

Scope, Function Calls and Storage Management

John Mitchell

Adapted by Mooly Sagiv

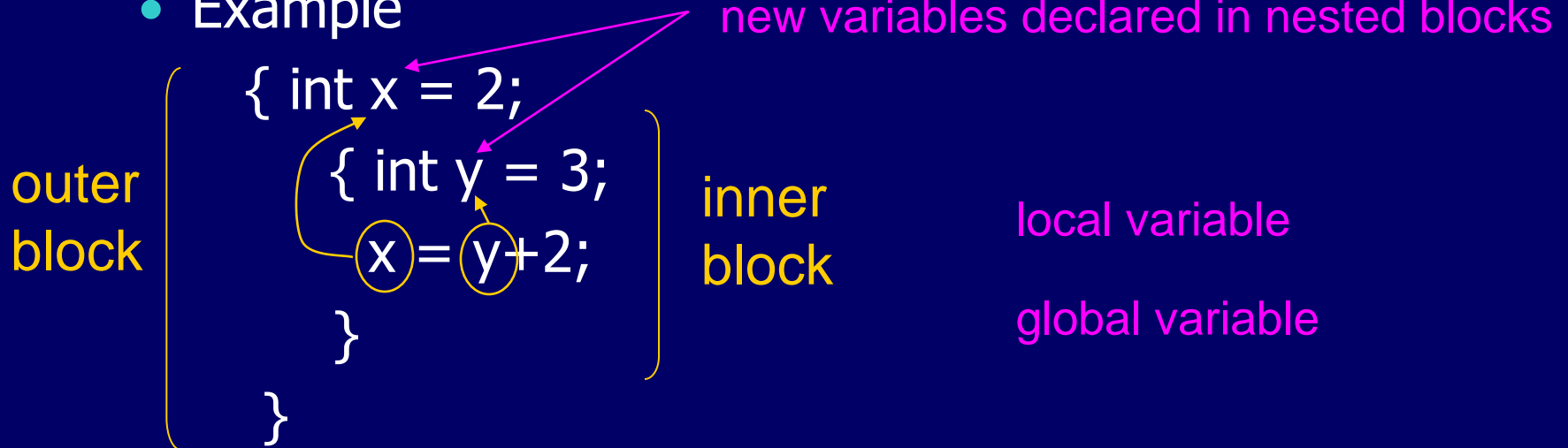
Topics

- ◆ Block-structured languages and stack storage
- ◆ In-line Blocks
 - activation records
 - storage for local, global variables
- ◆ First-order functions
 - parameter passing
 - tail recursion and iteration
- ◆ Higher-order functions
 - deviations from stack discipline
 - language expressiveness => implementation complexity
- ◆ Garbage Collection

Block-Structured Languages

◆ Nested blocks, local variables

- Example



- Storage management

- Enter block: allocate space for variables
- Exits block: some or all space may be deallocated

Examples

◆ Blocks in common languages

- C, ~~JavaScript~~ * { ... }
- Algol begin ... end
- ML let ... in ...

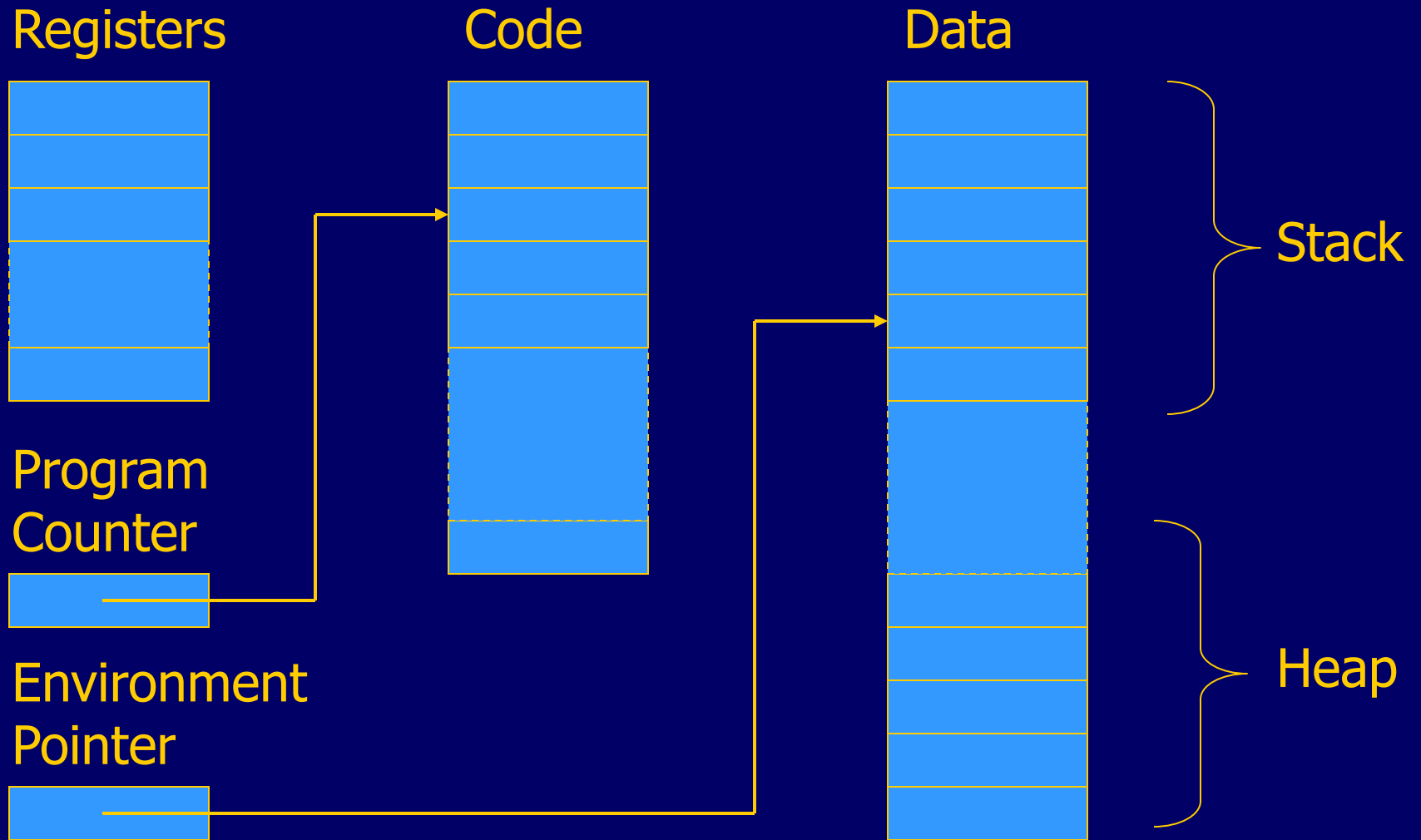
◆ Two forms of blocks

- In-line blocks
- Blocks associated with functions or procedures

◆ Topic: block-based memory management, access to local variables, parameters, global variables

* JavaScript functions provide blocks

Simplified Machine Model



Interested in Memory Mgmt Only

◆ Registers, Code segment, Program counter

- Ignore registers
- Details of instruction set will not matter

◆ Data Segment

- Stack contains data related to block entry/exit
- Heap contains data of varying lifetime
- Environment pointer points to current stack position
 - Block entry: add new activation record to stack
 - Block exit: remove most recent activation record

Some basic concepts

◆ Scope

- Region of program text where declaration is visible

◆ Lifetime (Duration)

- Period of time when location is allocated to program

```
{ int x = ... ;  
    { int y = ... ;  
        { int x = ... ;  
            ....  
        };  
    };  
};
```

- Inner declaration of x hides outer one.
- Called "hole in scope"
- Lifetime of outer x includes time when inner block is executed
- Lifetime \neq scope
- Lines indicate "contour model" of scope.

In-line Blocks

◆ Activation record

- Data structure stored on run-time stack
- Contains space for local variables

◆ Example

```
{ int x=0;  
  int y=x+1;  
    { int z=(x+y)*(x-y);  
      };  
};
```

Push record with space for x, y
Set values of x, y

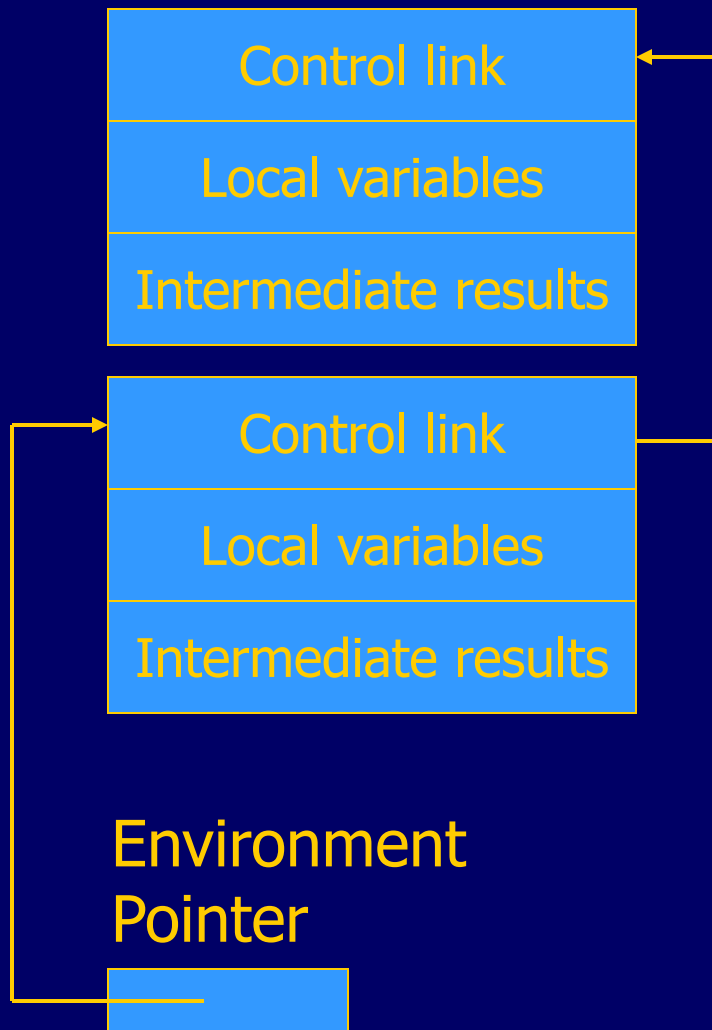
Push record for inner block
Set value of z

Pop record for inner block

Pop record for outer block

May need space for variables and intermediate results like $(x+y)$, $(x-y)$

Activation record for in-line block



◆ Control link

- pointer to previous record on stack

◆ Push record on stack:

- Set new control link to point to old env ptr
- Set env ptr to new record

◆ Pop record off stack

- Follow control link of current record to reset environment pointer

Can be optimized away, but assume not for purpose of discussion.

Example

```
{ int x=0;
  int y=x+1;
  { int z=(x+y)*(x-y);
    };
};
```

Push record with space for x, y

Set values of x, y

Push record for inner block

Set value of z

Pop record for inner block

Pop record for outer block

Control link	
x	0
y	1

Control link	
z	-1
x+y	1
x-y	-1

Environment
Pointer



Scoping rules

◆ Global and local variables

- x, y are local to outer block
- z is local to inner block
- x, y are global to inner block

```
{ int x=0;  
  int y=x+1;  
    { int z=(x+y)*(x-y);  
      };  
};
```

◆ Static scope

- global refers to declaration in closest enclosing block

◆ Dynamic scope

- global refers to most recent activation record

These are same until we consider function calls.

Functions and procedures

◆ Syntax of procedures (Algol) and functions (C)

procedure P (<pars>)

begin

 <local vars>

 <proc body>

end;

<type> function f(<pars>)

{

 <local vars>

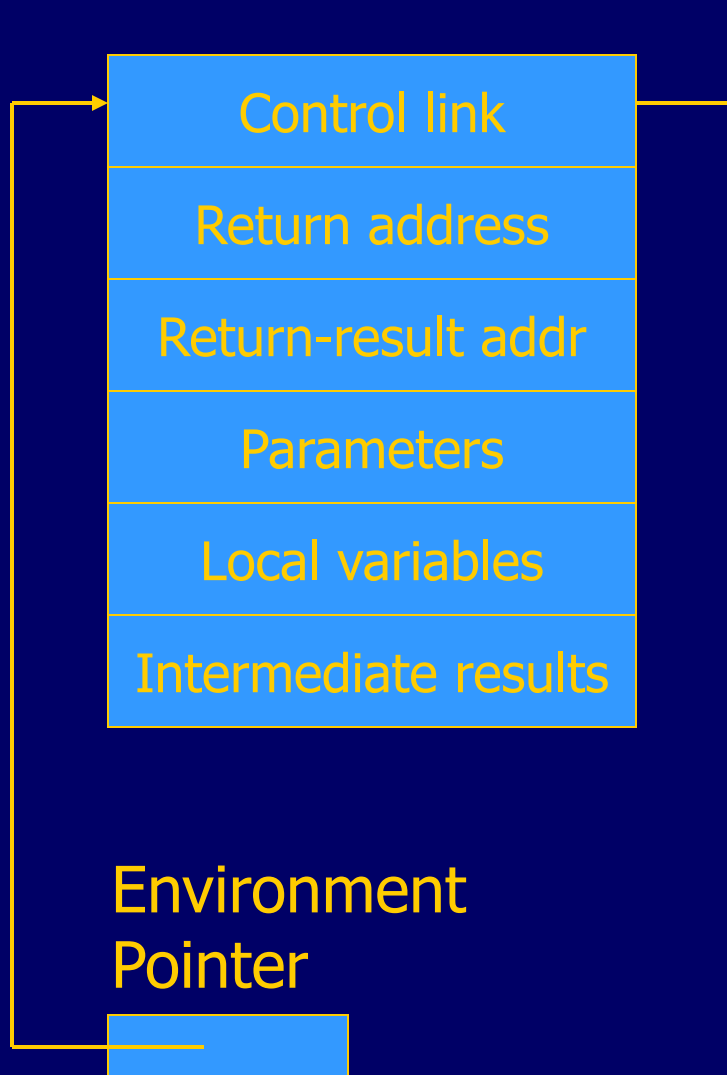
 <function body>

}

◆ Activation record must include space for

- parameters
- return address
- local variables, intermediate results
- return value (an intermediate result)
- location to put return value on function exit

Activation record for function



◆ Return address

- Location of code to execute on function return

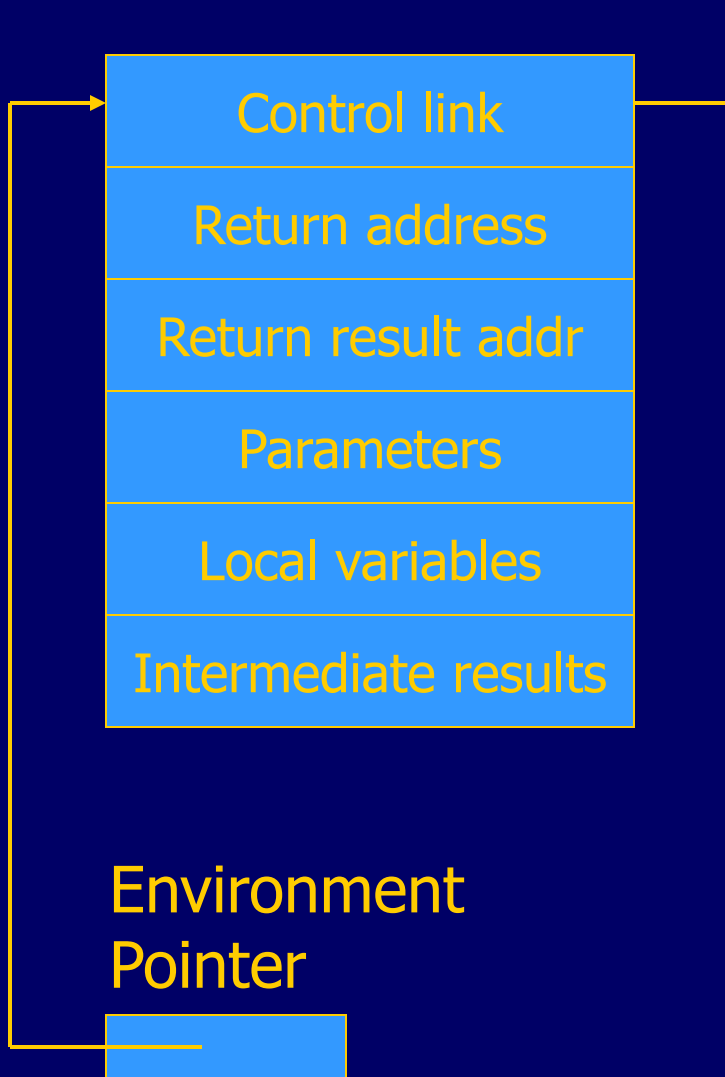
◆ Return-result address

- Address in activation record of calling block to receive return address

◆ Parameters

- Locations to contain data from calling block

Example



◆ Function

$\text{fact}(n) = \text{if } n \leq 1 \text{ then } 1$
 $\text{else } n * \text{fact}(n-1)$

- Return result address
- location to put $\text{fact}(n)$

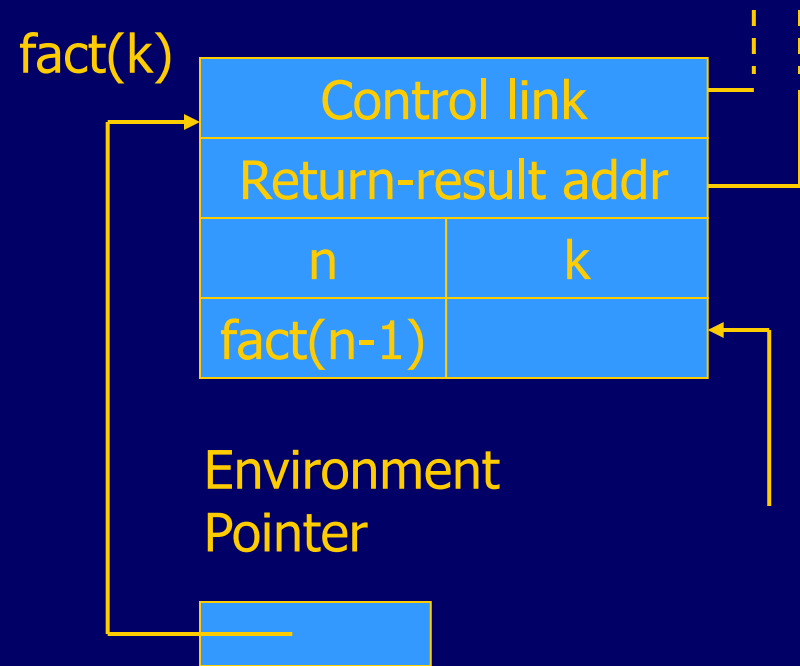
◆ Parameter

- set to value of n by calling sequence

◆ Intermediate result

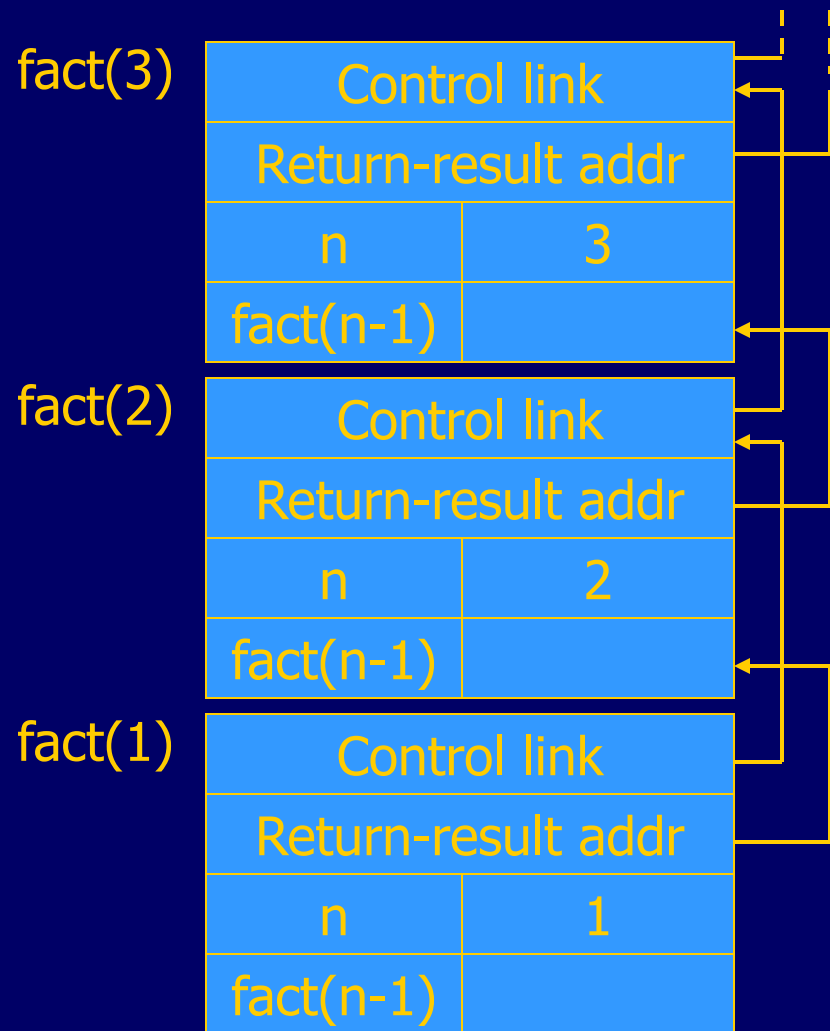
- locations to contain value of $\text{fact}(n-1)$

Function call



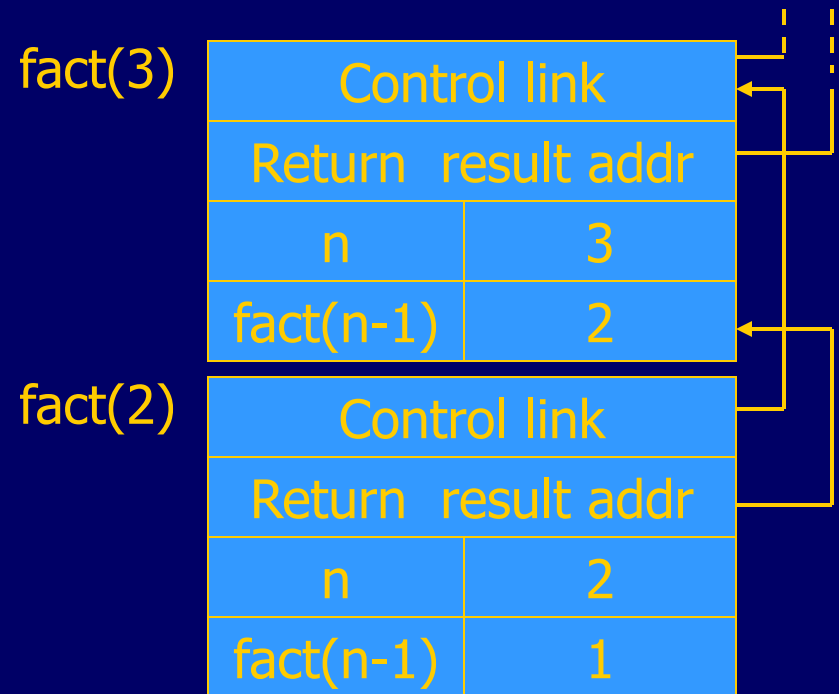
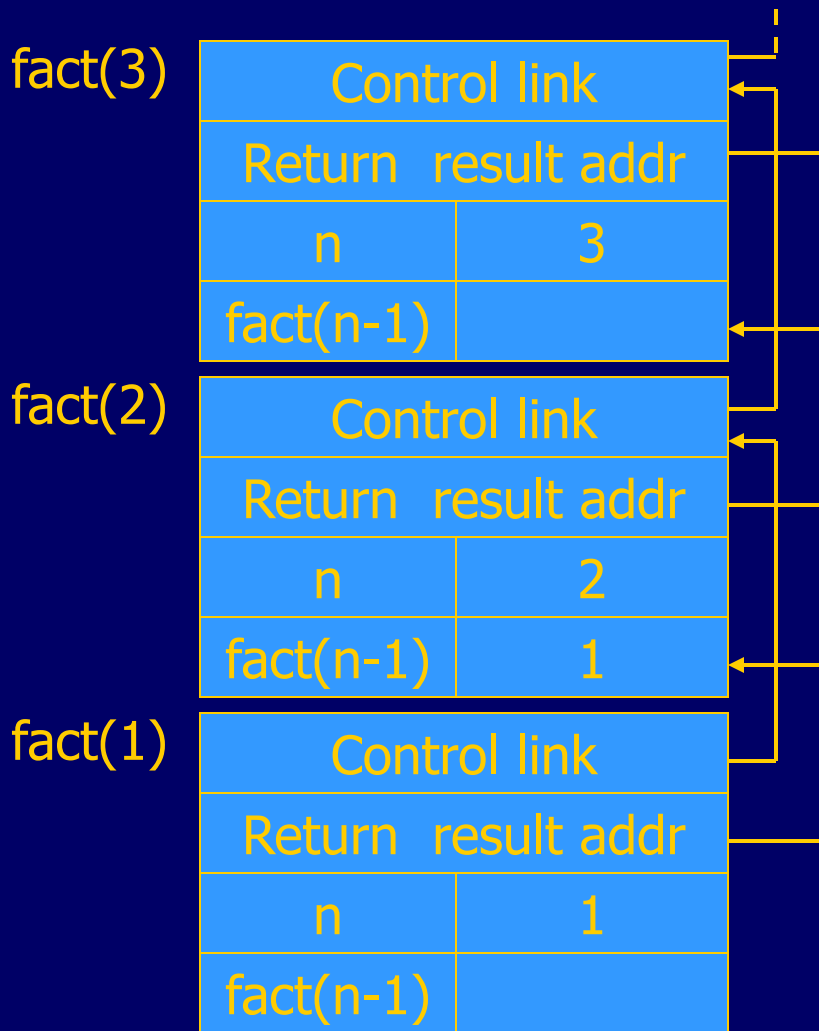
`fact(n) = if $n \leq 1$ then 1
else $n * \text{fact}(n-1)$`

Return address omitted; would
be ptr into code segment



Function return next slide →

Function return



$\text{fact}(n) = \text{if } n \leq 1 \text{ then } 1$
 $\text{else } n * \text{fact}(n-1)$

Topics for first-order functions

◆ Parameter passing

- pass-by-value: copy value to new activation record
- pass-by-reference: copy ptr to new activation record

◆ Access to global variables

- global variables are contained in an activation record higher “up” the stack

◆ Tail recursion

- an optimization for certain recursive functions

See this yourself: write factorial and run under debugger

L-values vs. R-values

◆ Assignment $x := \text{exp}$ is compiled into:

- Compute the **address** of x
- Compute the **value** of exp
- Store the value of exp into the address of x

◆ Generalization

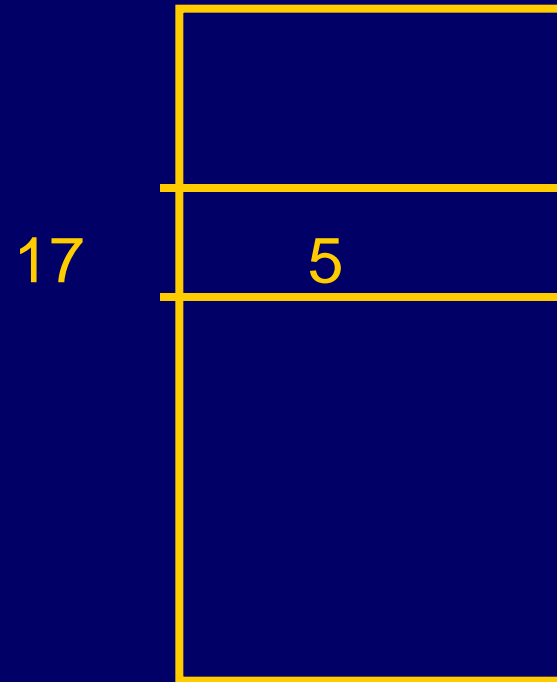
- R-value
 - Maps program expressions into Context values
- L-value
 - Maps program expressions into locations
 - Not always defined
- Java has no small L-values

A Simple Example

```
int x = 5;
```

```
x = x + 1;
```

Runtime memory



A Simple Example

```
int x = 5;
```

```
lvalue(x)=17, rvalue(x) =5
```

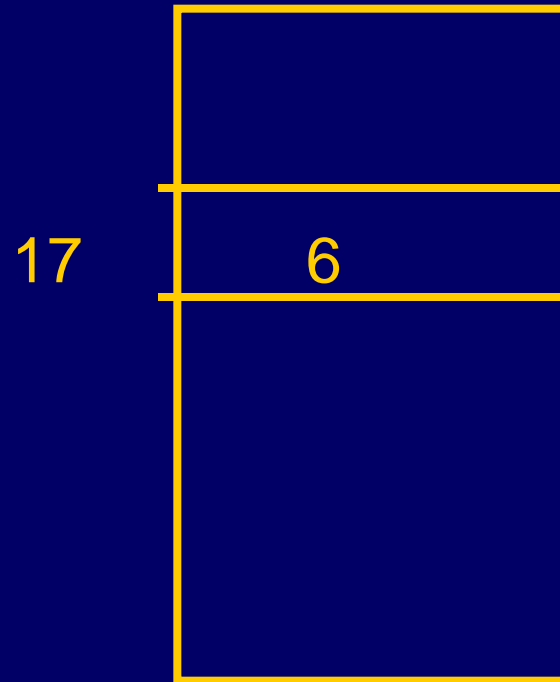
```
lvalue(5)=⊥, rvalue(5)=5
```

```
    x = x + 1;
```

```
lvalue(x)=17, rvalue(x) =5
```

```
lvalue(5)=⊥, rvalue(5)=5
```

Runtime memory



Partial rules for Lvalue in C

- ◆ Type of e is pointer to T
- ◆ Type of e1 is integer
- ◆ lvalue(e2) ≠ undefined

exp	lvalue	rvalue
id	location(id)	content(location(id))
const	undefined	value(const)
*e	rvalue(e)	content(rvalue(e))
&e2	undefined	lvalue(e2)
e + e1	undefined	rvalue(e)+sizeof(T)*rvalue(e1)

Parameter passing

◆ Pass-by-reference

- Place L-value (address) in activation record
- Function can assign to variable that is passed

◆ Pass-by-value

- Place R-value (contents) in activation record
- Function cannot change value of caller's variable
- Reduces aliasing (alias: two names refer to same loc)

Example

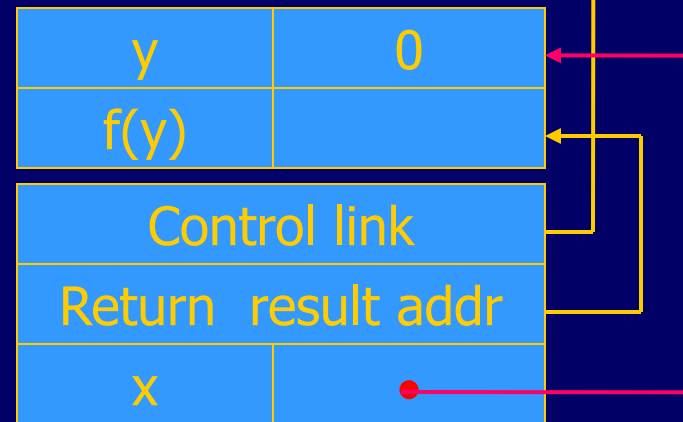
pseudo-code

```
function f (x) =  
  { x = x+1; return x; }  
var y = 0;  
print (f(y)+y);
```

pass-by-ref

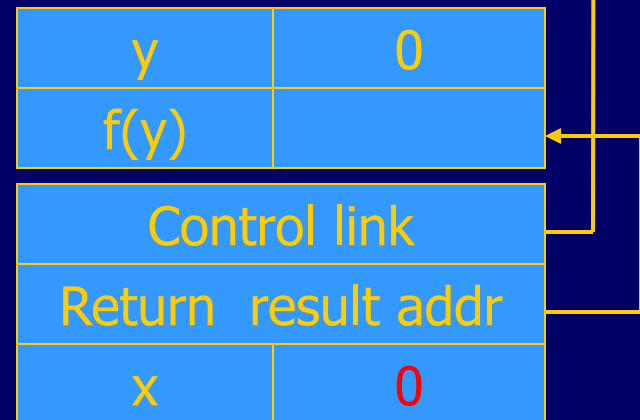
f(y)

activation records



pass-by-value

f(y)



Access to global variables

◆ Two possible scoping conventions

- Static scope: refer to closest enclosing block
- Dynamic scope: most recent activation record on stack

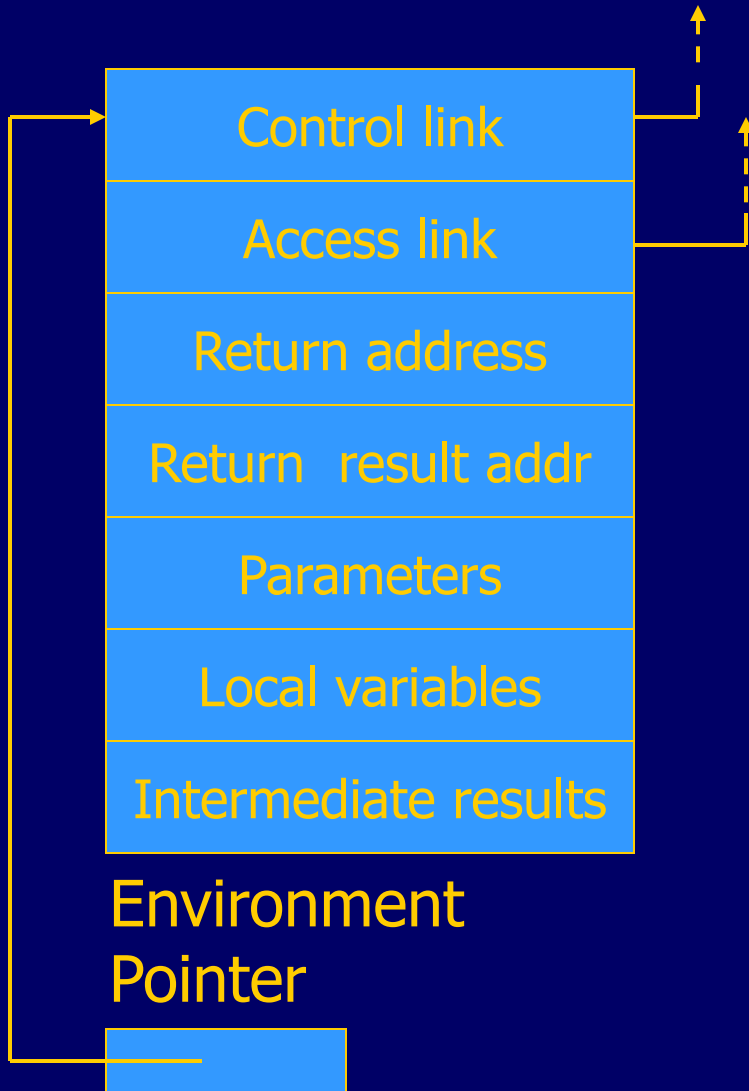
◆ Example

```
var x=1;
function g(z) { return x+z; }
function f(y) {
    var x = y+1;
    return g(y*x);
}
f(3);
```

outer block	x	1
f(3)	y	3
	x	4
g(12)	z	12

Which x is used for expression $x+z$?

Activation record for static scope



◆ Control link

- Link to activation record of previous (calling) block

◆ Access link

- Link to activation record of closest enclosing block in program text

◆ Difference

- Control link depends on dynamic behavior of prog
- Access link depends on static form of program text

Complex nesting structure

```
function m(...) {  
  var x=1;  
  ...  
  function n( ... ){  
    function g(z) { return x+z; }  
    ...  
    { ...  
      function f(y) {  
        var x = y+1;  
        return g(y*x); }  
      ...  
      f(3); ... }  
    ... n( ... ) ...}  
  ... m(...)
```

Simplify to

```
var x=1;  
function g(z) { return x+z; }  
function f(y)  
  { var x = y+1;  
    return g(y*x); }  
f(3);
```

Simplified code has same block nesting, if we follow convention that each declaration begins a new block.

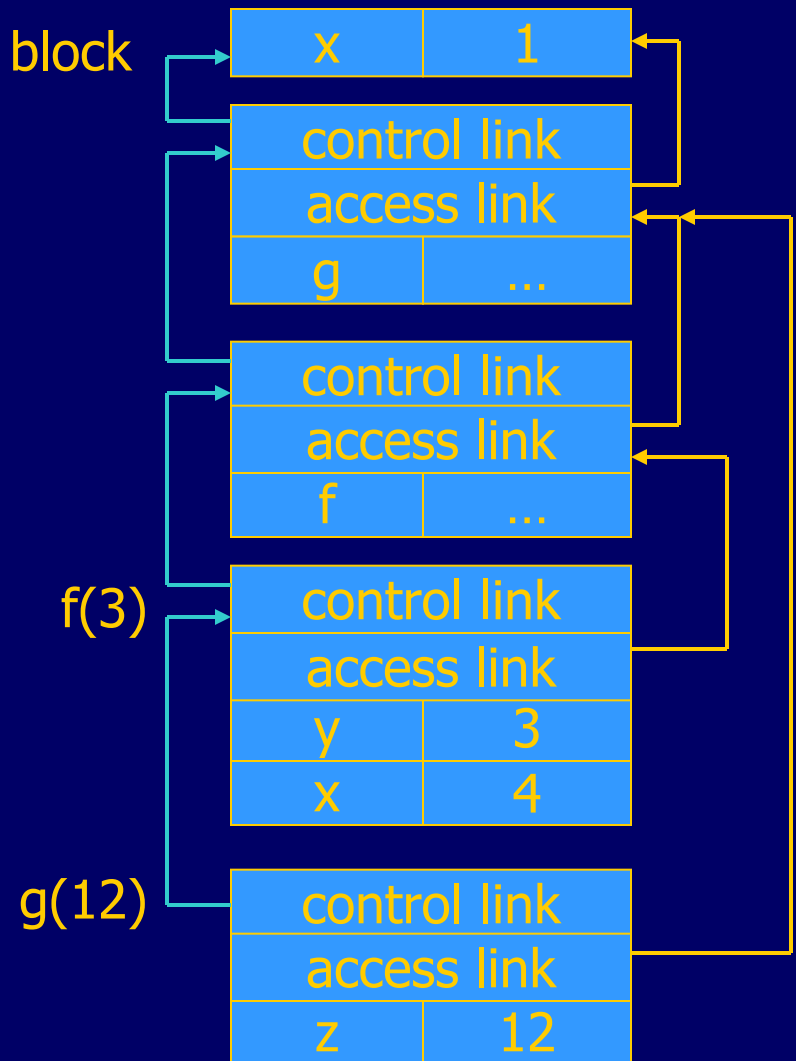
Static scope with access links

```
var x=1;
function g(z) = { return x+z; }
  function f(y) =
    { var x = y+1;
      return g(y*x); }
f(3);
```

Use access link to find global variable:

- Access link is always set to frame of closest enclosing lexical block
- For function body, this is block that contains function declaration

outer block



Tail recursion


(first-order case)

◆ Function g makes a *tail call* to function f if

- Return value of function f is return value of g

◆ Example

fun $g(x)$ = if $x > 0$ then $f(x)$ else $f(x) * 2$



◆ Optimization

- Can pop activation record on a tail call
- Especially useful for recursive tail call
 - next activation record has exactly same form

Example

Calculate least power of 2 greater than y

$f(1,3)$

control		↑
return val		↑
x	1	↑
y	3	

```
fun f(x,y) = if x>y
  then x
  else f(2*x, y);
f(1,3) + 7;
```

control		↑
return val		↑
x	1	↑
y	3	

control		↑
return val		↑
x	2	↑
y	3	

control		↑
return val		↑
x	4	↑
y	3	

Optimization

- Set return value address to that of caller

Question

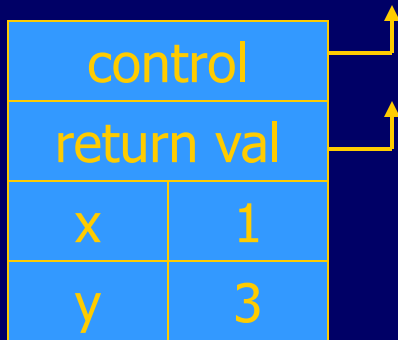
- Can we do the same with control link?

Optimization

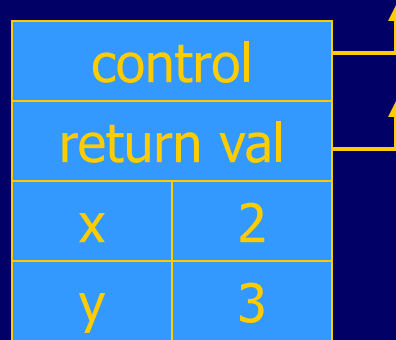
- avoid return to caller

Tail recursion elimination

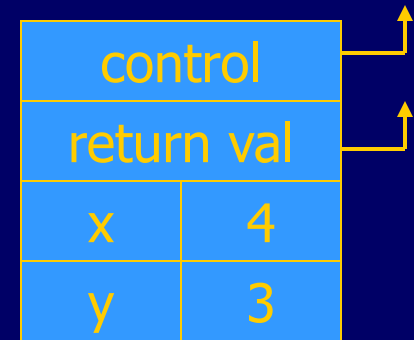
f(1,3)



f(2,3)



f(4,3)



```
fun f(x,y) = if x>y  
  then x  
  else f(2*x, y);  
f(1,3);
```

Optimization

- pop followed by push = reuse activation record in place

Conclusion

- Tail recursive function equiv to iterative loop

Tail recursion and iteration

f(1,3)

control		↑
return val		↑
x	1	
y	3	

f(2,3)

control		↑
return val		↑
x	2	
y	3	

f(4,3)

control		↑
return val		↑
x	4	
y	3	

```
fun f(x,y) = if x > y
  then x
  else f(2*x, y);
f(1,y);
```

test

loop body

initial value

```
function g(y) {
  var x = 1;
  while (!x > y)
    x = 2*x;
  return x;
}
```

Higher-Order Functions

◆ Language features

- Functions passed as arguments
- Functions that return functions from nested blocks
- Need to maintain environment of function

◆ Simpler case

- Function passed as argument
- Need pointer to activation record “higher up” in stack

◆ More complicated second case

- Function returned as result of function call
- Need to keep activation record of returning function

Pass function as argument

OCaml

```
let x = 4 in
  let f = fun y -> x*y in
    let g = fun h ->
      let x=7
      in
      h(3) + x
    in
    g(f)
```

Pseudo-JavaScript

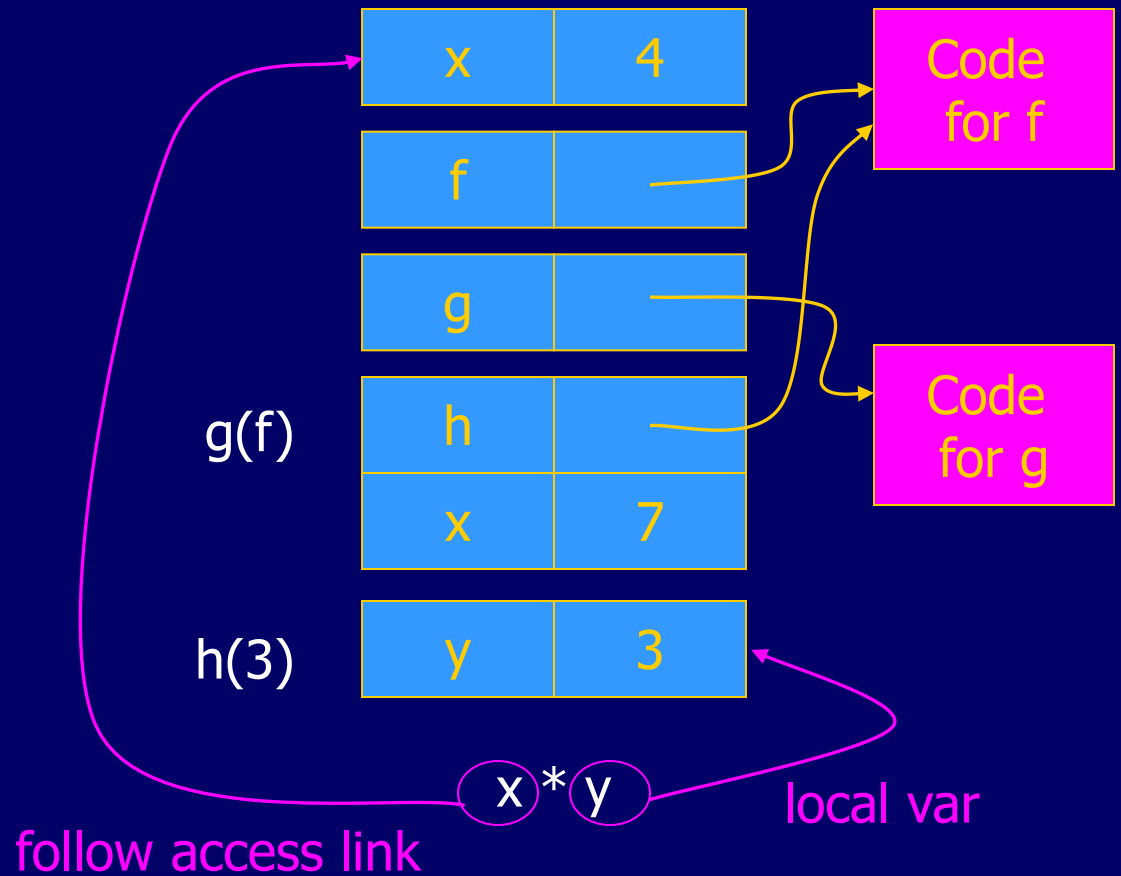
```
{ var x = 4;
  { function f(y) {return x*y};
    { function g(h) {
      var x = 7;
      return h(3) + x;
    };
    g(f);
  }
}
```

There are two declarations of x

Which one is used for each occurrence of x ?

Static Scope for Function Argument

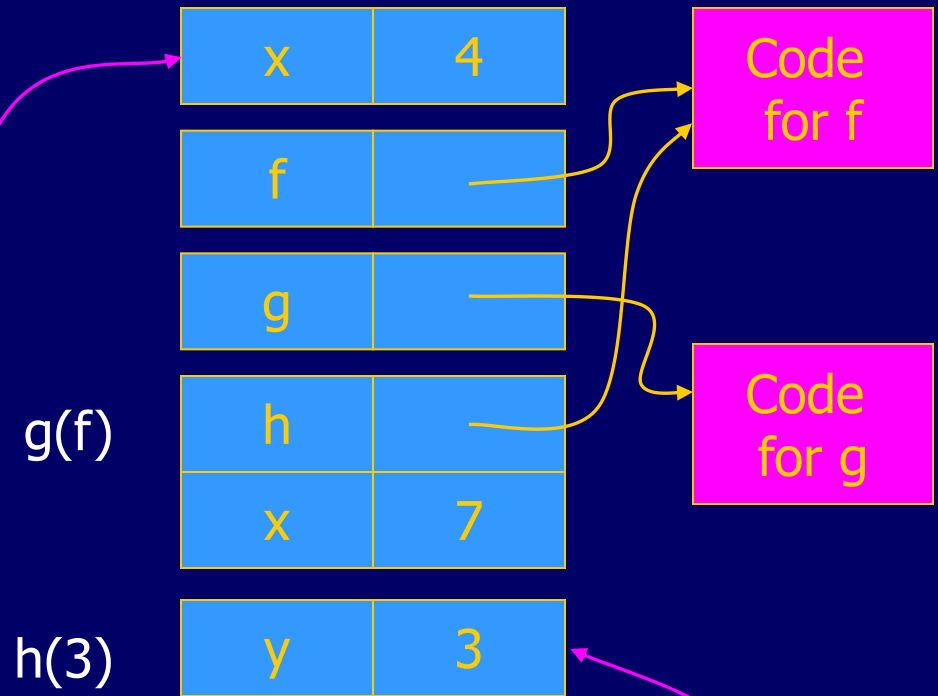
```
let x = 4 in
  let f = fun -> x*y in
    let g = fun h ->
      let
        int x=7
      in
        h(3) + x
    in
      g(f)
```



How is access link for `h(3)` set?

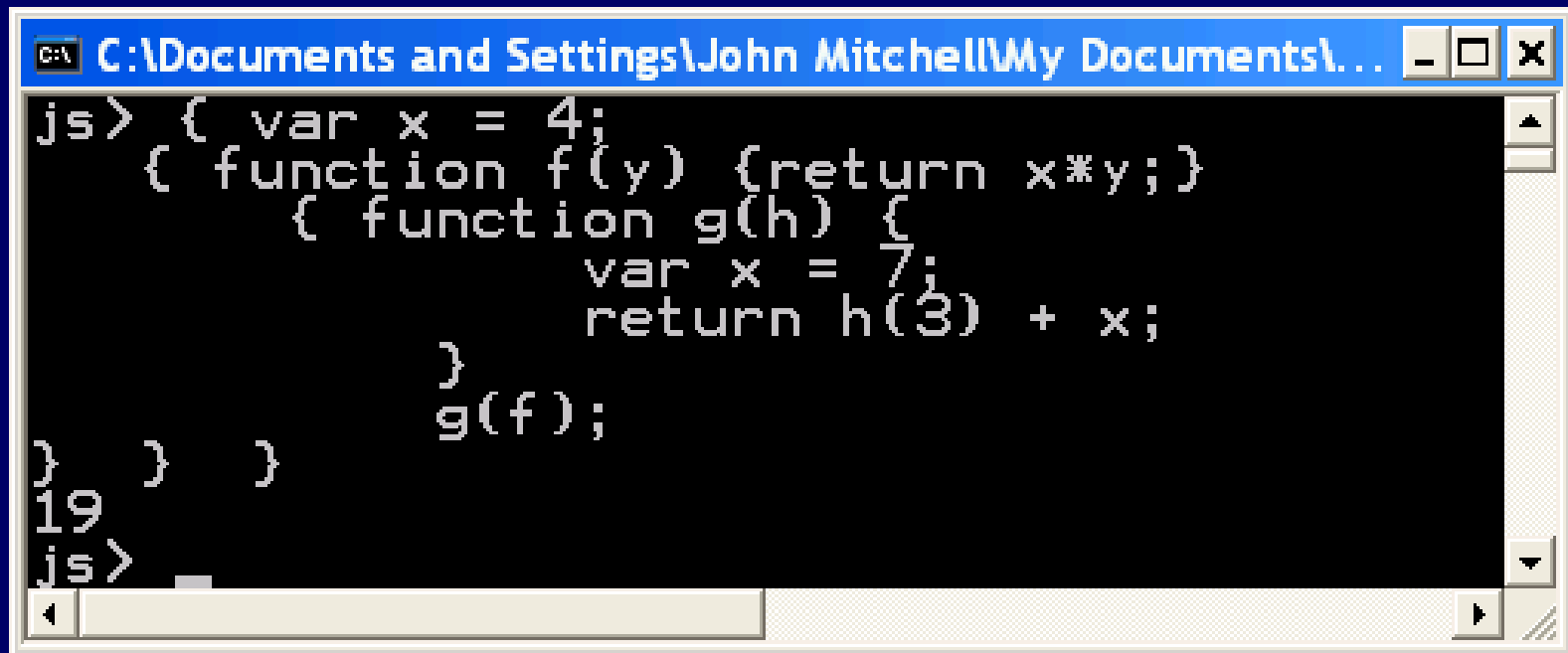
Static Scope for Function Argument

```
{ var x = 4;  
  { function f(y) {return x*y};  
    { function g(h) {  
      int x=7;  
      return h(3) + x;  
    };  
    g(f);  
  }  
}
```



How is access link for `h(3)` set?

Result of function call



```
js> { var x = 4;
      { function f(y) {return x*y;}
        { function g(h) {
          var x = 7;
          return h(3) + x;
        }
        g(f);
      }
    }
19
js>
```

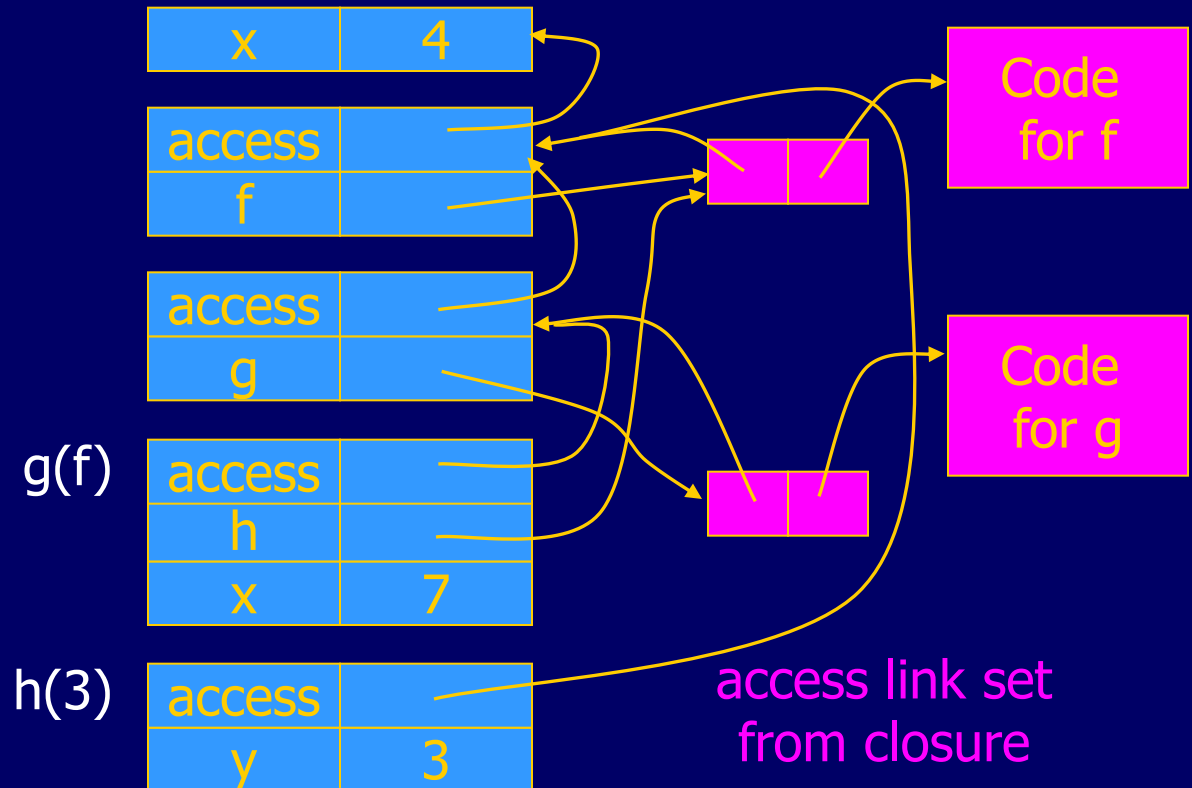
Closures

- ◆ Function value is pair *closure* = $\langle env, code \rangle$
- ◆ When a function represented by a closure is called,
 - Allocate activation record for call (as always)
 - Set the access link in the activation record using the environment pointer from the closure

Function Argument and Closures

Run-time stack with access links

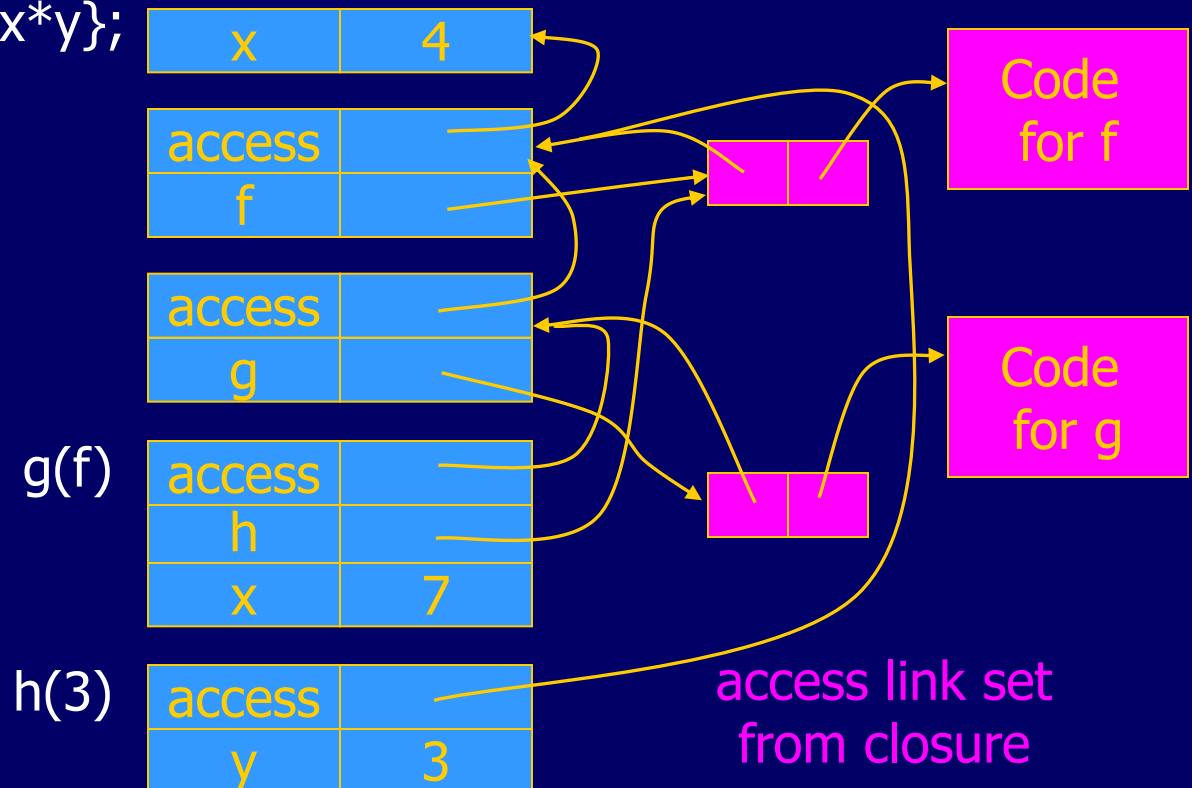
```
let x = 4 in
  let f = fun y->x*y in
    let g = fun h ->
      let
        x=7
      in
        h(3) + x
    in g(f)
```



Function Argument and Closures

Run-time stack with access links

```
{ var x = 4;  
  { function f(y){return x*y};  
    { function g(h) {  
      int x=7;  
      return h(3)+x;  
    };  
    g(f);  
  }  
}
```



Summary: Function Arguments

- ◆ Use closure to maintain a pointer to the static environment of a function body
- ◆ When called, set access link from closure
- ◆ All access links point “up” in stack
 - May jump past activ records to find global vars
 - Still deallocate activ records using stack (lifo) order

Return Function as Result

◆ Language feature

- Functions that return “new” functions
- Need to maintain environment of function

◆ Example

```
function compose(f,g)
  {return function(x) { return g(f (x)) }};
```

◆ Function “created” dynamically

- expression with free variables
values are determined at run time
- function value is closure = $\langle \text{env}, \text{code} \rangle$
- code *not* compiled dynamically (in most languages)

Example: Return fctn with private state

OCaml

```
let mk_counter = fun init ->
  let count = ref init in
  let counter = fun inc ->
    (count := !count + inc; !count)
  in
    counter
in
  let c = mk_counter 1
  in
    c(2) + c(2)
```

- Function to “make counter” returns a closure
- How is correct value of count determined in `c(2)` ?

Example: Return fctn with private state

JS

```
function mk_counter (init) {  
    var count = init;  
    function counter(inc) {count=count+inc; return count};  
    return counter};  
var c = mk_counter(1);  
c(2) + c(2);
```

Function to “make counter” returns a closure

How is correct value of count determined in call `c(2)` ?

Function Results and Closures

```

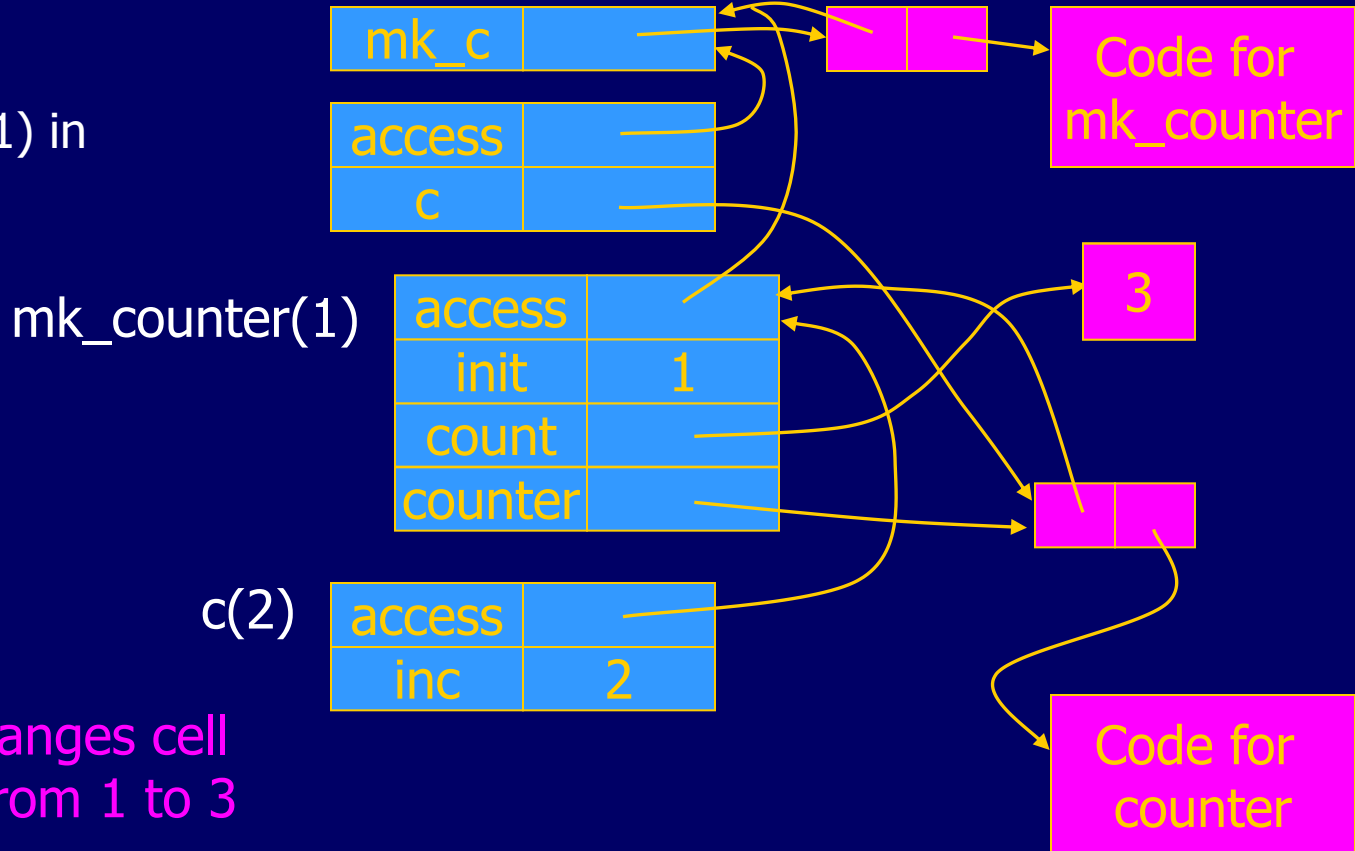
let mk_counter = fun init ->
  let count = ref init in
    let counter = fun inc -> (count := !count + inc; !count)
    in counter

```

```

in
let c = mk_counter(1) in
c(2) + c(2)

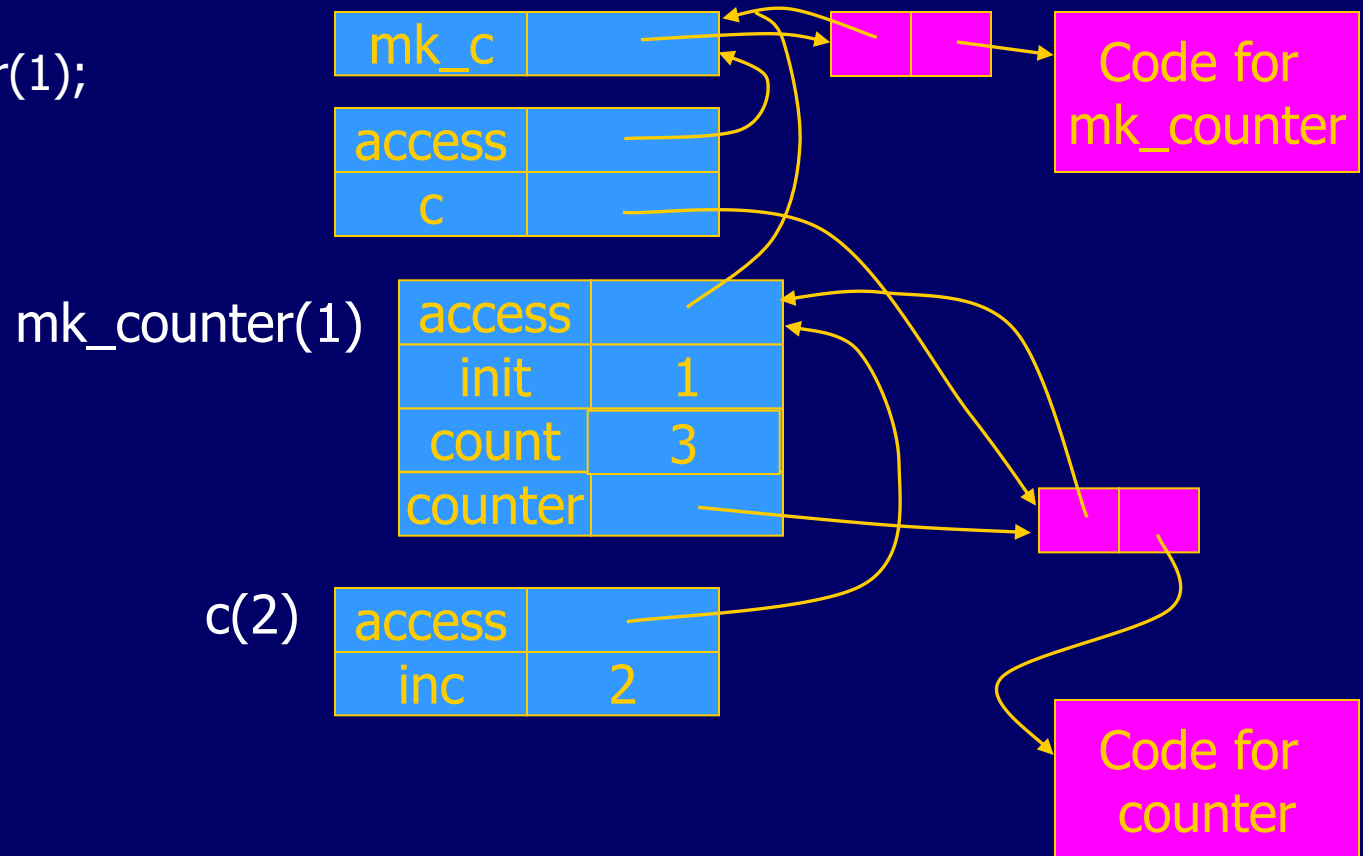
```



Call changes cell value from 1 to 3

Function Results and Closures

```
function mk_counter (init) {
  var count = init;
  function counter(inc) {count=count+inc; return count};
  return counter};
var c = mk_counter(1);
c(2) + c(2);
```



Closures in Web programming

◆ Useful for event handlers in Web programming:

```
function AppendButton(container, name, message) {  
    var btn = document.createElement('button');  
    btn.innerHTML = name;  
    btn.onclick = function (evt) { alert(message); }  
    container.appendChild(btn);  
}
```

◆ Environment pointer lets the button's click handler find the message to display

Summary: Return Function Results

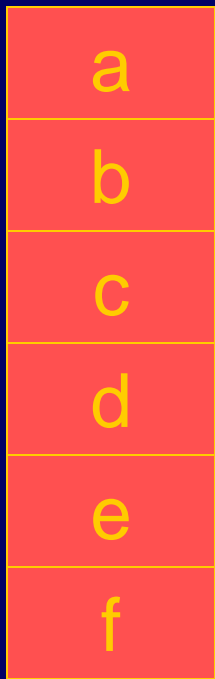
- ◆ Use closure to maintain static environment
- ◆ May need to keep activation records after return
 - Stack (lifo) order fails!
- ◆ Possible “stack” implementation
 - Forget about explicit deallocation
 - Put activation records on heap
 - Invoke garbage collector as needed
 - Not as totally crazy as it sounds
 - May only need to search reachable data

Summary of scope issues

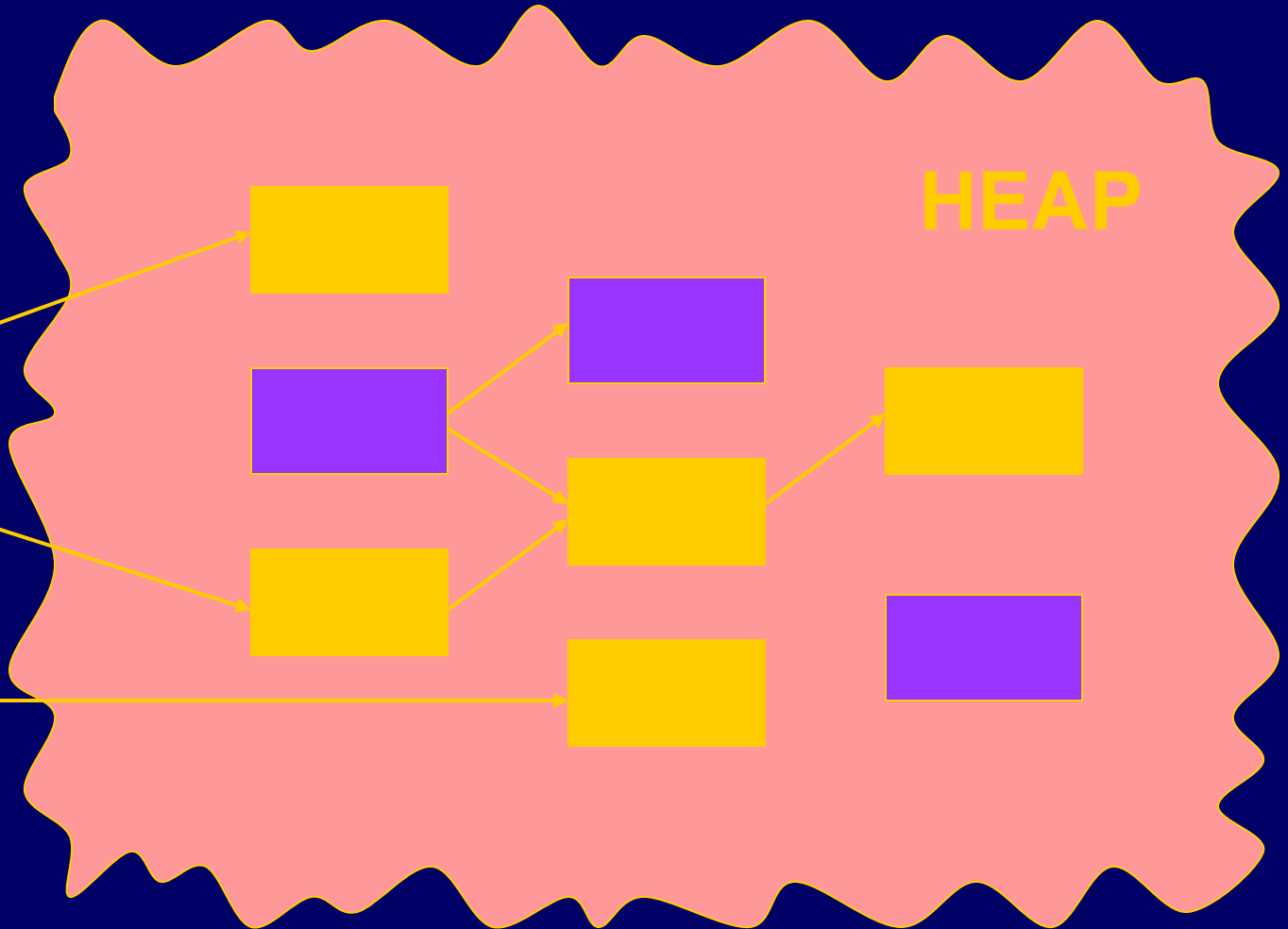
- ◆ Block-structured lang uses stack of activation records
 - Activation records contain parameters, local vars, ...
 - Also pointers to enclosing scope
- ◆ Several different parameter passing mechanisms
- ◆ Tail calls may be optimized
- ◆ Function parameters/results require closures
 - Closure environment pointer used on function call
 - Stack deallocation may fail if function returned from call
 - Closures *not* needed if functions not in nested blocks

Garbage Collection

ROOT SET



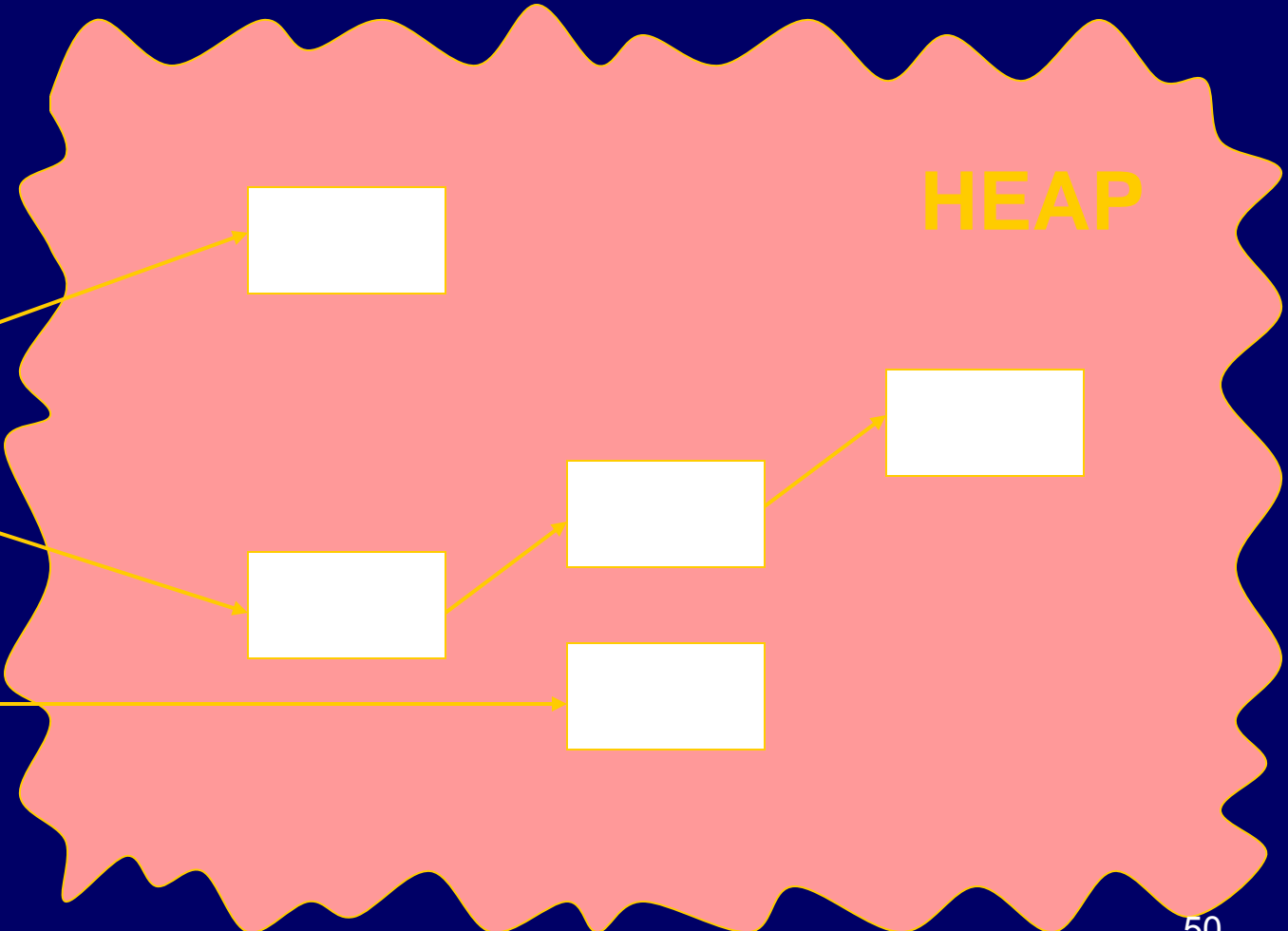
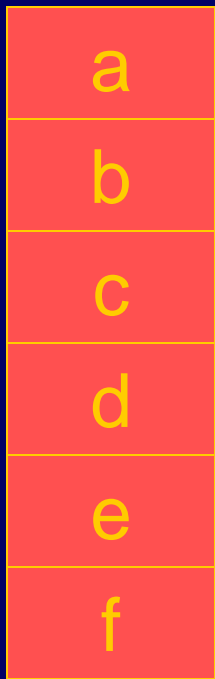
Stack



HEAP

Garbage Collection

ROOT SET



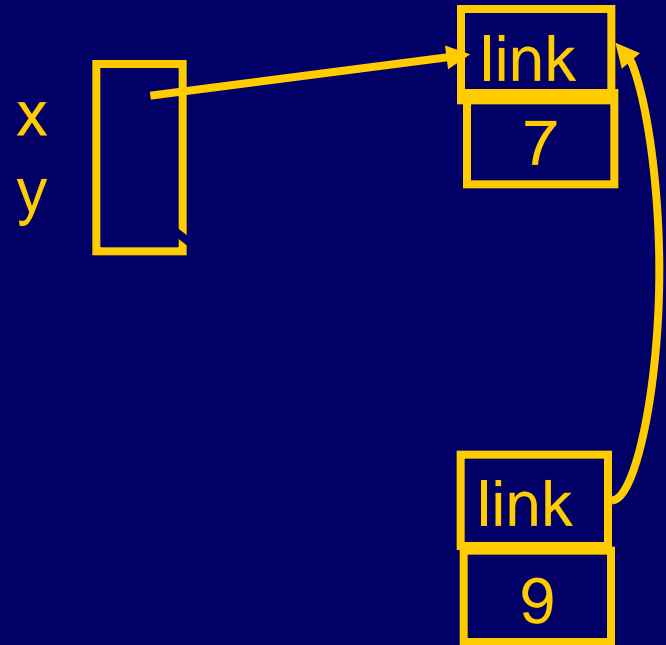
Stack

What is garbage collection

- ◆ The runtime environment reuse chunks that were allocated but are not subsequently used garbage chunks
 - not live
- ◆ It is undecidable to find the garbage chunks:
 - Decidability of liveness
 - Decidability of type information
- ◆ **conservative collection**
 - every live chunk is identified
 - some garbage runtime chunk are not identified
- ◆ Find the reachable chunks via pointer chains
- ◆ Often done in the allocation function

stack

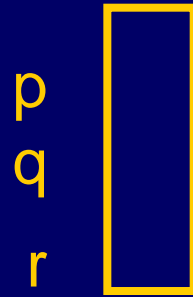
heap



```
typedef struct list {struct list *link; int key} *List;
typedef struct tree {int key;
                    struct tree *left;
                    struct tree *right} *Tree;
foo() { List x = cons(NULL, 7);
      List y = cons(x, 9);
      x->link = y;
      }
void main() {
  Tree p, r; int q;
  foo();
  p = maketree(); r = p->right;
  q= r->key;
  showtree(r);}
```

stack

heap

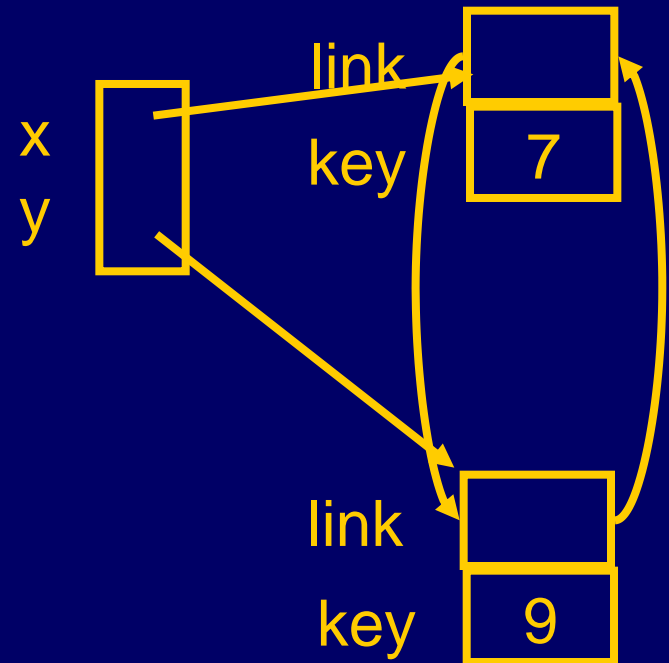


```
typedef struct list {struct list *link; int key} *List;
typedef struct tree {int key;
                    struct tree *left;
                    struct tree *right} *Tree;

foo() { List x = cons(NULL, 7);
      List y = cons(x, 9);
      x->link = y;
      }

void main() {
  Tree p, r; int q;
  foo();
  p = maketree(); r = p->right;
  q= r->key;
  showtree(r);}

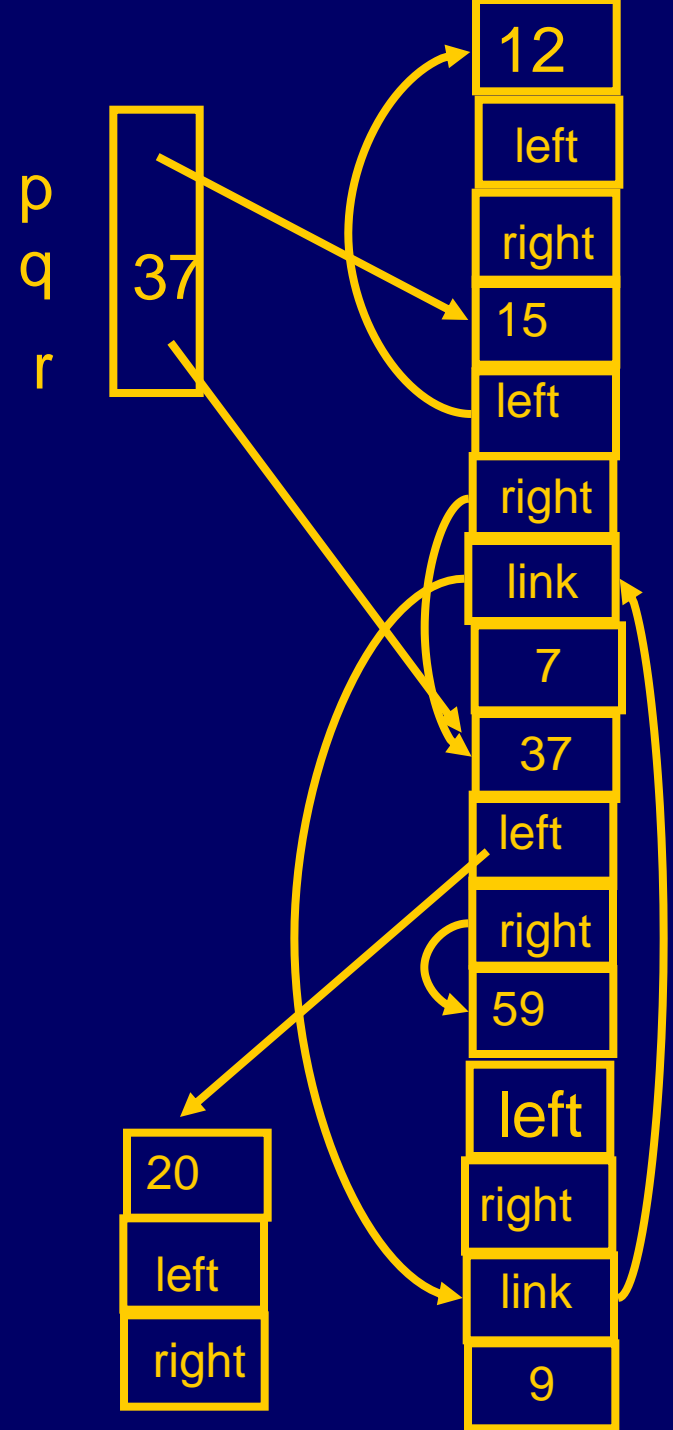
```



```

typedef struct list {struct list *link; int key}
*List;
typedef struct tree {int key;
                    struct tree *left;
                    struct tree *right} *Tree;
foo() { List x = create_list(NULL, 7);
      List y = create_list(x, 9);
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  p = maketree(); r = p->right;
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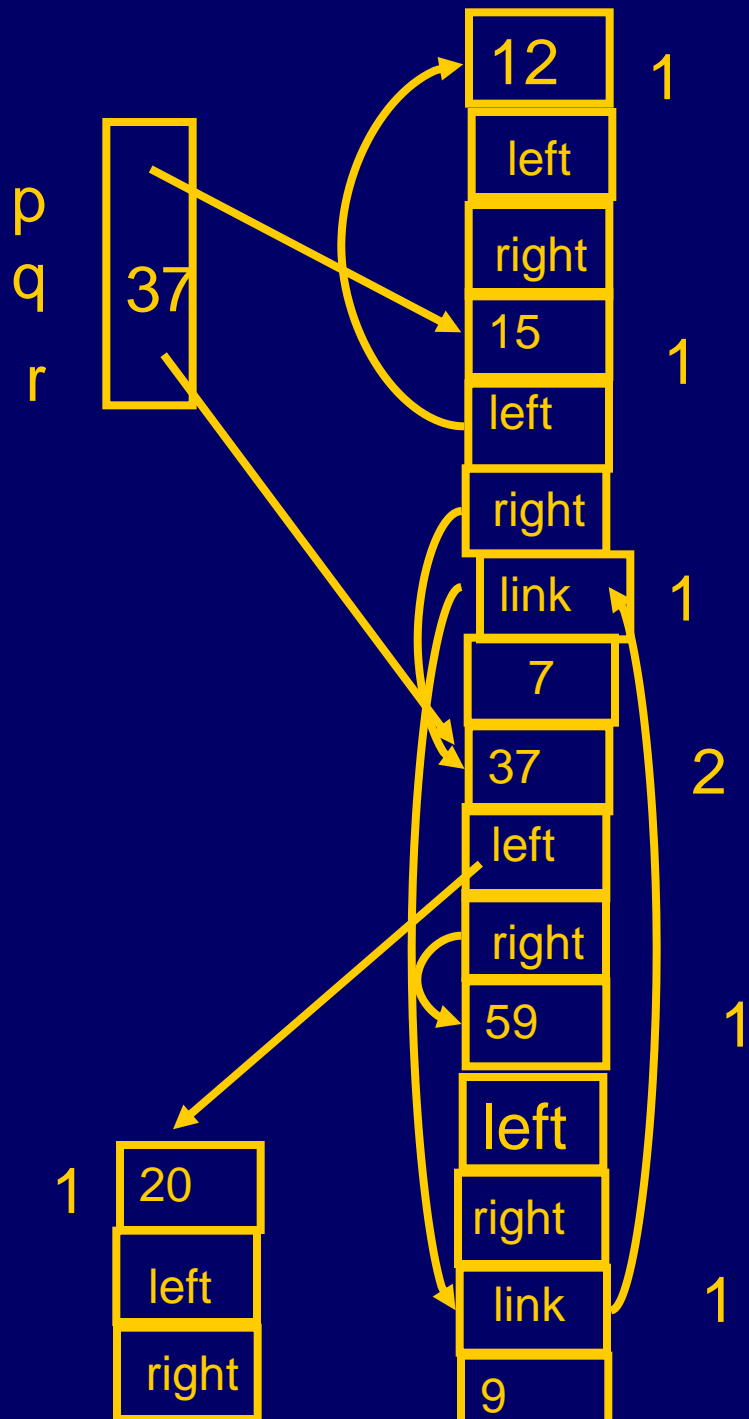
Garbage Collection Techniques

◆ Tracing

- Scan the reachable heaps from the root
- Release unreachable elements
- Cost proportional to reachable heap

◆ Reference Counting

- Maintain a counter of references to each chunk of memory
- The compiler generates the update code for references when pointers are manipulated
- Release objects with zero reference counter
- Constant cost



Garbage Collection vs. Explicit Memory Deallocation

- ◆ Faster program development
- ◆ Less error prone
- ◆ Can lead to faster programs
 - Can improve locality of references
- ◆ Support very general programming styles, e.g. higher order and OO programming
- ◆ Standard in ML, Java, C#, Javascript
- ◆ Supported in C and C++ via separate libraries
- ◆ May require more space
- ◆ Needs a large memory
- ◆ Can lead to long pauses
- ◆ Can change locality of references
- ◆ Effectiveness depends on programming language and style
- ◆ Hides documentation
- ◆ More trusted code

Summary

- ◆ Runtime memory management is crucial for functionality and correctness
- ◆ Lexical scope is natural
 - Becomes tricky with higher order functions
 - Closures
- ◆ Garbage Collection permits general programming style