, global variables

\* JavaScript functions provide blocks

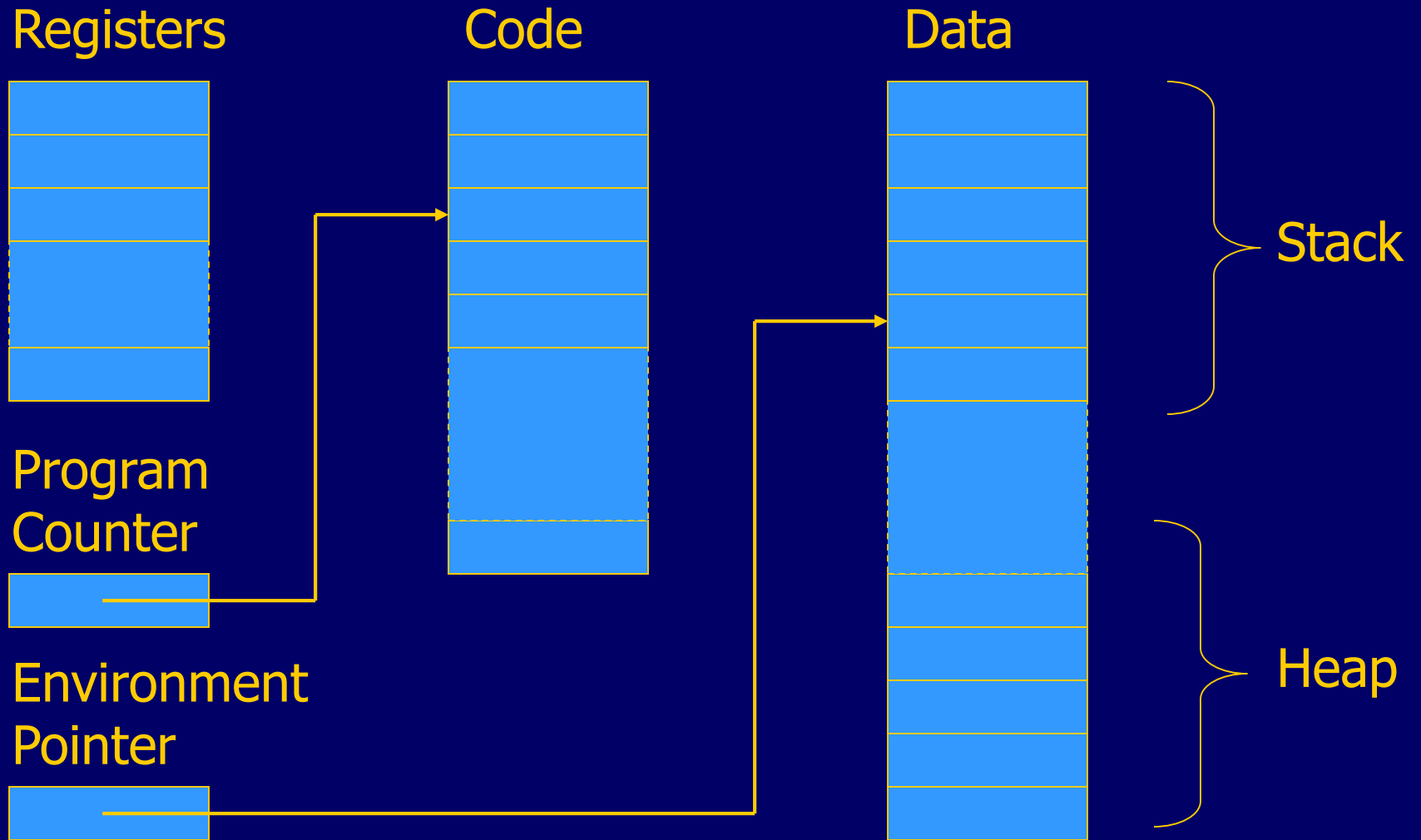
# Stack Frames

- Allocate a separate space for every procedure incarnation
- Relative addresses
- Provide a simple mean to achieve modularity
- Supports separate code generation of procedures
- Naturally supports recursion
- Efficient memory allocation policy
  - Low overhead
  - Hardware support may be available
- LIFO policy
- Not a pure stack
  - Non local references
  - Updated using arithmetic

# A Typical Stack Frame



# Simplified Machine Model





# Interested in Memory Mgmt Only

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## ◆ Registers, Code segment, Program counter

- Ignore registers
- Details of instruction set will not matter

## ◆ Data Segment

- Stack contains data related to block entry/exit
- Heap contains data of varying lifetime
- Environment pointer points to current stack position
  - Block entry: add new activation record to stack
  - Block exit: remove most recent activation record

# Some basic concepts

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## ◆ Scope

- Region of program text where declaration is visible

## ◆ Lifetime (Duration)

- Period of time when location is allocated to program

```
{ int x = ... ;  
    { int y = ... ;  
        { int x = ... ;  
            ....  
        };  
    };  
};
```

- Inner declaration of x hides outer one.
- Called "hole in scope"
- Lifetime of outer x includes time when inner block is executed
- Lifetime  $\neq$  scope
- Lines indicate "contour model" of scope.

# In-line Blocks

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## ◆ Activation record

- Data structure stored on run-time stack
- Contains space for local variables

## ◆ Example

```
{ int x=0;  
  int y=x+1;  
    { int z=(x+y)*(x-y);  
      };  
};
```

Push record with space for x, y  
Set values of x, y

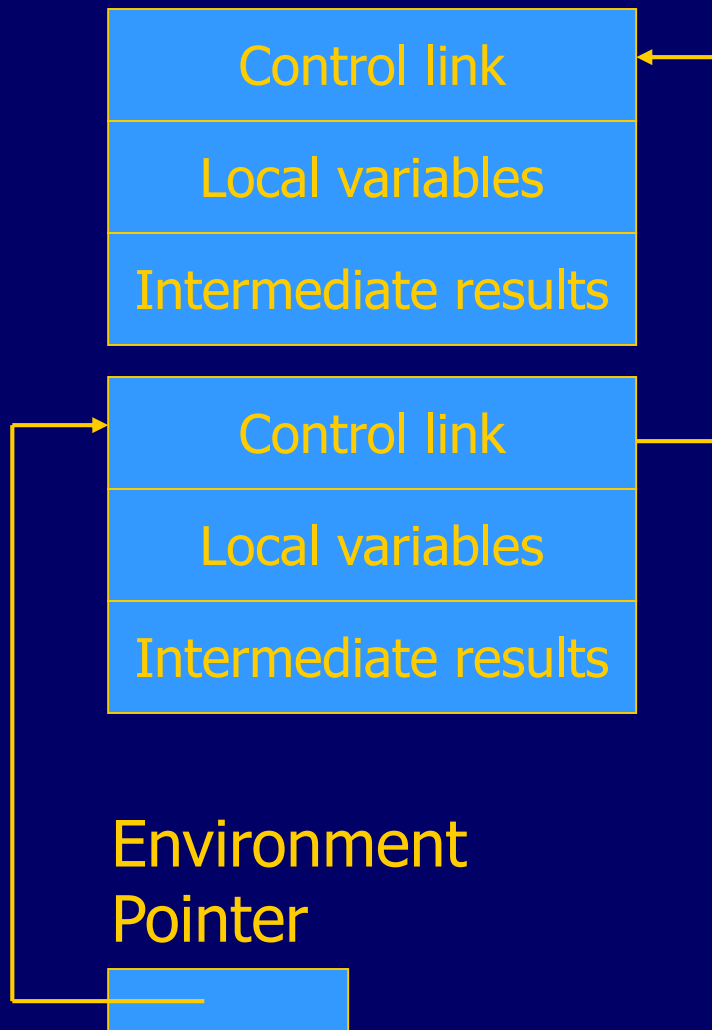
Push record for inner block  
Set value of z

Pop record for inner block

Pop record for outer block

May need space for variables and intermediate results like  $(x+y)$ ,  $(x-y)$

# Activation record for in-line block



## ◆ Control link

- pointer to previous record on stack

## ◆ Push record on stack:

- Set new control link to point to old env ptr
- Set env ptr to new record

## ◆ Pop record off stack

- Follow control link of current record to reset environment pointer

Can be optimized away, but assume not for purpose of discussion.

# Example

```
{ int x=0;
  int y=x+1;
  { int z=(x+y)*(x-y);
    };
};
```

Push record with space for x, y

Set values of x, y

Push record for inner block

Set value of z

Pop record for inner block

Pop record for outer block

Control link	
x	0
y	1

Control link	
z	-1
x+y	1
x-y	-1

Environment  
Pointer



# Scoping rules

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## ◆ Global and local variables

- x, y are local to outer block
- z is local to inner block
- x, y are global to inner block

```
{ int x=0;  
  int y=x+1;  
    { int z=(x+y)*(x-y);  
      };  
};
```

## ◆ Static scope

- global refers to declaration in closest enclosing block

## ◆ Dynamic scope

- global refers to most recent activation record

These are same until we consider function calls.

# Functions and procedures

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## ◆ Syntax of procedures (Algol) and functions (C)

procedure P (<pars>)

begin

    <local vars>

    <proc body>

end;

<type> function f(<pars>)

{

    <local vars>

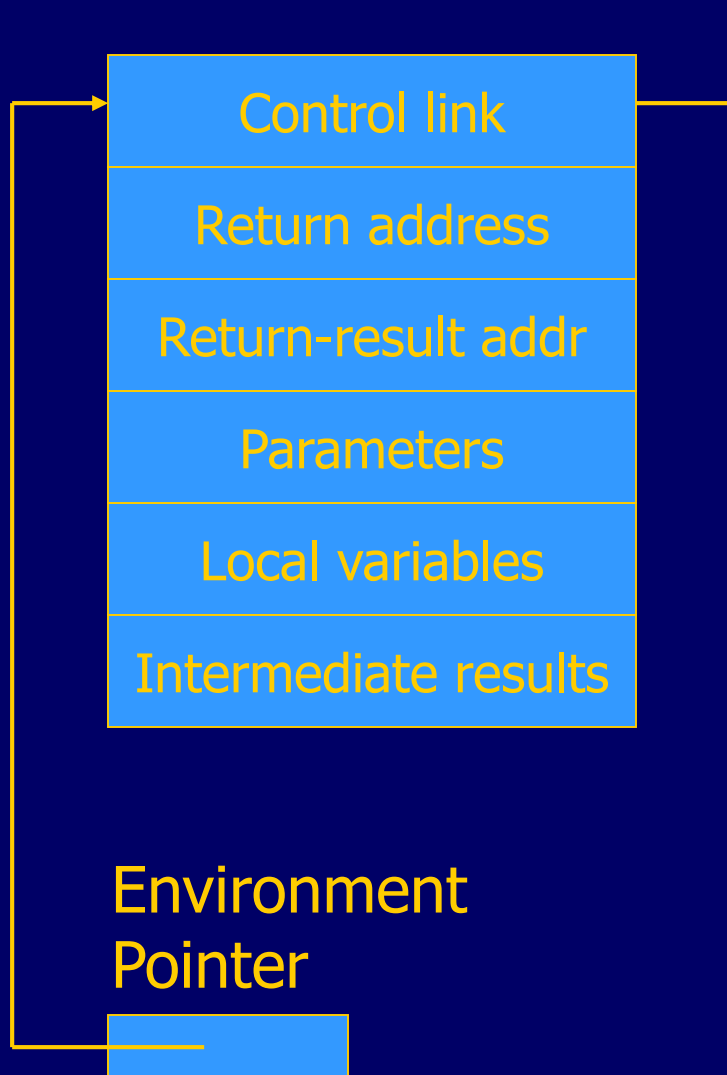
    <function body>

}

## ◆ Activation record must include space for

- parameters
- return address
- local variables, intermediate results
- return value (an intermediate result)
- location to put return value on function exit

# Activation record for function



## ◆ Return address

- Location of code to execute on function return

## ◆ Return-result address

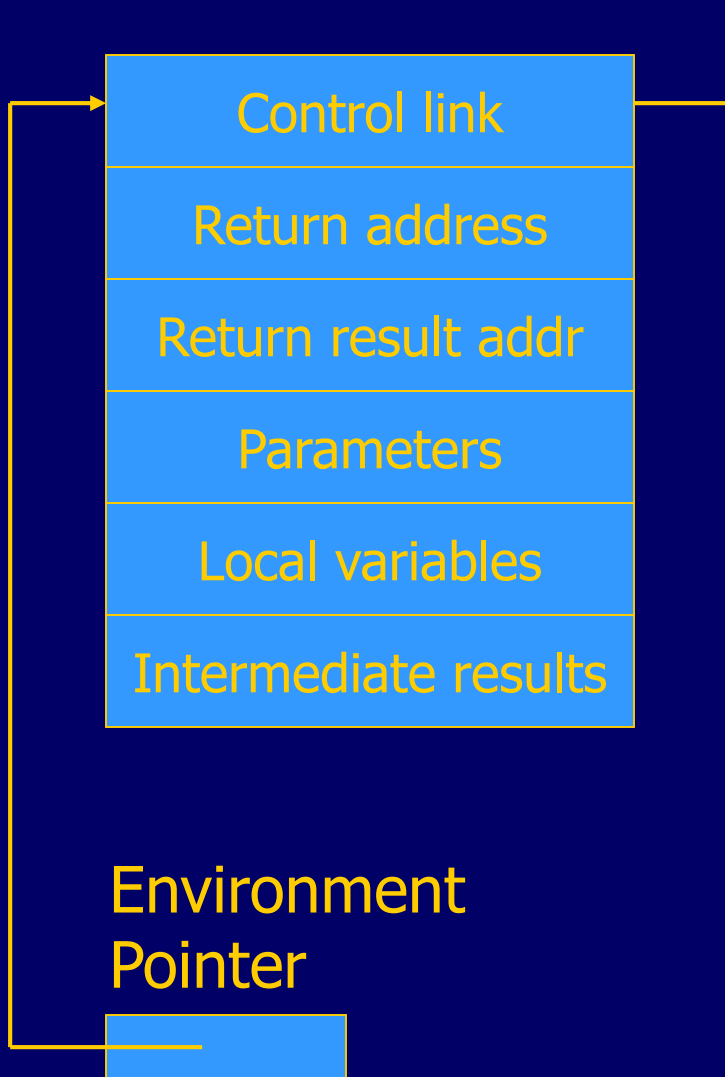
- Address in activation record of calling block to receive return address

## ◆ Parameters

- Locations to contain data from calling block



# Example



## ◆ Function

$\text{fact}(n) = \text{if } n \leq 1 \text{ then } 1$   
 $\text{else } n * \text{fact}(n-1)$

- Return result address
- location to put  $\text{fact}(n)$

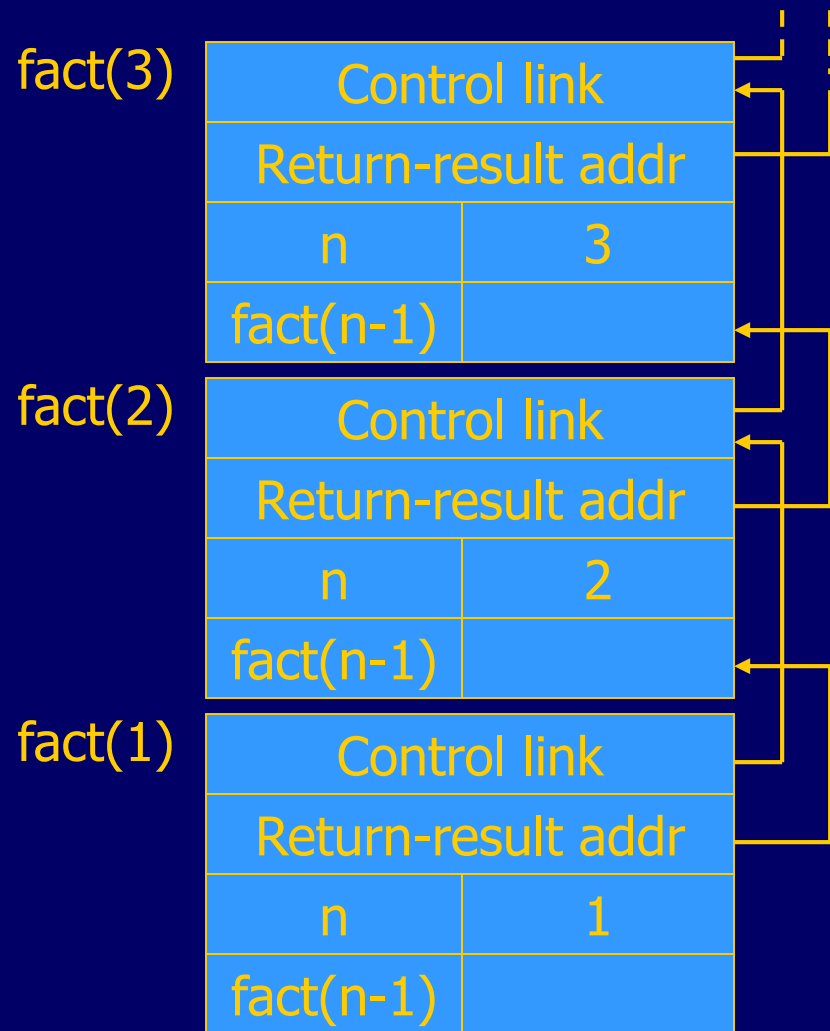
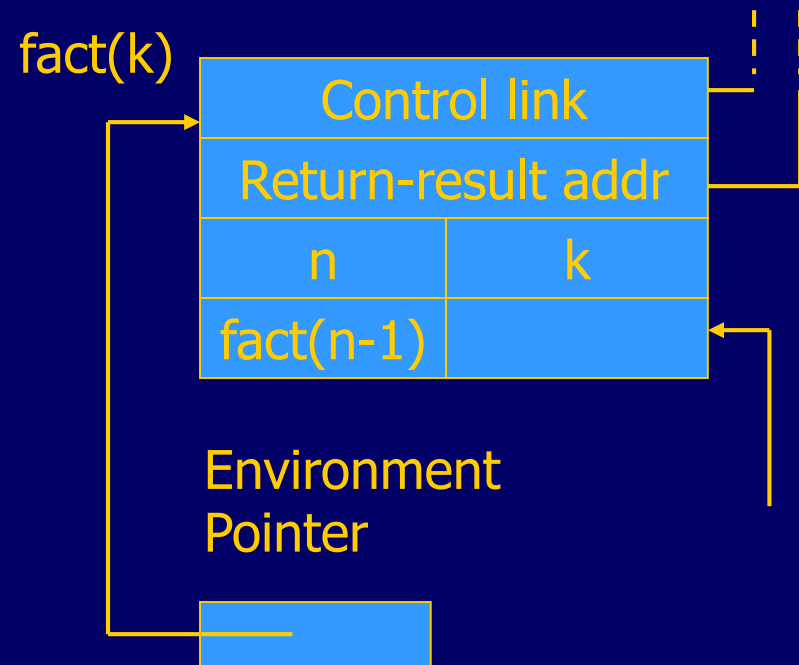
## ◆ Parameter

- set to value of  $n$  by calling sequence

## ◆ Intermediate result

- locations to contain value of  $\text{fact}(n-1)$

# Function call

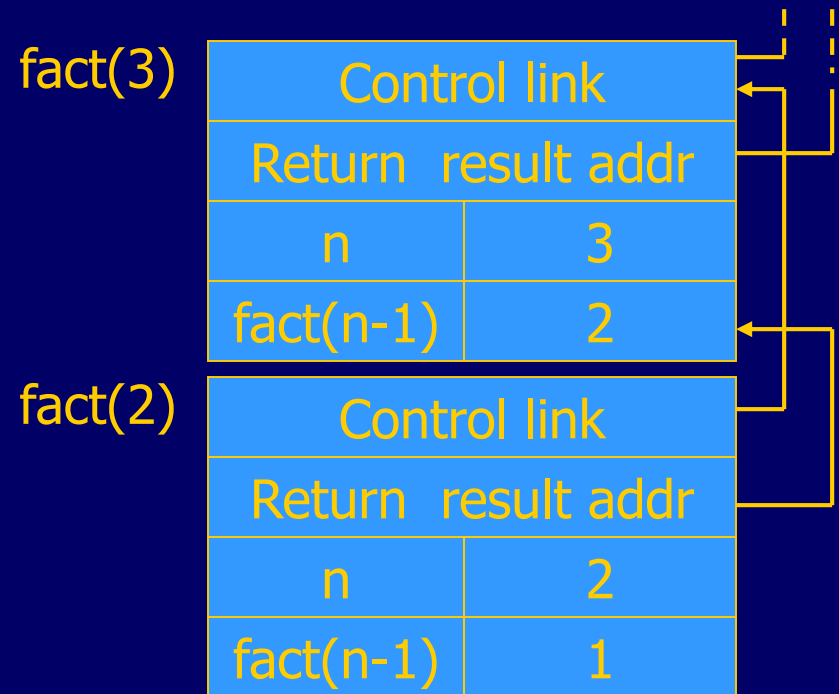
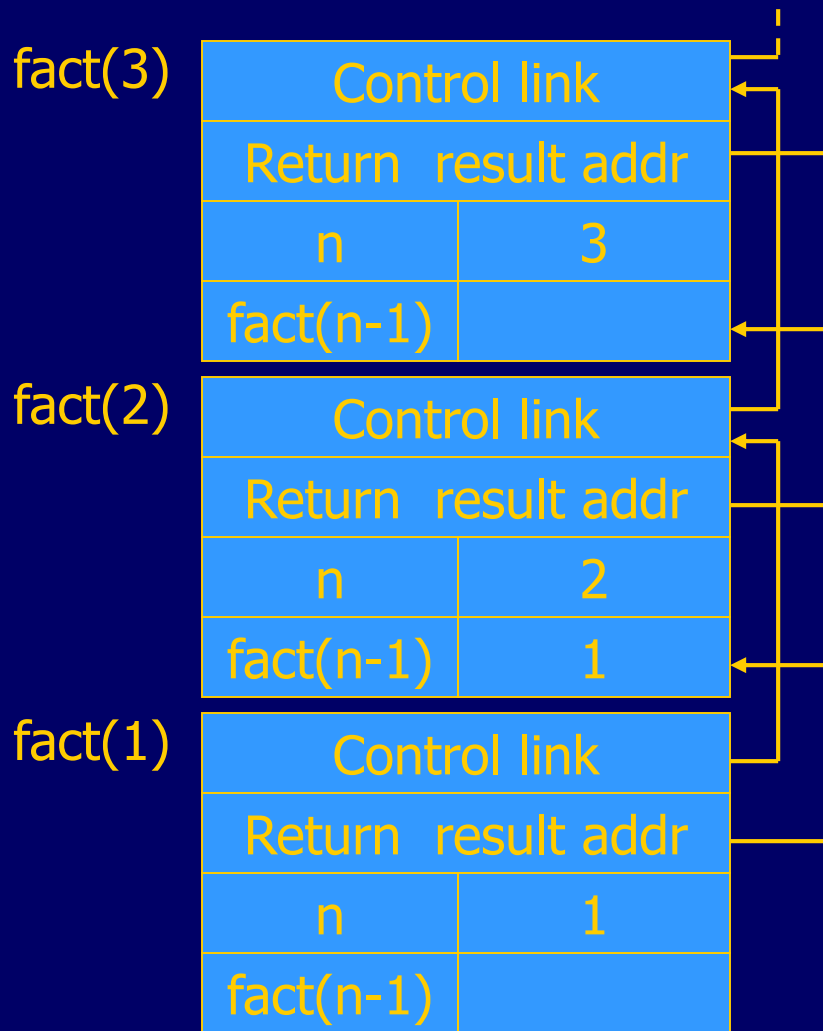


`fact(n) = if  $n \leq 1$  then 1  
else  $n * \text{fact}(n-1)$`

Return address omitted; would be ptr into code segment

Function return next slide →

# Function return



$\text{fact}(n) = \text{if } n \leq 1 \text{ then } 1$   
 $\text{else } n * \text{fact}(n-1)$

# Topics for first-order functions

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## ◆ Parameter passing

- pass-by-value: copy value to new activation record
- pass-by-reference: copy ptr to new activation record

## ◆ Access to global variables

- global variables are contained in an activation record higher “up” the stack

## ◆ Tail recursion

- an optimization for certain recursive functions

See this yourself: write factorial and run under debugger

# L-values vs. R-values

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## ◆ Assignment $x := \text{exp}$ is compiled into:

- Compute the **address** of  $x$
- Compute the **value** of  $\text{exp}$
- Store the value of  $\text{exp}$  into the address of  $x$

## ◆ Generalization

- R-value
  - Maps program expressions into Context values
- L-value
  - Maps program expressions into locations
  - Not always defined
- Java has no small L-values

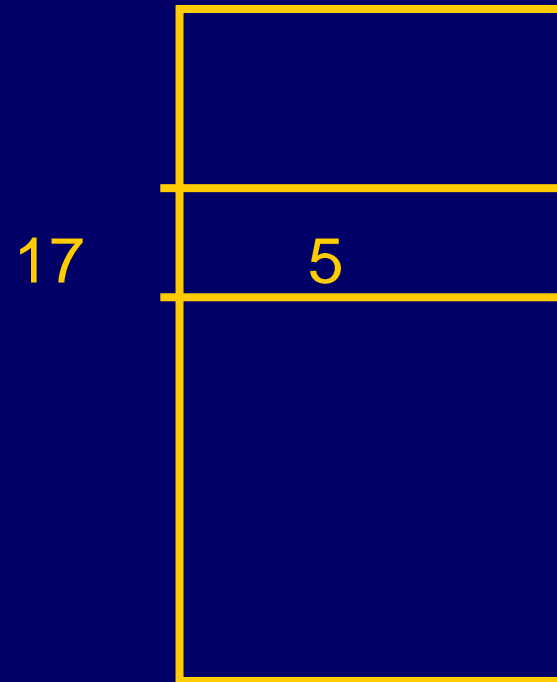
# A Simple Example

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```
int x = 5;
```

```
x = x + 1;
```

Runtime memory



# A Simple Example

---

```
int x = 5;
```

```
lvalue(x)=17, rvalue(x) =5
```

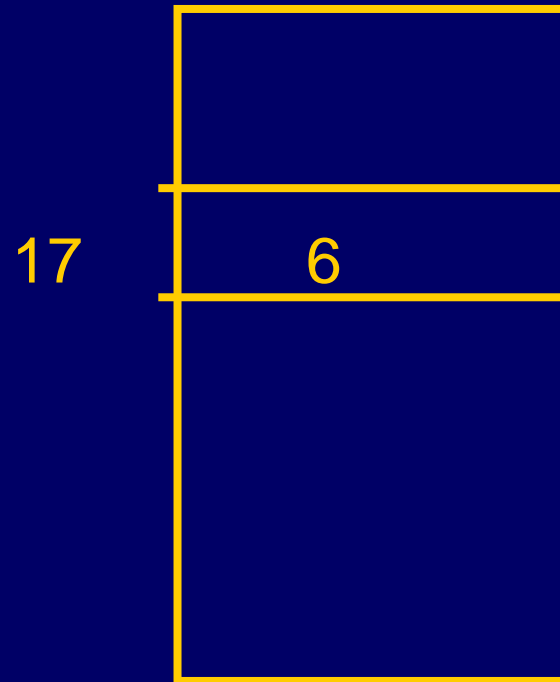
```
lvalue(5)=⊥, rvalue(5)=5
```

```
    x = x + 1;
```

```
lvalue(x)=17, rvalue(x) =6
```

```
lvalue(5)=⊥, rvalue(5)=5
```

Runtime memory



# Partial rules for Lvalue in C

- ◆ Type of e is pointer to T
- ◆ Type of e1 is integer
- ◆ lvalue(e2) ≠ undefined

```
{ int a[100];  
*(a + 5) = 8;  
}
```

exp	lvalue	rvalue
id	location(id)	content(location(id))
const	undefined	value(const)
*e	rvalue(e)	content(rvalue(e))
&e2	undefined	lvalue(e2)
e + e1	undefined	rvalue(e)+sizeof(T)*rvalue(e1)



# Parameter passing

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## ◆ Pass-by-reference

- Place L-value (address) in activation record
- Function can assign to variable that is passed

## ◆ Pass-by-value

- Place R-value (contents) in activation record
- Function cannot change value of caller's variable
- Reduces aliasing (alias: two names refer to same loc)

# Example

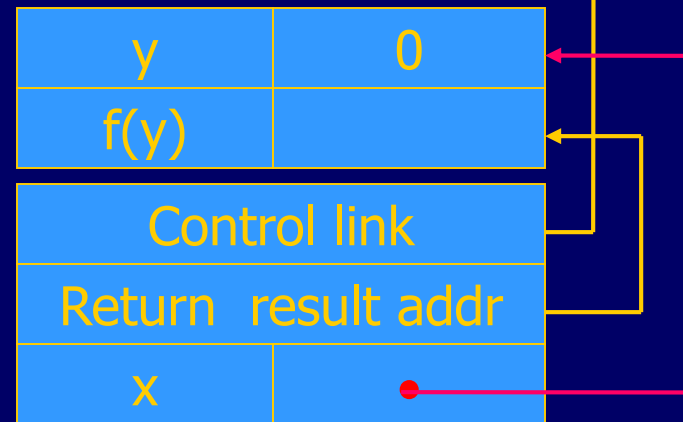
pseudo-code

```
function f (x) =  
  { x = x+1; return x; }  
var y = 0;  
print (f(y)+y);
```

*pass-by-ref*

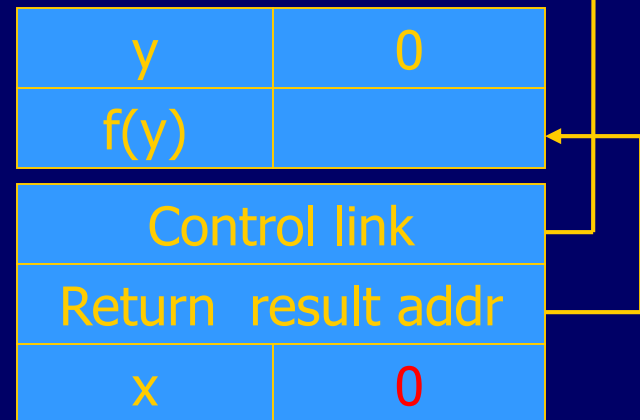
f(y)

activation records



*pass-by-value*

f(y)



# Access to global variables

## ◆ Two possible scoping conventions

- Static scope: refer to closest enclosing block
- Dynamic scope: most recent activation record on stack

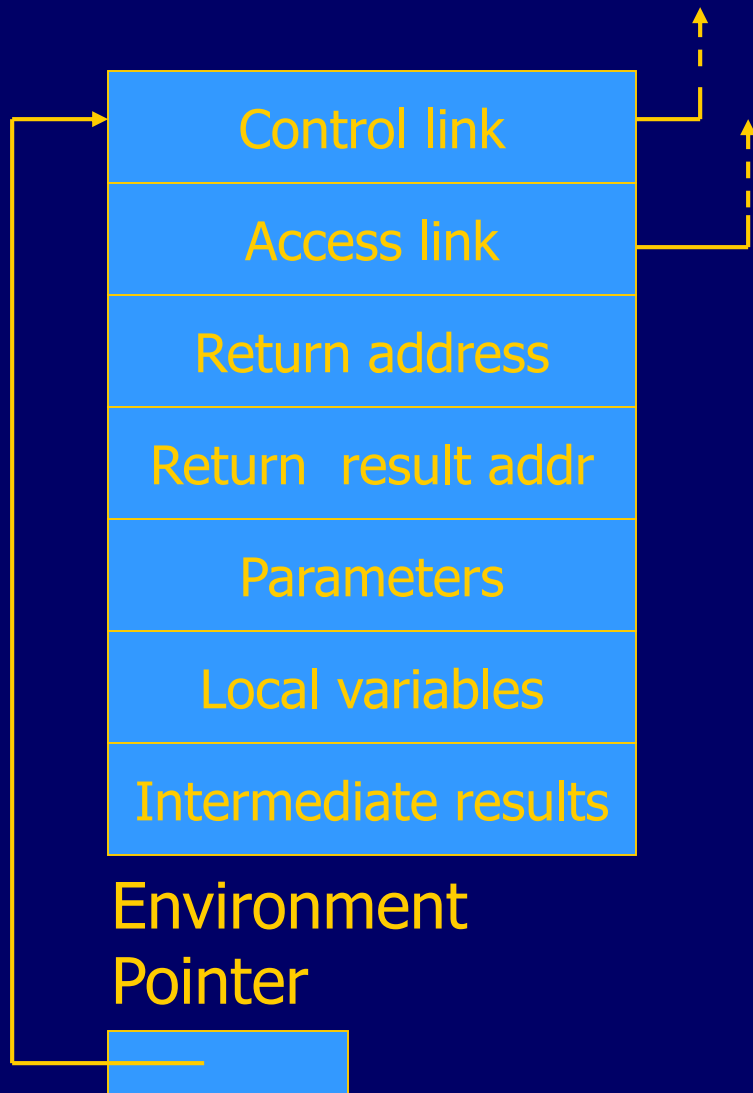
## ◆ Example

```
var x=1;
function g(z) { return x+z; }
function f(y) {
    var x = y+1;
    return g(y*x);
}
f(3);
g(4)
```

outer block	x	1
f(3)	y	3
	x	4
g(12)	z	12

Which x is used for expression x+z ?

# Activation record for static scope



## ◆ Control link

- Link to activation record of previous (calling) block

## ◆ Access link

- Link to activation record of closest enclosing block in program text

## ◆ Difference

- Control link depends on dynamic behavior of prog
- Access link depends on static form of program text

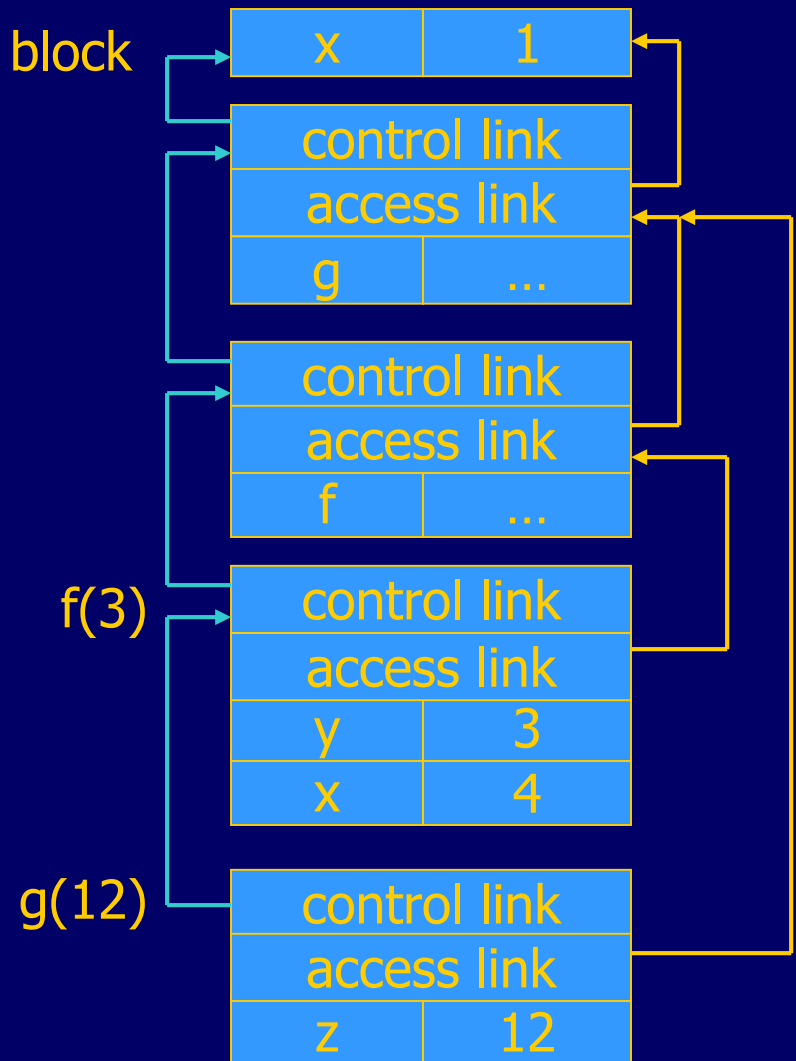
# Static scope with access links

```
var x=1;
function g(z) = { return x+z; }
  function f(y) =
    { var x = y+1;
      return g(y*x); }
f(3);
```

Use access link to find global variable:

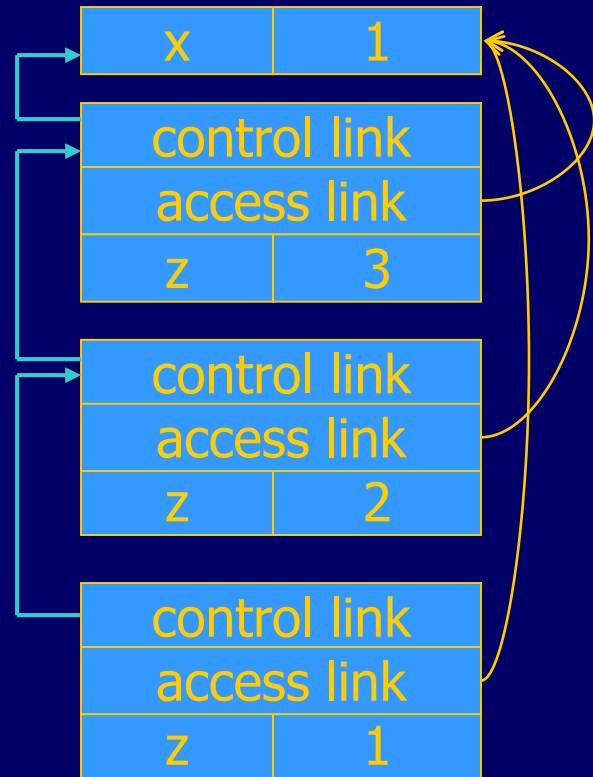
- Access link is always set to frame of closest enclosing lexical block
- For function body, this is block that contains function declaration

outer block



# Static scope with access links & recursion

```
var x=1;
function fac(z) = {
  if z = 1 then return x;
  else return z * fac(z-1);
}
fac(3)
```



# Tail recursion


(first-order case)

◆ Function  $g$  makes a *tail call* to function  $f$  if

- Return value of function  $f$  is return value of  $g$

◆ Example

fun  $g(x) =$  if  $x > 0$  then  $f(x)$  else  $f(x) * 2$



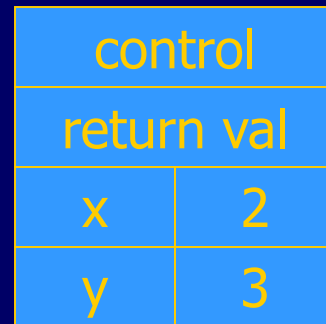
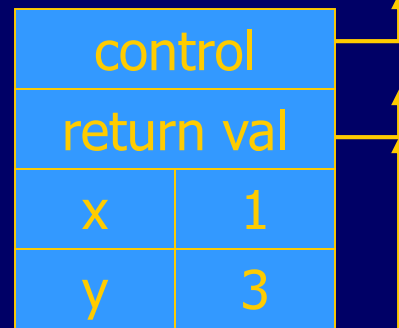
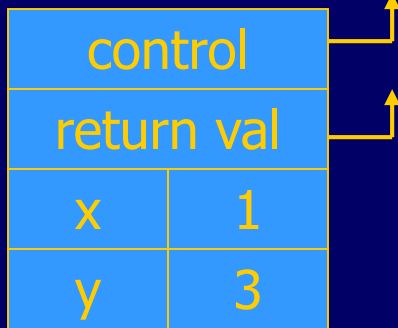
◆ Optimization

- Can pop activation record on a tail call
- Especially useful for recursive tail call
  - next activation record has exactly same form

# Example

Calculate least power of 2 greater than  $y$

$f(1,3)$



```
fun f(x,y) = if x>y
  then x
  else f(2*x, y);
f(1,3) + 7;
```

## Optimization

- Set return value address to that of caller

## Question

- Can we do the same with control link?

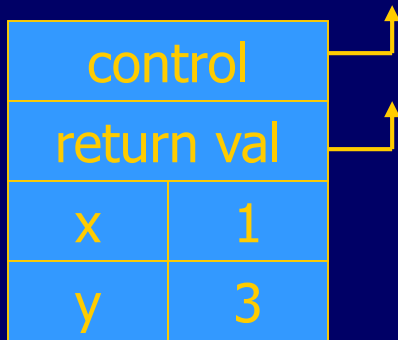
## Optimization

- avoid return to caller

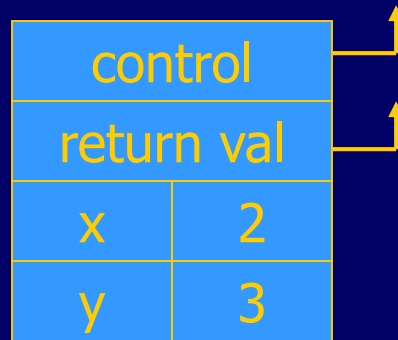


# Tail recursion elimination

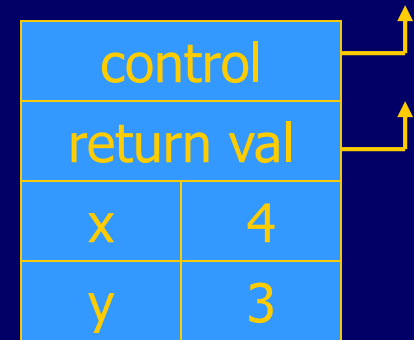
f(1,3)



f(2,3)



f(4,3)



```
fun f(x,y) = if x>y
  then x
  else f(2*x, y);
f(1,3);
```

## Optimization

- pop followed by push = reuse activation record in place

## Conclusion

- Tail recursive function equiv to iterative loop

# Tail recursion and iteration

f(1,3)

control		↑
return val		↑
x	1	
y	3	

f(2,3)

control		↑
return val		↑
x	2	
y	3	

f(4,3)

control		↑
return val		↑
x	4	
y	3	

```
fun f(x,y) = if x > y
  then x
  else f(2*x, y);
f(1,y);
```

test

loop body

initial value

```
function g(y) {
  var x = 1;
  while (!x > y)
    x = 2*x;
  return x;
}
```

# Higher-Order Functions

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## ◆ Language features

- Functions passed as arguments
- Functions that return functions from nested blocks
- Need to maintain environment of function

## ◆ Simpler case

- Function passed as argument
- Need pointer to activation record “higher up” in stack

## ◆ More complicated second case

- Function returned as result of function call
- Need to keep activation record of returning function

# Pass function as argument

OCaml

```
let x = 4 in
  let f = fun y -> x*y in
    let g = fun h ->
      let x=7
      in
      h(3) + x
    in
    g(f)
```

Pseudo-JavaScript

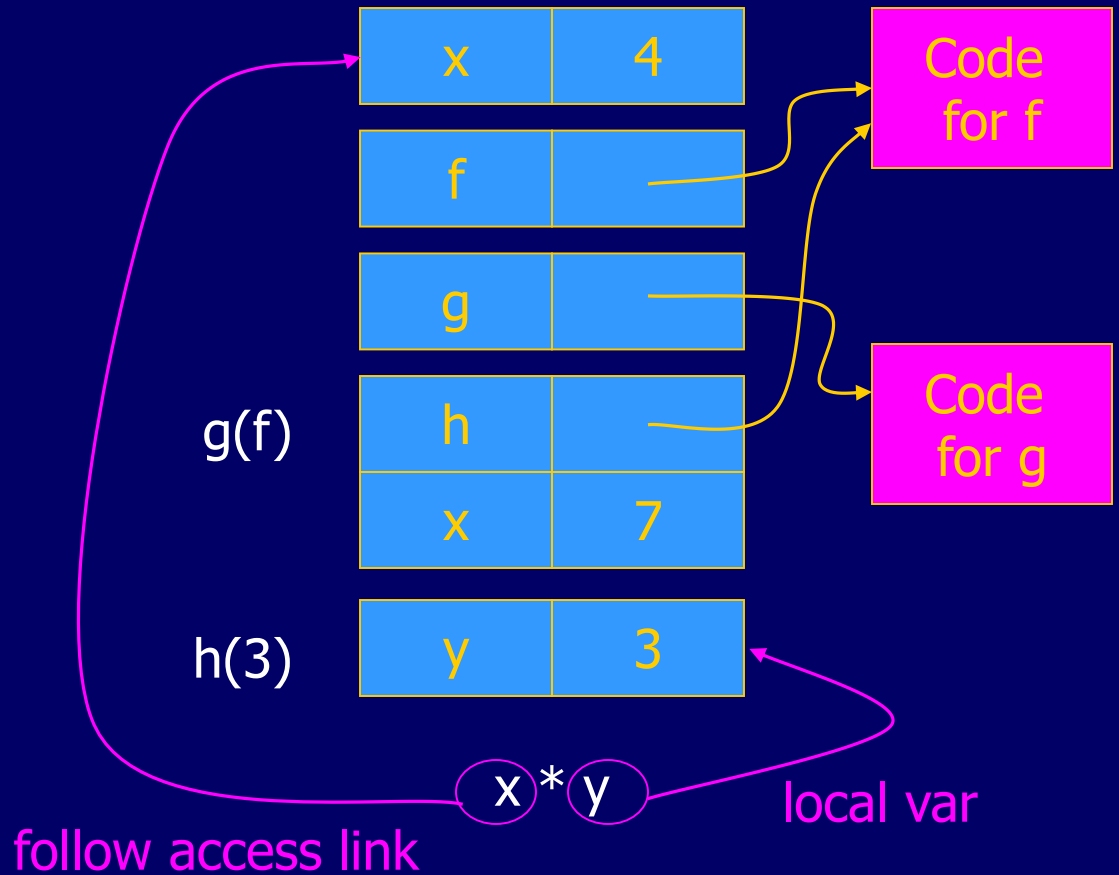
```
{ var x = 4;
  { function f(y) {return x*y};
    { function g(h) {
      var x = 7;
      return h(3) + x;
    };
    g(f);
  }
}
```

There are two declarations of  $x$

Which one is used for each occurrence of  $x$ ?

# Static Scope for Function Argument

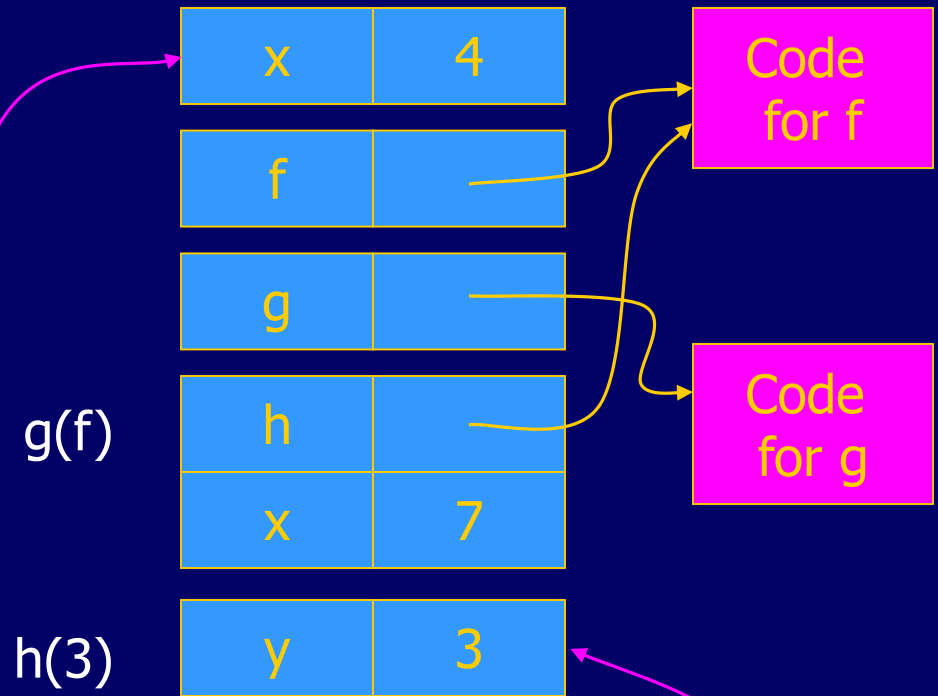
```
let x = 4 in
  let f = fun -> x*y in
    let g = fun h ->
      let
        int x=7
      in
        h(3) + x
    in
      g(f)
```



How is access link for h(3) set?

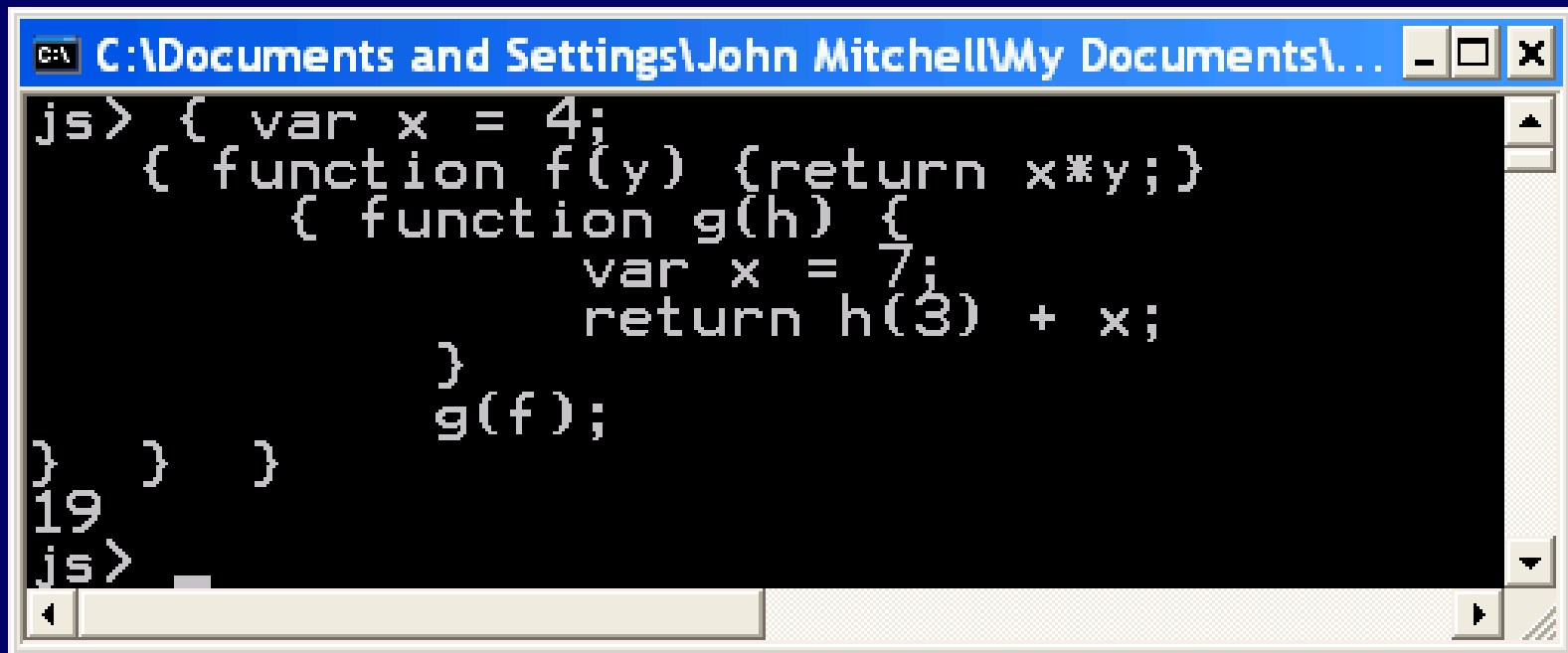
# Static Scope for Function Argument

```
{ var x = 4;  
  { function f(y) {return x*y};  
    { function g(h) {  
      int x=7;  
      return h(3) + x;  
    };  
    g(f);  
  }  
}
```



How is access link for `h(3)` set?

# Result of function call



```
js> { var x = 4;
      { function f(y) {return x*y;}
        { function g(h) {
            var x = 7;
            return h(3) + x;
          }
          g(f);
        }
      }
}
19
js>
```

# Closures

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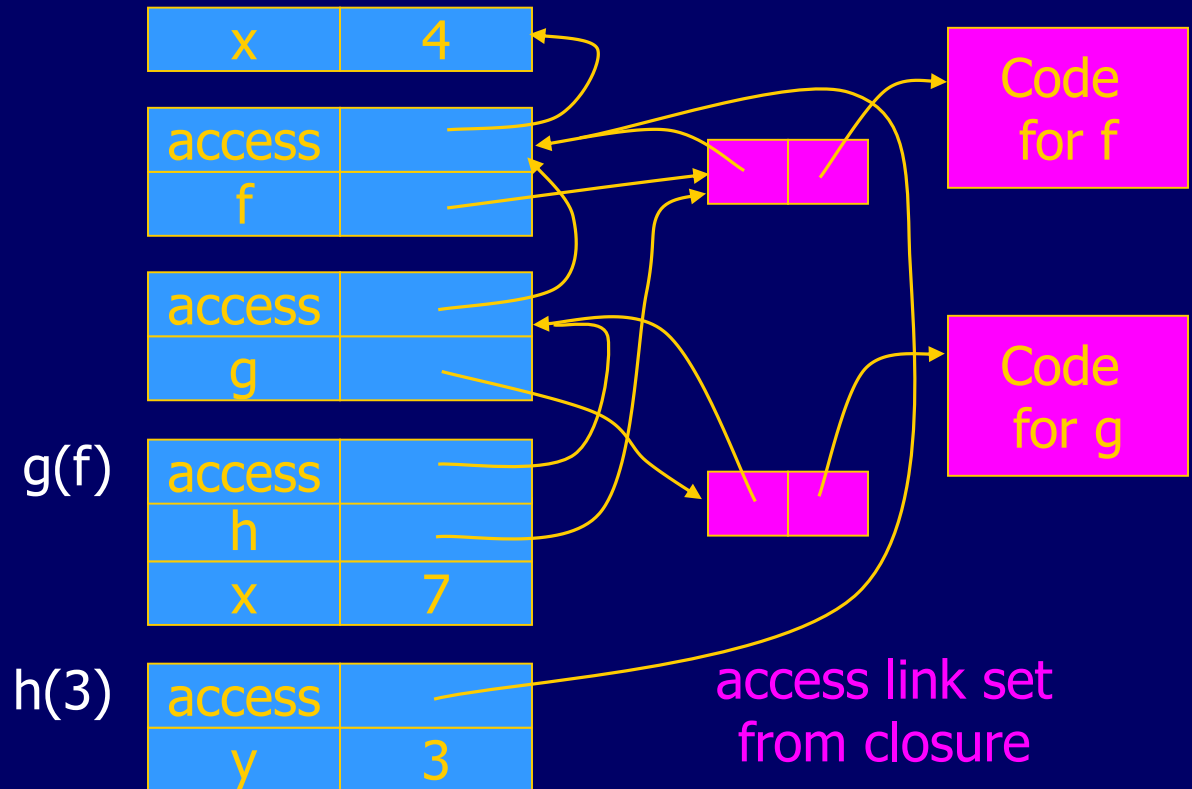
- ◆ Function value is pair *closure* =  $\langle env, code \rangle$
- ◆ When a function represented by a closure is called,
  - Allocate activation record for call (as always)
  - Set the access link in the activation record using the environment pointer from the closure



# Function Argument and Closures

## Run-time stack with access links

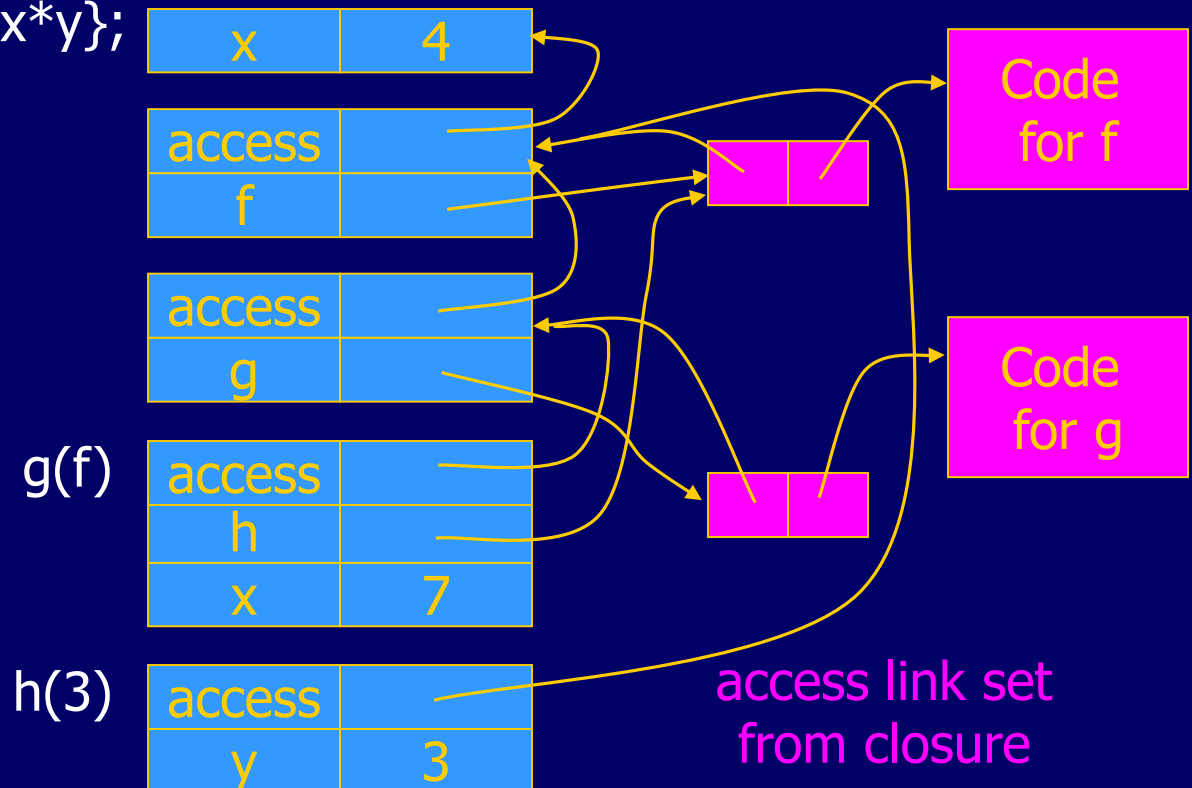
```
let x = 4 in
  let f = fun y->x*y in
    let g = fun h ->
      let
        x=7
      in
        h(3) + x
    in g(f)
```



# Function Argument and Closures

## Run-time stack with access links

```
{ var x = 4;  
  { function f(y){return x*y};  
    { function g(h) {  
      int x=7;  
      return h(3)+x;  
    };  
    g(f);  
  }  
}
```



# Summary: Function Arguments

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- ◆ Use closure to maintain a pointer to the static environment of a function body
- ◆ When called, set access link from closure
- ◆ All access links point “up” in stack
  - May jump past activ records to find global vars
  - Still deallocate activ records using stack (lifo) order

# Return Function as Result

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## ◆ Language feature

- Functions that return “new” functions
- Need to maintain environment of function

## ◆ Example

```
function compose(f,g)
    {return function(x) { return g(f (x)) }};
```

## ◆ Function “created” dynamically

- expression with free variables  
values are determined at run time
- function value is closure =  $\langle \text{env}, \text{code} \rangle$
- code *not* compiled dynamically (in most languages)

# Example: Return fctn with private state

OCaml

```
let mk_counter = fun init ->
  let count = ref init in
  let counter = fun inc ->
    (count := !count + inc; !count)
  in
    counter
in
  let c = mk_counter 1
  in
    c(2) + c(2)
```

- Function to “make counter” returns a closure
- How is correct value of count determined in `c(2)` ?

# Example: Return fctn with private state

---

JS

```
function mk_counter (init) {  
    var count = init;  
    function counter(inc) {count=count+inc; return count};  
    return counter};  
var c = mk_counter(1);  
c(2) + c(2);
```

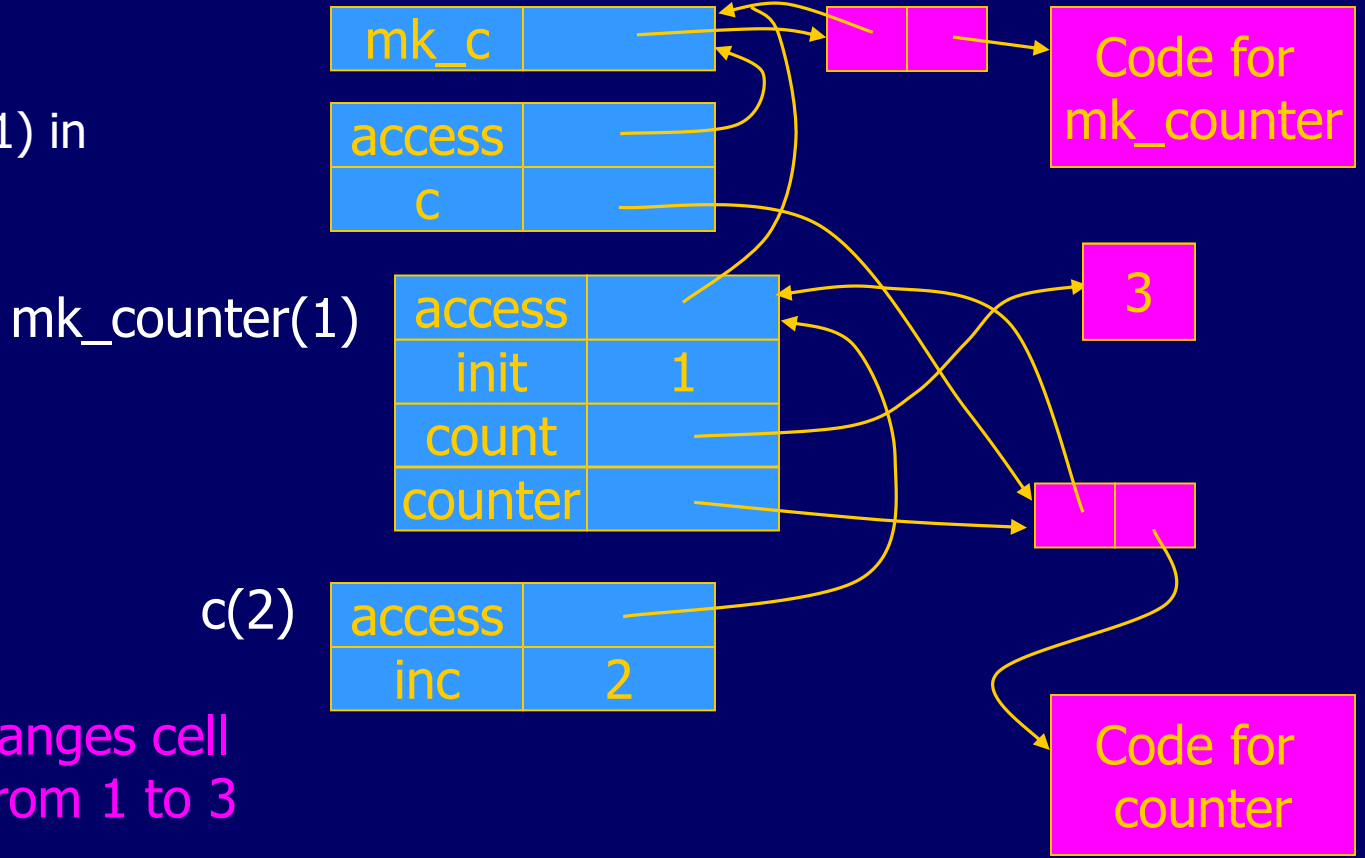
Function to “make counter” returns a closure

How is correct value of count determined in call `c(2)` ?

# Function Results and Closures

```
let mk_counter = fun init ->  
  let count = ref init in  
  let counter = fun inc -> (count := !count + inc; !count)  
  in counter
```

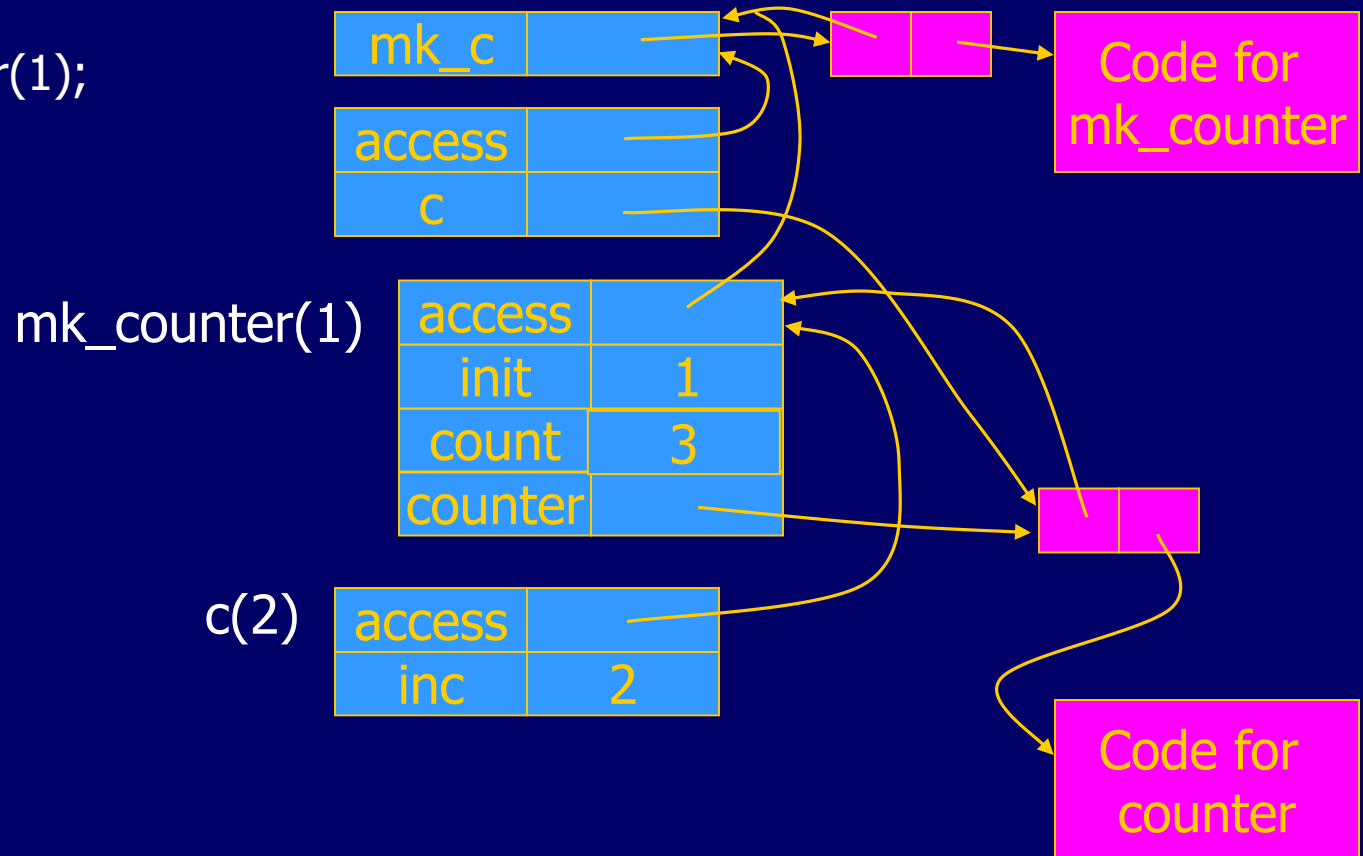
```
in  
let c = mk_counter(1) in  
c(2) + c(2)
```



Call changes cell value from 1 to 3

# Function Results and Closures

```
function mk_counter (init) {
  var count = init;
  function counter(inc) {count=count+inc; return count};
  return counter};
var c = mk_counter(1);
c(2) + c(2);
```





# Closures in Web programming

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## ◆ Useful for event handlers in Web programming:

```
function AppendButton(container, name, message) {  
    var btn = document.createElement('button');  
    btn.innerHTML = name;  
    btn.onclick = function (evt) { alert(message); }  
    container.appendChild(btn);  
}
```

## ◆ Environment pointer lets the button's click handler find the message to display

# Simple C Program

---

```
foo (int y) {  
    int x = y ;  
    if (x > 8) {  
        int x = y + 1 ;  
        x = x + 1 ;  
    }  
}
```

foo(9)

control	
return val	
x	9
y	9
x	10

# The C Programming Language

---

- ◆ Designed to allow stack allocation
- ◆ Local variables are flattened
- ◆ No need for control link
- ◆ Permit
  - Nested blocks
  - Passing functions as parameters and return values
- ◆ Forbid
  - Nested functions

# Summary: Return Function Results

---

- ◆ Use closure to maintain static environment
- ◆ May need to keep activation records after return
  - Stack (lifo) order fails!
- ◆ Possible “stack” implementation
  - Forget about explicit deallocation
  - Put activation records on heap
  - Invoke garbage collector as needed
  - Not as totally crazy as it sounds
    - May only need to search reachable data

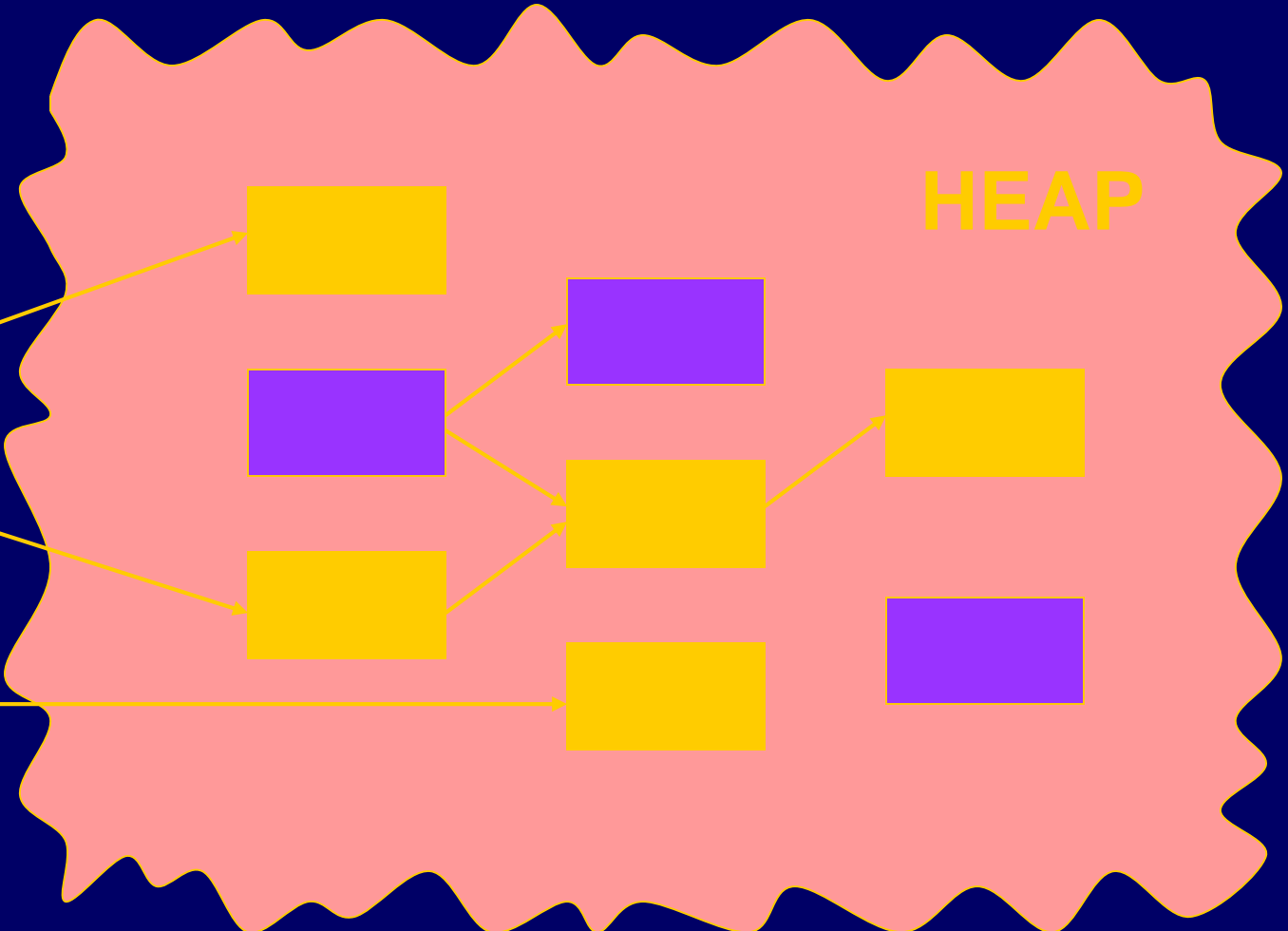
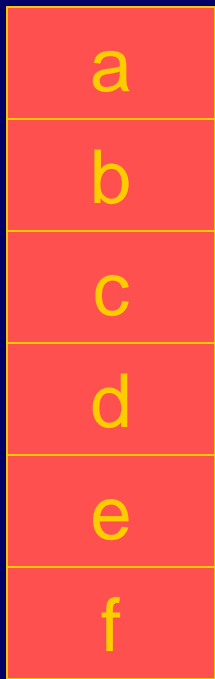
# Summary of scope issues

---

- ◆ Block-structured lang uses stack of activation records
  - Activation records contain parameters, local vars, ...
  - Also pointers to enclosing scope
- ◆ Several different parameter passing mechanisms
- ◆ Tail calls may be optimized
- ◆ Function parameters/results require closures
  - Closure environment pointer used on function call
  - Stack deallocation may fail if function returned from call
  - Closures *not* needed if functions not in nested blocks

# Garbage Collection

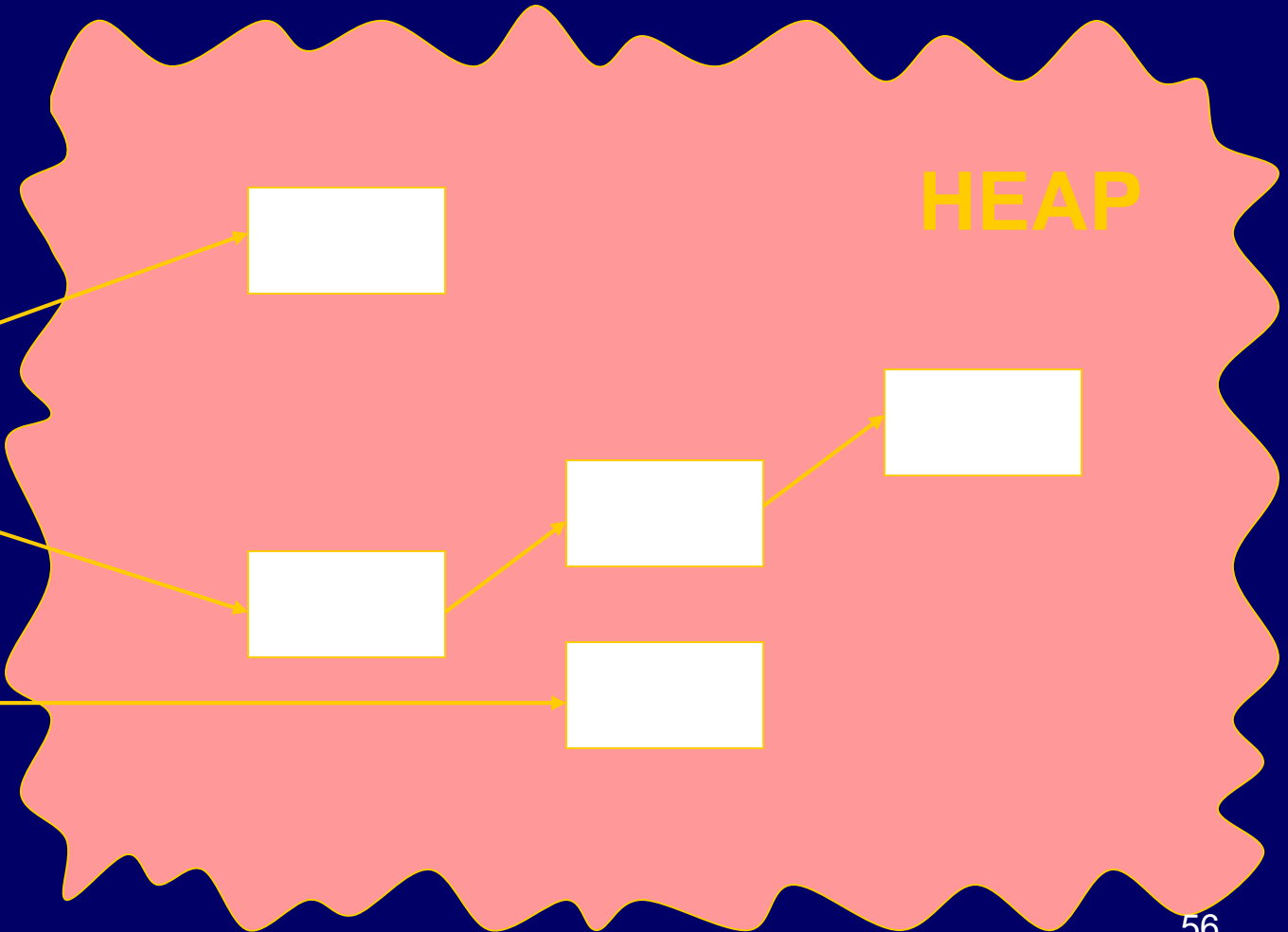
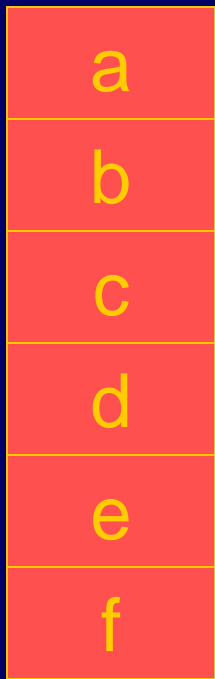
**ROOT SET**



Stack

# Garbage Collection

**ROOT SET**



Stack

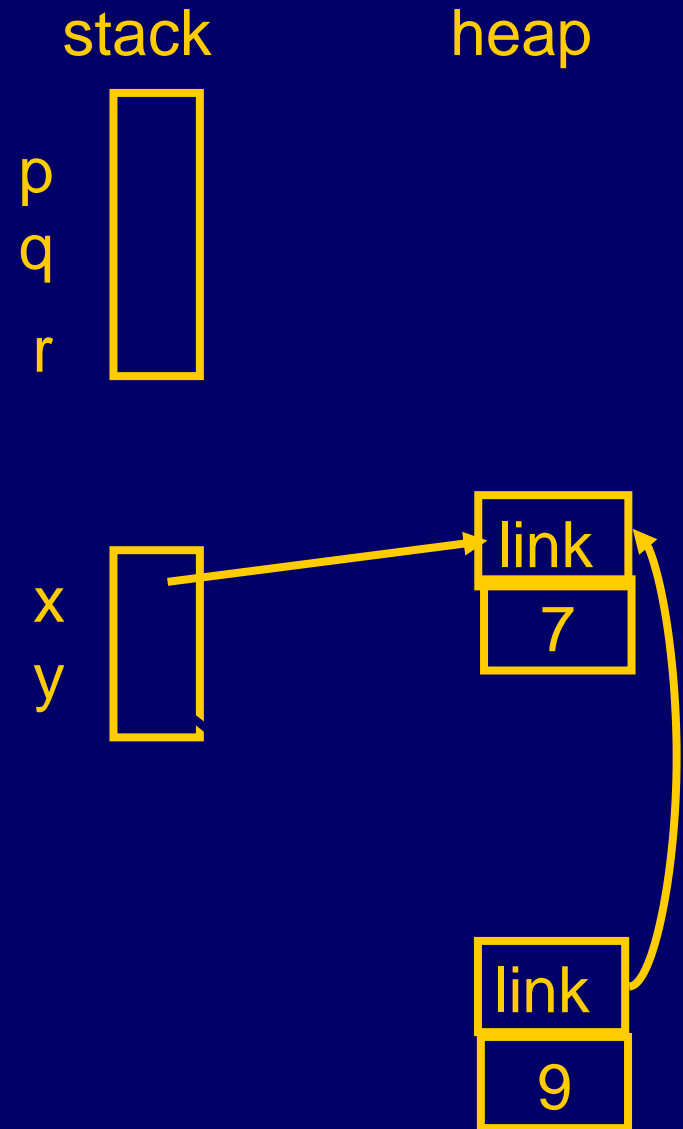
# What is garbage collection

---

- ◆ The runtime environment reuse chunks that were allocated but are not subsequently used garbage chunks
  - not live
- ◆ It is undecidable to find the garbage chunks:
  - Decidability of liveness
  - Decidability of type information
- ◆ **Conservative collection**
  - every live chunk is identified
  - some garbage runtime chunk are not identified
- ◆ Find the reachable chunks via pointer chains
- ◆ Often done in the allocation function



```
typedef struct list {struct list *link; int key} *List;
typedef struct tree {int key;
                    struct tree *left;
                    struct tree *right} *Tree;
foo() { List x = cons(NULL, 7);
      List y = cons(x, 9);
      x->link = y;
      }
void main() {
  Tree p, r; int q;
  foo();
  p = maketree(); r = p->right;
  q= r->key;
  showtree(r);}
```



stack

heap

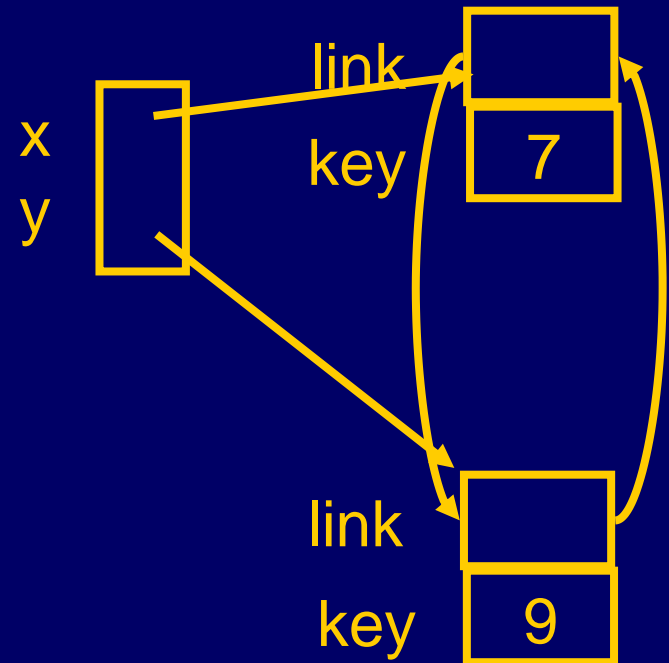


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  p = maketree(); r = p->right;
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```



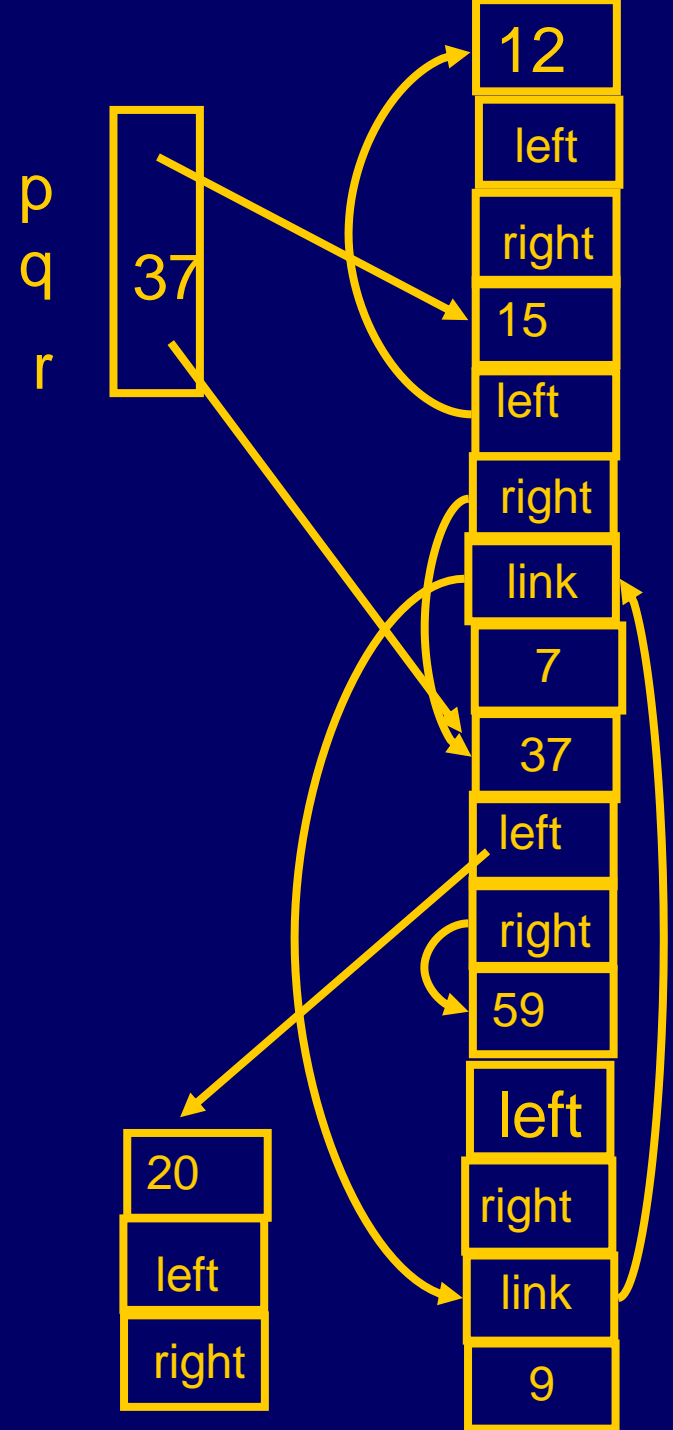
```

typedef struct list {struct list *link; int key} *List;
typedef struct tree {int key;
                    struct tree *left;
                    struct tree *right} *Tree;

foo() { List x = create_list(NULL, 7);
       List y = create_list(x, 9);
       x->link = y;
       }

void main() {
  Tree p, r; int q;
  foo();
  p = maketree(); r = p->right;
  q= r->key;
  showtree(r);}

```



# Garbage Collection Techniques

---

## ◆ Tracing

- Scan the reachable heaps from the root
- Release unreachable elements
- Cost proportional to reachable heap

## ◆ Reference Counting

- Maintain a counter of references to each chunk of memory
- The compiler generates the update code for references when pointers are manipulated
- Release objects with zero reference counter
- Constant cost

# Mark-and-Sweep(Scan) Collection

---

- ◆ **Mark** the chunks reachable from the roots (stack, static variables and machine registers)
- ◆ **Sweep** the heap space by moving unreachable chunks to the freelist (Scan)

# The Mark Phase

---

for each root  $v$   
DFS( $v$ )

function DFS( $x$ )

if  $x$  is a pointer and chunk  $x$  is not  
marked

mark  $x$

for each reference field  $f_i$  of

chunk  $x$

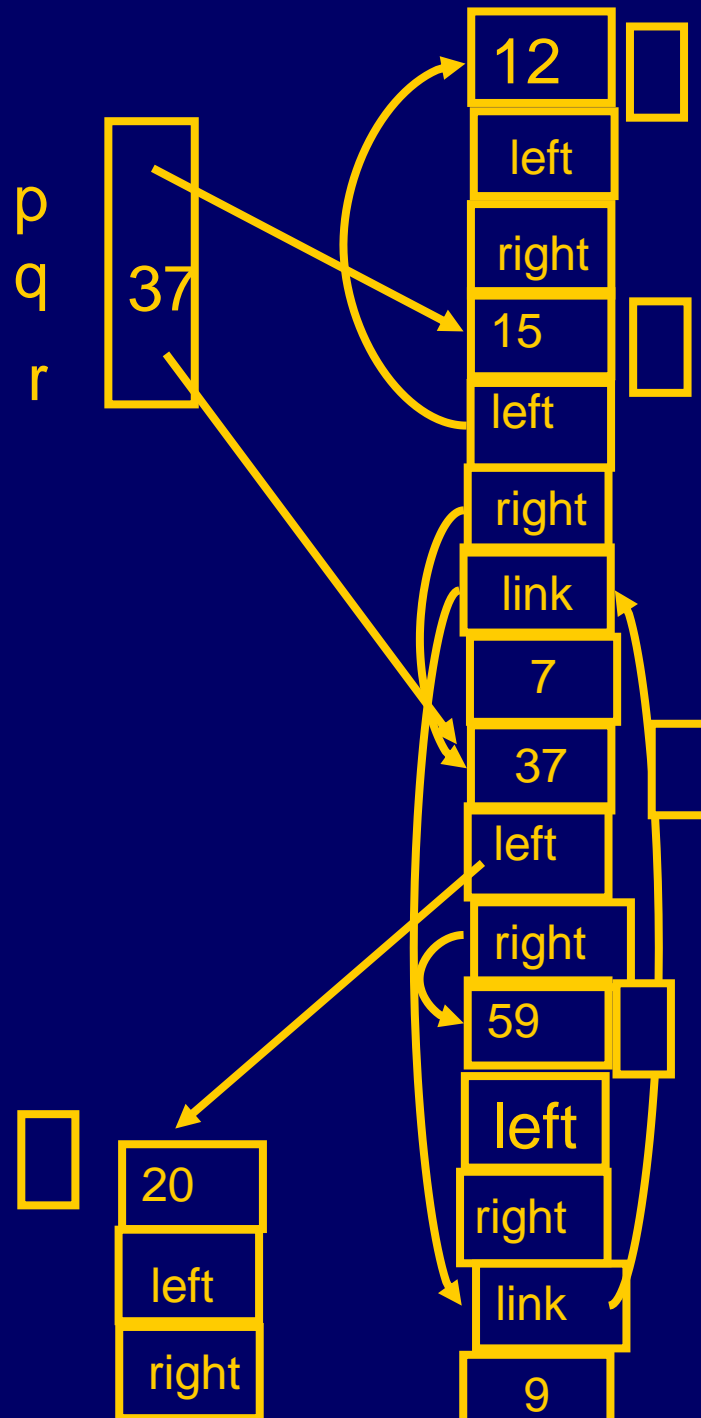
DFS( $x.f_i$ )

# The Sweep Phase

---

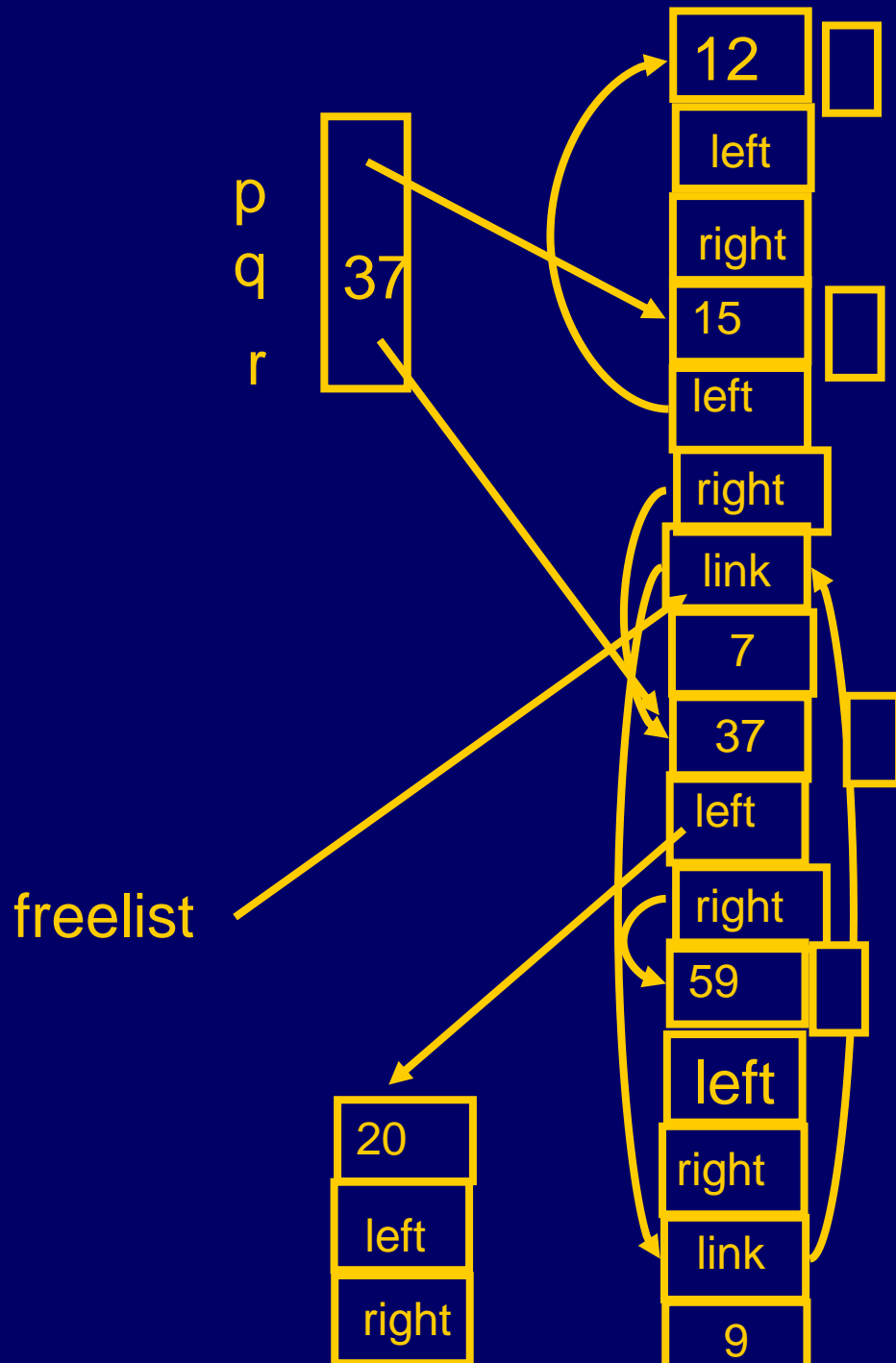
```
p := first address in heap
while p < last address in the heap
  if chunk p is marked
    unmark p
  else let f1 be the first pointer reference field in
p
    p.f1 := freelist
    freelist := p
  p := p + size of chunk p
```

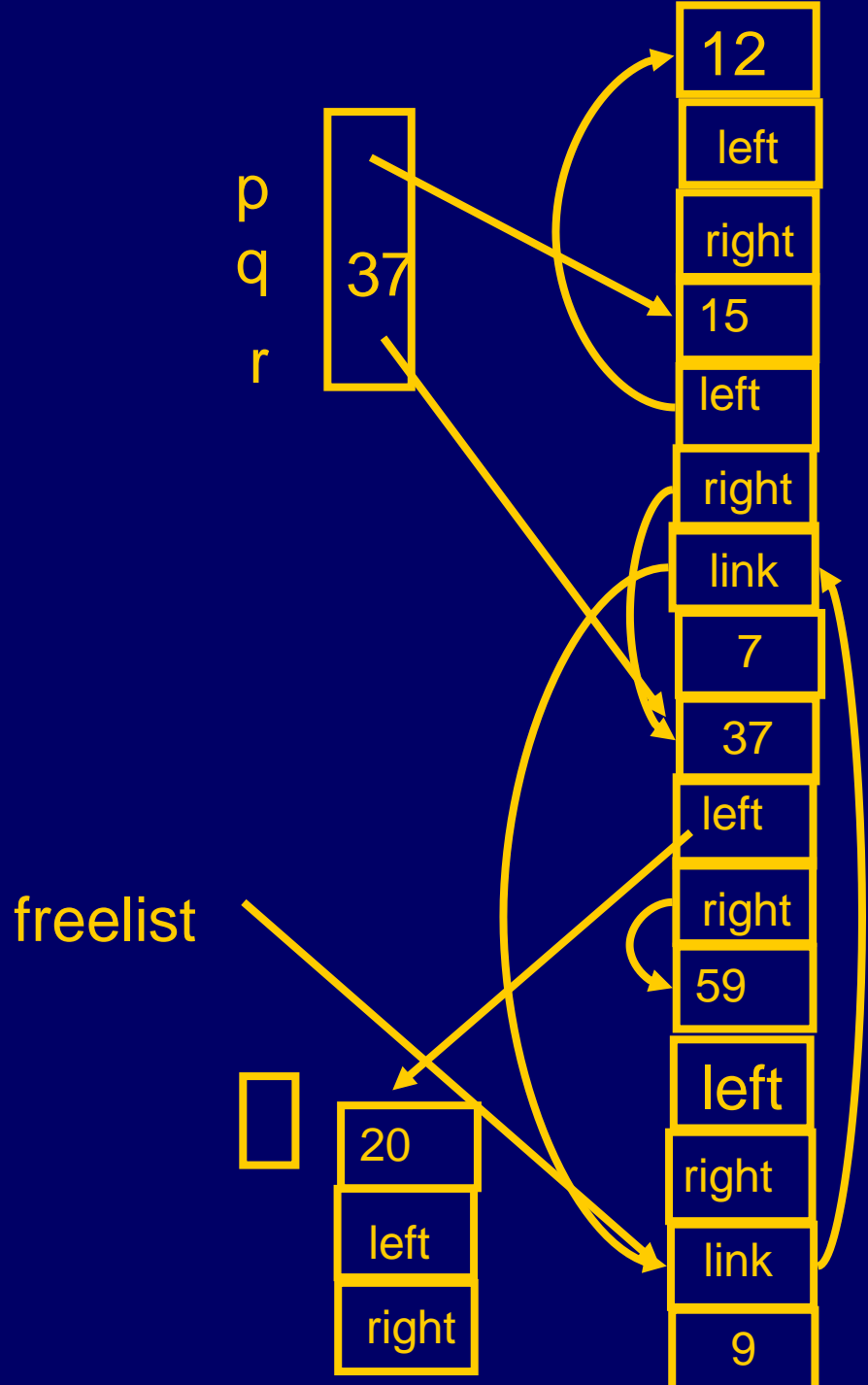
Mark





Sweep





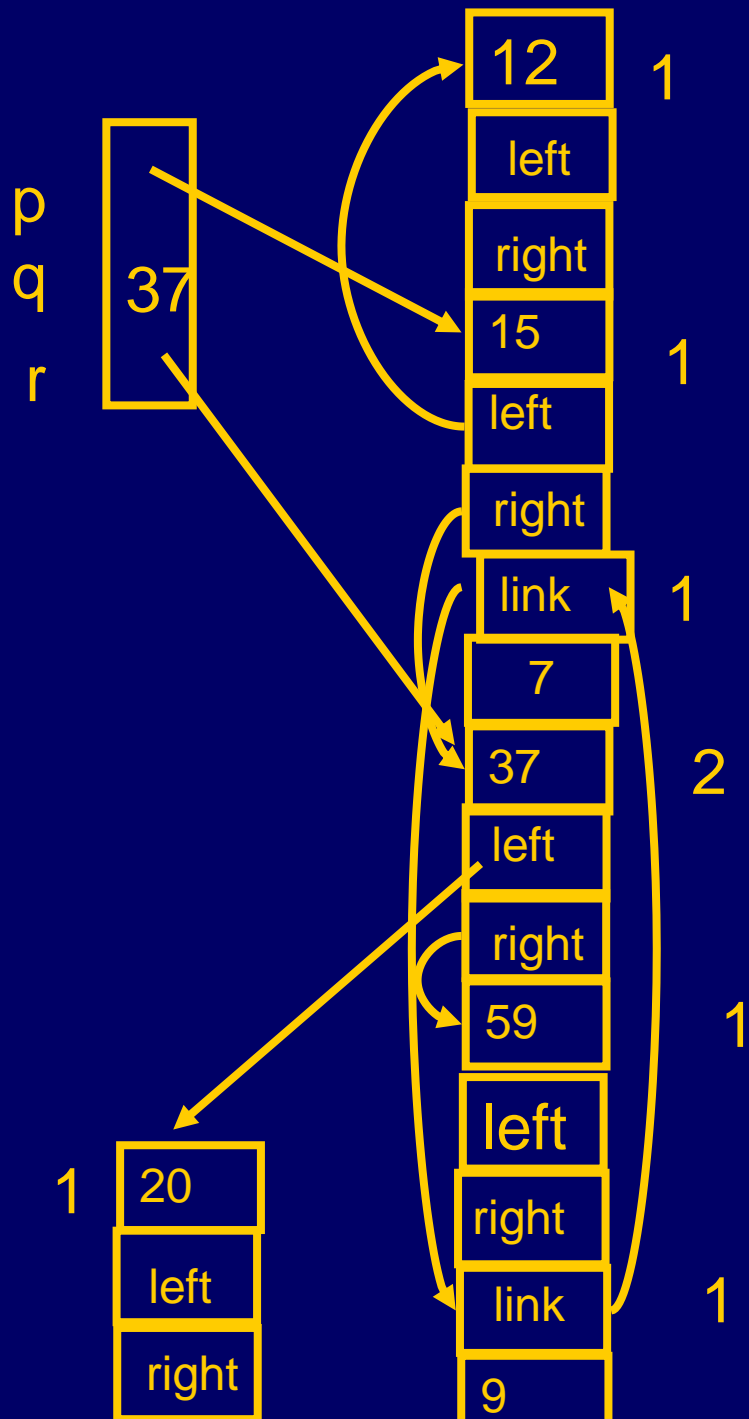
# Cost of GC

- ◆ The cost of a single garbage collection can be linear in the size of the store
  - may cause quadratic program slowdown
- ◆ Amortized cost
  - collection-time/storage reclaimed
  - Cost of one garbage collection
    - $c_1 R + c_2 H$
  - $H - R$  Reclaimed chunks
  - Cost per reclaimed chunk
    - $(c_1 R + c_2 H) / (H - R)$
  - If  $R/H > 0.5$ 
    - increase  $H$
  - if  $R/H < 0.5$ 
    - cost per reclaimed word is  $c_1 + 2c_2 \sim 16$
  - There is no lower bound

# Reference Counting

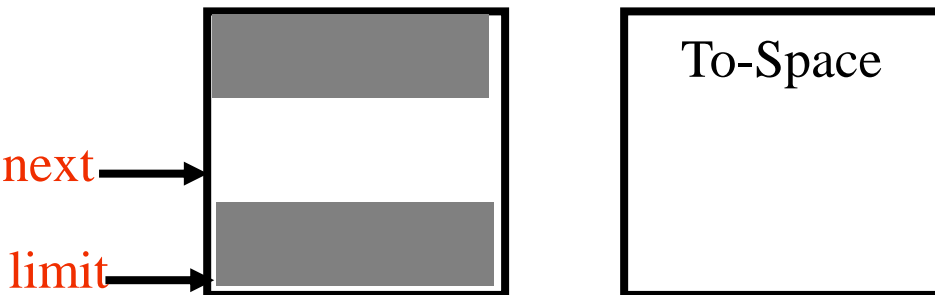
---

- ◆ Maintain a counter per object
- ◆ The compiler generates updates for counters
- ◆ Release object with zero counters
- ◆ Cannot reclaim cyclic objects



# Copying Collection

- Maintains two separate heaps
  - from-space
  - to-space
- pointer **next** to the next free chunk in from-space
- A pointer **limit** to the last chunk in from-space
- If **next** = **limit** copy the reachable chunks from from-space into to-space
  - set **next** and **limit**
  - Switch from-space and to-space
- Requires type information



# Generational Garbage Collection

- Newly created objects contain higher percentage of garbage
- Partition the heap into generations  $G_1$  and  $G_2$
- First garbage collect the  $G_1$  heap
  - chunks which are reachable
- After two or three collections chunks are promoted to  $G_2$
- Once a while garbage collect  $G_2$
- Can be generalized to more than two heaps
- But how can we garbage collect in  $G_1$ ?

# Scanning roots from older generations

- **remembered list**
  - The compiler generates code after each destructive update  $b.f_i := a$  to put  $b$  into a vector of updated objects scanned by the garbage collector
- **remembered set**
  - remembered-list + “set-bit”
- **Card marking**
  - Divide the memory into  $2^k$  cards
- **Page marking**
  - $k =$  page size
  - virtual memory system catches updates to old-generations using the dirty-bit



# Incremental Collection

- Even the most efficient garbage collection can interrupt the program for quite a while
- Under certain conditions the collector can run concurrently with the program (mutator)
- Need to guarantee that mutator leaves the chunks in consistent state, e.g., may need to restart collection
- Two solutions
  - compile-time
    - Generate extra instructions at store/load
  - virtual-memory
    - Mark certain pages as read(write)-only
    - a write into (read from) this page by the program restart mutator

# Garbage Collection vs. Explicit Memory Deallocation

---

- ◆ Faster program development
- ◆ Less error prone
- ◆ Can lead to faster programs
  - Can improve locality of references
- ◆ Support very general programming styles, e.g. higher order and OO programming, Closure
- ◆ Standard in ML, Java, C#, Javascript
- ◆ Supported in C and C++ via separate libraries
- ◆ May require more space
- ◆ Needs a large memory
- ◆ Can lead to long pauses
- ◆ Can change locality of references
- ◆ Effectiveness depends on programming language and style
- ◆ Hides documentation
- ◆ More trusted code

# Summary

---

- ◆ Runtime memory management is crucial for functionality and correctness
- ◆ Lexical scope is natural
  - Becomes tricky with higher order functions
  - Closures
- ◆ Garbage Collection permits general programming style