Natural Language Processing

Discriminative models for syntactic parsing
<table>
<thead>
<tr>
<th>Generation Method</th>
<th>Tagging Method</th>
<th>Parsing Method</th>
</tr>
</thead>
<tbody>
<tr>
<td>Generative</td>
<td>HMMs</td>
<td>PCFGs</td>
</tr>
<tr>
<td>Log-linear</td>
<td>Greedy</td>
<td>Transition-based parsing</td>
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<tr>
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<td>History-based</td>
<td>Viterbi</td>
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<td>CKY</td>
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<tr>
<td></td>
<td>Global</td>
<td>forward-backward</td>
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<td></td>
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<td>Inside-outside</td>
</tr>
</tbody>
</table>
Motivation

- Incorporate arbitrary overlapping features for discrimination

Tagging:

- word/tag pairs
- prefixes <5/tag pairs
- suffixes <5/tag pairs
- tag trigrams
- tag bigrams
- tag unigrams
- word/tag pairs for previous word
- word/tag pairs for subsequent word
Motivation

- Parsing (CRF parsing in this case):
  - Conjunction of rule and
    - first word, last word, word before split, word after split, word before, word after
  - Replace rule with parent category
  - Span shape
  - Span length (binned)
Log-linear models

- **Input**: domain $X$, label set $Y$

- **Feature function**:
  \[ f : X \times Y \rightarrow \mathbb{R}^m \]

- **Parameters**:
  \[ \theta \in \mathbb{R}^m \]

- **Output**: $p(y \mid x)$
  \[
p_{\theta}(y \mid x) = \frac{e^{f(x,y)\top \theta}}{\sum_{y' \in Y} e^{f(x,y')\top \theta}}
  \]
Plan

• Locally normalized models
  • AKA, transition-based, greedy parsers
• Globally normalized models (CRF)
• Neural CRF
Locally-normalized
Log-linear models for tagging

- Input: \( w_1 \ldots w_n \)
- Output: \( t_1 \ldots t_n \)

\[
p(t_1, \ldots, t_n \mid w_1, \ldots, w_n, t_{-1}, t_0) = \prod_{i=1}^{n} p(t_i \mid t_{-1}, \ldots, t_{i-1}, w_1, \ldots, w_n)
\]

\[
= \prod_{i=1}^{n} p(t_i \mid t_{i-2}, t_{i-1}, w_1, \ldots, w_n)
\]

- **Learning**: estimate \( p(t_i \mid t_{i-2}, t_{i-1}, w_1, \ldots, w_n) \)
- **Decoding**: Viterbi
  - \( \text{argmax}_{t_1 \ldots t_n} \log p(t_1 \ldots t_n \mid w_1 \ldots w_n, t_{-1}, t_0) \)
Log-linear models for parsing

• Goal: define a model for $p(t \mid s)$

• $t$ is a tree

• $s$ is the sentence $w_1 \ldots w_n$

• Difficulty: In tagging, we made tagging decisions left-to-right. What is the order for parsing?
Outline of approach

• Represent a tree as a sequence of $m$ decisions:

$$T = (d_1, d_2, \ldots, d_m)$$

• Tree probability:

$$p(t \mid s) = \prod_{i=1}^{m} p(d_i \mid d_1, \ldots d_{i-1}, s)$$

• Decision probability is a log-linear model:

$$p(d_i \mid d_1, \ldots d_{i-1}, s) = \frac{e^{f(d_1, \ldots, d_{i-1}, d_i, s) \top \theta}}{\sum_{d'} e^{f(d_1, \ldots, d_{i-1}, d', s) \top \theta}}$$

• Search for high(est?) probability tree based on $p(t \mid s)$
Decomposing a tree
Ratnaparkhi, 1997

- Bottom-up, left-to-right transition system
- Three layers of decisions
  - Part-of-speech tags
  - Chunks
  - The rest
Layer 1: part-of-speech tags

- (d₁, …, dₙ) = (DT, NN, VBD, DT, NN, IN, DT, NN)

- We define the first $n$ steps in the total $m$ decisions:

  - (d₁, …, dₙ) = (DT, NN, VBD, DT, NN, IN, DT, NN)

  the lawyer questioned the witness about the revolver
Layer 2: chunks

- **Chunks**: any phrase, where all children are part-of-speech tags (height 2 trees)
- **Motivation**: can be recovered accurately and improve layer 3
Layer 2: chunks

<table>
<thead>
<tr>
<th>Start(NP)</th>
<th>Join(NP)</th>
<th>Other</th>
<th>Start(NP)</th>
<th>Join(NP)</th>
<th>Other</th>
<th>Start(NP)</th>
<th>Join(NP)</th>
</tr>
</thead>
<tbody>
<tr>
<td>DT</td>
<td>NN</td>
<td>VBD</td>
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<tr>
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<td>the</td>
<td>witness</td>
<td>about</td>
<td>the</td>
<td>revolver</td>
</tr>
</tbody>
</table>

- Next \( n \) decisions are chunking decisions:
  - \((d_1, \ldots, d_n, d_{n+1}, \ldots, d_{2n}) = (DT, NN, VBD, DT, NN, IN, DT, NN, Start(NP), Join(NP), Other, Start(NP), Join(NP), Other, Start(NP), Join(NP))\)
Layer 3: the rest

- Alternate between two classes of actions:
  - $\text{Join}(X)$ or $\text{Start}(X)$ where $X$ is a label (NP, VP, …)
  - $\text{Check}=$YES or $\text{Check}=$No

- Meaning:
  - $\text{Start}(X)$: start a new constituent with label $X$
  - $\text{Join}(X)$: continue a constituent with label $X$
    - Both act on leftmost constituent not rooted by $\text{Start}()$ or $\text{Join}()$
  - Check: “NO” does nothing, “YES” finalizes a constituent
Illustration

The lawyer questioned the witness about the revolver.

Leftmost constituent without Start() or Join()
the lawyer questioned the witness about the revolver

Leftmost constituent without Start() or Join()
the lawyer questioned the witness about the revolver

Leftmost constituent without Start() or Join()
Illustration

Start(S)

NP

VBD

NP

IN

NP

DT

NN

VBD

DT

NN

IN

DT

NN

the

lawyer

questioned

the

witness

about

the

revolver

Leftmost constituent without Start() or Join()

Start(S)

Check=NO
Illustration

Start(S)
Start(VP)
NP
VBD
NP
IN
NP

DT
NN
VBD
DT
NN
IN
DT
NN

the
lawyer
questioned
the
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about
the
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Leftmost constituent without Start() or Join()
Illustration

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</tr>
<tr>
<td>NN</td>
<td>DT</td>
</tr>
<tr>
<td>the revolver</td>
<td>NN</td>
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**Leftmost constituent without Start() or Join()**

Start(S)
Check=NO
Start(VP)
Check=NO
### Illustration

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<tr>
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<th>Start(VP)</th>
<th>Join(VP)</th>
<th>Leftmost constituent without Start() or Join()</th>
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<tr>
<td>NP</td>
<td>VBD</td>
<td>NP</td>
<td>the lawyer questioned the witness about the revolver</td>
</tr>
<tr>
<td>DT</td>
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**Start(S)**
- Check=NO

**Start(VP)**
- Check=NO

**Join(VP)**
- Check=NO
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Leftmost constituent without Start() or Join()
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**Leftmost constituent without Start() or Join()**

- Start(S) Check=NO
- Check=NO
- Start(VP) Check=NO
- Start(PP) Check=NO
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Leftmost constituent without Start() or Join()
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**Leftmost constituent without Start() or Join()**

- Start(S): Check=NO
- Start(VP): Check=NO
- Start(PP): Check=NO
- Join(PP): Check=YES
**Illustration**

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*Leftmost constituent without Start() or Join()*

- **Start(S)**: Check=NO
- **Join(PP)**: Check=NO
- **Start(PP)**: Check=NO
- **Join(VP)**: Check=NO
- **Start(VP)**: Check=NO
- **Start(S)**: Check=NO
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**Leftmost constituent without Start() or Join()**

Start(S)       Join(VP)       Join(PP)
Check=NO        Check=NO        Check=YES
Start(VP)      Start(PP)
Check=NO        Check=NO          

### Illustration

<table>
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Leftmost constituent without Start() or Join():

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<table>
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### Illustration

The lawyer questioned the witness about the revolver.

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<td></td>
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<td></td>
<td>about</td>
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<tr>
<td>Check=NO</td>
<td>Check=NO</td>
<td>Check=NO</td>
<td>Check=YES</td>
<td></td>
</tr>
</tbody>
</table>

Leftmost constituent without Start() or Join():

```
Start(S)  | Join(VP) | Join(PP)
Check=NO  | Check=NO | Check=NO
Start(VP) | Start(PP) | Check=YES
Check=NO  | Check=NO
```
**Illustration**

<table>
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</tr>
<tr>
<td>Check=NO</td>
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<td></td>
</tr>
</tbody>
</table>
Illustration

Start(S) | Start(VP) | Join(VP) | Start(PP) | Join(PP)
---|---|---|---|---
NP | VBD | NP | IN | NP
DT | NN | VBD | DT | NN | IN | DT | NN
the | lawyer | questioned | the | witness | about | the | revolver

Leftmost constituent without Start() or Join()
### Illustration

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**Leftmost constituent without Start() or Join()**

- **Start(S)**: Check=NO
- **Start(VP)**: Check=NO
- **Join(VP)**: Check=NO
- **Start(PP)**: Check=YES
- **Join(PP)**: Check=NO
Illustration

Start(S)    Start(VP)    Join(VP)    Start(PP)    Join(PP)
NP          VBD          NP          IN          NP
DT          NN           VBD          DT          NN
the          lawyer      questioned   the          witness
Start(S)    Join(VP)    Join(PP)
Check=NO    Check=NO    Check=YES
Start(VP)    Start(PP)
Check=NO    Check=NO
### Illustration

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Leftmost constituent without `Start()` or `Join()`

- **Start(S)**
  - Check=NO
- **Start(VP)**
  - Check=NO
- **Start(PP)**
  - Check=NO
- **Join(PP)**
  - Check=YES
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</table>

Leftmost constituent without Start() or Join()
Illustration

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**Leftmost constituent without Start() or Join()**

- Start(S) Check=NO
- Start(VP) Check=NO
- Start(PP) Check=NO
- Join(VP) Check=NO
- Join(PP) Check=YES
The lawyer questioned the witness about the revolver.

Leftmost constituent without Start() or Join():

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**Leftmost constituent without Start() or Join()**

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Leftmost constituent without Start() or Join()

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Check=NO            Check=NO            Check=NO
Start(VP)           Start(PP)           Check=NO
Check=NO            Check=NO            Check=YES
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<td>revolver</td>
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Leftmost constituent without Start() or Join():

```
Join(VP)
Check=YES
```
Illustration

Start(S)  Start(VP)  Join(VP)  PP
NP  VBD  NP  IN  NP
DT  NN  DT  NN  IN  DT  NN
the  lawyer  the  witness  about  the  revolver

Leftmost constituent without Start() or Join()

Join(S)
Check=YES
Illustration

<table>
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</tr>
<tr>
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<td></td>
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<td>about</td>
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### Illustration

- $d_1, \ldots, d_m = (\text{DT, NN, VBD, DT, NN, IN, DT, NN, Start(NP), Join(NP), Other, Start(NP), Join(NP), Other, Start(NP), Join(NP), Start(S), Check=NO, Start(VP), Check=NO, Join(VP), Check=NO, Start(PP), Check=NO, Join(PP), Check=NO, Start(S), Check=YES, Join(VP), Check=YES, Join(S), Check=YES})$
Log-linear model

\[ p(d_i \mid d_1, \ldots, d_{i-1}, s) = \frac{e^f(d_1, \ldots, d_{i-1}, d_i, s) \theta}{\sum d' e^f(d_1, \ldots, d_{i-1}, d', s) \theta} \]

- Denominator is over all possible actions at each point
Features

- Can condition on the partial trees we have built so far. Log-linear models allow arbitrary features.
- Especially if we do not do exact decoding
- **Tagging decisions**: similar to POS tags we saw
- **Chunking decisions**: Similar to tagging (word, previous chunks) + features over any POS tag
Layer 3 features

- For Start() and Join()
  - Head word, constituent label and start/join annotations of previous two trees
  - Head word and constituent label for current and next trees
  - Bi-gram and tri-gram features over multiple adjacent trees for words, tags and constituent labels
Layer 3 features

• For CHECK:
  • Various features over the proposed new tree
Search

• In POS tagging we could use Viterbi because we used a Markov assumption

\[ p(t_1, \ldots, t_n \mid w_1, \ldots, w_n, t_{-1}, t_0) = \prod_{i=1}^{n} p(t_i \mid t_{-1}, \ldots, t_{i-1}, w_1, \ldots, w_n) \]

\[ = \prod_{i=1}^{n} p(t_i \mid t_{i-2}, t_{i-1}, w_1, \ldots, w_n) \]

• Here features depend on arbitrary past decisions, and thus dynamic programming is not used
Beam search

• Keep K possible decision sequences at every point
  • Expand the K sequences in all possible ways
  • Keep the top-K ones for the next step
• Stop once you have M completed parse trees
Evaluation

- Slightly worse than lexicalized PCFGs (86.9 F₁)
- But is faster! (linear empirically)
Shift-reduce parser

• Another greedy transition-based parser

• Linear time complexity

• Based on a transition-based parser for dependency parsing, very popular and useful nowadays

• Supports unary and binary rules

• The main difference is the transition system
Data structures

- Buffer $B$: holds pos-tagged words to be processed
- Stack $S$: hold partially constructed trees
- *the man ate an apple*
Initialization and termination

- **Initialization**: entire sentence is in the buffer (first word at the front, empty stack)

- **Termination**: buffer is empty, stack has one tree, which is the output

```
DT    NN    VBD   DT    NN
the    man    ate    an   apple
```

```
S

B

S(ate)
  NP(man)
    DT(the)  NN(man)
    DT(an)  NN(apple)

VP(ate)
    VBD(ate)
    man
    an
    apple
```
Actions: shift

- **Shift**: remove pos-tagged word from buffer and push to the stack
Actions: reduce-X-left

• pop from the stack the top two trees. Construct new tree with category X, with the top tree as right child and bottom tree as left child. Copy head from the left child
Actions: reduce-X-right

- pop from the stack the top two trees. Construct new tree with category X, with the top tree as right child and bottom tree as left child. Copy head from the right child.
Actions: reduce-X-unary

- pop from the stack a tree. Construct new tree with category X with the popped tree as a child. Copy the head.
Action sequence

• *The men ate an apple*

<table>
<thead>
<tr>
<th>Buffer</th>
<th>Stack</th>
<th>Action</th>
</tr>
</thead>
<tbody>
<tr>
<td>The men ate an apple</td>
<td>the</td>
<td>shift</td>
</tr>
<tr>
<td>men ate an apple</td>
<td>men</td>
<td>the</td>
</tr>
<tr>
<td>ate an apple</td>
<td>(NP the men)</td>
<td>reduce-NP-right</td>
</tr>
<tr>
<td>an apple</td>
<td>ate</td>
<td>(NP the men)</td>
</tr>
<tr>
<td>apple</td>
<td>an</td>
<td>ate</td>
</tr>
<tr>
<td></td>
<td>apple</td>
<td>an</td>
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<tr>
<td></td>
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<td>ate</td>
</tr>
<tr>
<td></td>
<td>(VP ate an apple)</td>
<td>(NP the men)</td>
</tr>
<tr>
<td></td>
<td>(S the men ate an apple)</td>
<td>Reduce-S-right</td>
</tr>
</tbody>
</table>
Justification/Proof

• Any parse tree can be constructed with a sequence of these actions (let’s ignore unaries)

• **Height of a tree**: number of edges on longest path from root to leaves (POS tags)
  - **Height 0**: single word sentences. Obtained by a single shift action
  - **Height 1**: only one binary tree is possible (adding unaries is easy) and is obtained by the action sequence of shift-shift-reduce

• Assume we can build tree of length < \( n \). For height \( n \):
  - Construct the left child. Now there is one item in the stack
  - Construct the right child. Now there are two items in the stack and an empty buffer.
  - reduce
Training

- As usual:
  - Input: $s, d_1, \ldots, d_{i-1}$
  - Output: $d_i$

- Learning:
  - Sagae and Lavie use the perceptron learning algorithm
  - Log-linear models
  - Neural network
Features

• Based on
  • Top four items on stack
  • Top four items on buffer
  • Standard binary features (non-terminals at root and children, POS tags, words, children, ...)
• What if you want to use a neural network?
Complexity

• For a sentence with $n$ words
  
  • $n$ shift actions
  
  • $n-1$ binary reductions
  
  • Do not allow more than $k(=3)$ consecutive unary reduction actions
  
  • Linear number of actions
Evaluation

- 87.5 F1 (slightly lower than best LPCFG at the time)
- ~3-4x faster than a lexicalized PCFG parser
Globally-normalized
Globally-normalized models

- Given a training set \((x, y)\) of pairs of sentences with their parse trees

\[
p_\theta(y \mid x) = \frac{\exp(f(x, y)^\top \theta)}{\sum_{y' \in \mathcal{Y}} \exp(f(x, y')^\top \theta)}
\]

\(\mathcal{Y} : \) all parse trees for \(x\)
Global linear models

• Motivations:
  • Optimize what you care about
  • Flexibility in feature function
  • Avoid the label bias problem
Globally-normalized models

• Contain three components

  • A feature function $f$ mapping a pair $(x, y)$ to a feature vector $f(x, y)$

  • A generating function $GEN(x)$ enumerating all candidate outputs

  • A parameter vector $\theta$

\[ F(x) = \arg \max_y f(x, y) \top \theta \]
Parse re-ranking

- Assume we define $\text{GEN}(x)$ be a set of top-$K$ parse trees given by a lexicalized PCFG

- There is no decoding! This is a re-reranking

- We can define any feature over the parse tree
Example: coordination

- Parallelism in coordination
  - *Bars in New-York and pubs in London*
  - *Bars in New-York and pubs*

- It is not trivial to featurize this with a PCFG (even lexicalized). Easy to do given the full parse tree
  - Count the number of parallel/non-parallel coordination structures
Example: complex VPs

• No need to binarize, since there is no decoding
  • For a rule VP—> PP VBD NP NP SBAR
    • All adjacent non-terminal bigrams to the left and right of the head
      • <s> PP, NP NP, NP SBAR, SBAR </s>
    • Grandparent features
      • S—>VP—> PP VBD NP NP SBAR
    • Sibling features
      • S—>VP—> PP VBD NP NP SBAR and
      • S—>NP
Parsing without re-ranking

- What if want to parse from scratch?
- We need to use CKY-style algorithms for learning and decoding
- Features need to decompose
Rule productions

- Assume an input sentence $x$
- Assume a CFG in CNF $G=(V, \Sigma, R, S)$
- The CFG defines a set of parse trees $Y$
- A tree $y$ in $Y$ is a set of rule productions of the form:
  - $(A, B, C, i, k, j)$: the rule $A \rightarrow B C$ is seen with non-terminal $A$ spanning $x_i \ldots x_j$, non-terminal $B$ spanning $x_i \ldots x_k$, and non-terminal $C$ spanning $x_{k+1} \ldots x_j$
  - $(A, i)$: The rule $A \rightarrow x_i$ is in the parse tree
Example

S, NP VP, 1, 2, 5
NP, NN, NNS, 1, 1, 2
VP, VB, NP, 3, 3, 5
NP, DT, NN, 4, 4, 5
NN, 1
NNS, 2
VB, 3
DT, 4
NN, 5
Tagging: global feature function

- Global feature function

\[ f(x, y) = \sum_{i,j} g_j(h, i, t) = \sum_i g(h, i, t) \]

- Features are now counts, rather than binary
  - How many times a word ending in ‘ing’ was tagged as VBG
Parsing: global feature function

- **Warning**: all feature functions can look at $x$, I didn’t always consistently write that.

- Features decompose over rule productions:
  \[
  f(x, y) = \sum_{r \in y} g(r) \Theta = \sum_{r \in y} g(x, A, B, C, i, j, k) \Theta
  \]

- Example features:
  - The PCFG rule used
  - Conjunction of LHS with $x_i, x_{i-1}, x_j, x_{j+1}, \ldots$
Global linear model

\[ p_\theta(y \mid x) = \frac{\exp(f(x, y)^\top \theta)}{\sum_{y' \in \text{GEN}(x)} \exp(f(x, y')^\top \theta)} \]

\[ = \frac{\exp(\sum_r g(r)^\top \theta)}{\sum_{y' \in \text{GEN}(x)} \exp(\sum_{r' \in y'} g(r')^\top \theta)} \]
Decoding

\[ p_\theta(y \mid x) = \frac{\exp(f(x, y)^\top \theta)}{\sum_{y' \in \text{GEN}(x)} \exp(f(x, y')^\top \theta)} \]
\[ = \frac{\exp(\sum_r g(r)^\top \theta)}{\sum_{y' \in \text{GEN}(x)} \exp(\sum_{y' \in y'} g(r')^\top \theta)} \]

- Assume we have learned the parameters
  - It is enough to find \( y \) that maximizes the nominator
  - Because features decompose we can use CKY
  - Define the potential function:

\[ \Psi(r) = \exp(g(r)^\top \theta), \quad \Psi(y) = \prod_{r \in y} \Psi(r) = \exp(\sum_{r \in y} g(r)^\top \theta) \]
CKY works

- just replace q with $\psi$

**Input:** sentence $s = w_1 \ldots w_n$, A CFG $G = (V, \Sigma, S, R)$

**Initialization:**

for all $A \in N, i \in 1 \ldots n$

$$\pi(i, i, A) = \begin{cases} 
\Psi(x, A, i) & (A \rightarrow i) \in R \\
0 & \text{otherwise}
\end{cases}$$

**Algorithm:**

for all $i \in 1 \ldots (n - 1), l \in 1 \ldots (n - l)$

$j = i + l$

for all $A \in N,$

$$\pi(i, j, A) = \max_{(A \rightarrow BC) \in R} \Psi(x, A, B, C, i, j, k) \times \pi(i, s, B) \times \pi(s + 1, j, C)$$

$s \in i \ldots (j - 1)$

$$\text{bp}(i, j, A) = \arg \max_{(A \rightarrow BC) \in R} \Psi(x, A, B, C, i, j, k) \times \pi(i, s, B) \times \pi(s + 1, j, C)$$

$s \in i \ldots (j - 1)$
Learning

\[ L(\theta) = \sum_i \log p_\theta(y_i \mid x_i) \]

\[ \nabla L(\theta)_i = f(x_i, y_i) - \sum_{y'} p_\theta(y' \mid x) f(x, y') \]

How to compute the second term?
Learning

\[
\sum_{y} p_{\theta}(y \mid x)f(x, y) = \sum_{y} \sum_{r} p_{\theta}(y \mid x)g(x, r)
\]

\[
= \sum_{r=(A,B,C,i,j,k)} \sum_{y} p_{\theta}(y \mid x)g(x, r)
\]

\[
= \sum_{r=(A,B,C,i,j,k)} g(x, r) \sum_{y: r \in y} p_{\theta}(y \mid x)
\]

\[
= \sum_{r=(A,B,C,i,j,k)} g(x, r)q(x, r)
\]
Learning

- If we compute the $q$ terms efficiently then we can compute the gradients efficiently and learn.

- The $q$ terms are computed with a dynamic programming algorithm called *inside-outside*.

- Also used in unsupervised parameter estimation for PCFGs.

- Similar to CKY (sum instead of max).
Inside-outside algorithm

• **Input:**
  • sentence $x=x_1 \ldots x_n$
  • A CFG $G$
  • A potential function

$$\Psi(r) = \exp(g(r)^\top \theta), \quad \Psi(y) = \prod_{y \in y} \Psi(r) = \exp(\sum_{y \in y} g(r)^\top \theta)$$

• **Output:**

$$Z = \sum_{y \in \text{GEN}(x)} \Psi(y)$$

$$\mu(r) = \sum_{y : r \in y} \Psi(y)$$

Note that $q(r) = \frac{\mu(r)}{Z}$
Overall idea

- In forward-backward, we computed the probability until a certain position $i$ with tag $t$ and from position $i$ with tag $t$ until the end of the sequence (prefix and suffix)

```
I ate the large cake
```

```
DT
```

forward    backward
Overall idea

- Here the analog will be inside tree score and outside tree score
- We will compute those for every non-terminal and span
Inside scores

• Let $Y(A, i, j)$ be the set of trees (over $x$) with root $A$ that span $x_i \ldots x_j$.

• We will compute with dynamic programming the sum of potentials for all trees in $Y(A, i, j)$

$$\alpha(A, i, j) = \sum_{y \in Y(A, i, j)} \Psi(y)$$
Inside scores

- Computing inside scores recursively:

**Initialization:**
For all $i \in 1 \ldots n$, for all $A \in N$:

$$\alpha(A, i, i) = \Psi(A, i) \text{ if } (A \rightarrow x_i \in R), \ 0 \text{ otherwise}$$

**Recursion:**
For all $1 \leq i < j \leq n$, for all $A \in N$:

$$\alpha(A, i, j) = \sum_{A \rightarrow B} \sum_{C \ k=i}^{j-1} (\Psi(A, B, C, i, j, k) \times \alpha(B, i, k) \times \alpha(C, k, j))$$
Outside scores

- Let $O(A, i, j)$ be the set of outside trees with nonterminal $A$ over span $x_i \ldots x_j$.

- An outside tree is:
  - Rooted in $S$
  - Uses rules from the CFG
  - Yields $x_1 \ldots x_{i-1}Ax_{j+1} \ldots x_n$
Outside tree example

The dog saw the man in the park

O(NP, 4, 5)
Outside scores

- We compute with dynamic programming the sum of potentials of all outside trees for every non-terminal and span:

\[ \beta(A, i, j) = \sum_{y \in \mathcal{O}(A, i, j)} \Psi(y) \]
Outside scores

Initialization:
For all $A \in N$ :
$$\beta(A, 1, n) = 1 \text{ if } A = S, \ 0 \text{ otherwise}$$

Recursion:
For all $1 \leq i \leq j \leq n, (i, j) \neq (1, n)$, for all $A \in N$ :
$$\beta(A, i, j) = \sum_{B \rightarrow C} \sum_{A}^{i-1} \left( \Psi(B, C, A, k, i - 1, j) \times \alpha(C, k, i - 1) \times \beta(B, k, j) \right)$$
$$+ \sum_{B \rightarrow A} \sum_{C}^{n} \left( \Psi(B, A, C, i, j, k) \times \alpha(C, j + 1, k) \times \alpha(B, i, k) \right)$$
Combining inside and outside scores

\[ Z = \sum_{y \in \mathcal{Y}} \Psi(y) = \alpha(S, 1, n) \]

Let \( t^i_{A, i, j}, t^o_{A, i, j} \) be the inside tree and outside tree for a span \( x_i \ldots x_j \) non-terminal \( A \) for any tree \( y \) containing rule production \( r = (A, B, C, i, j, k) \):

\[ \Psi(t) = \Psi(t^o_{A, i, j}) \times \Psi(r) \times \Psi(t^i_{B, i, k}) \times \Psi(t^i_{C, k+1, j}) \]

It follow that:

\[ \mu(r) = \sum_{y: r \in y} \Psi(t) = \sum_{t_1 \in \mathcal{O}(A, i, j)} \sum_{t_2 \in \mathcal{T}(B, i, k)} \sum_{t_3 \in \mathcal{T}(C, k, j)} \Psi(t_1) \times \Psi(r) \times \Psi(t_2) \times \Psi(t_3) \]

\[ = \Psi(r) \times ( \sum_{t_1 \in \mathcal{O}(A, i, j)} \Psi(t_1) ) \times ( \sum_{t_2 \in \mathcal{T}(B, i, k)} \Psi(t_2) ) \times ( \sum_{t_3 \in \mathcal{T}(C, k, j)} \Psi(t_3) ) \]

\[ = \Psi(r) \times \beta(A, i, j) \times \alpha(B, i, k) \times \alpha(C, k, j) \]

Similarly it is simple to show that \( \mu(A, i) = \alpha(A, i, i) \times \beta(A, i, i) \)
Remaining details

• Complexity:
  • To compute both inside and outside scores we again go over every span and every split point and sum over all rules and split points
  • $O(n^3|N|^3)$

• Evaluation (with work on feature engineering):
  • 90.5 F1

• Finkel et al., 2008, Hall et al., 2014, …
Summary

• To use a global linear model (CRF) for parsing
  • Features need to decompose
  • Use Viterbi for decoding
  • Need to compute rule production marginals for the gradient
    • inside-outside algorithm
  • Complexity is the same as Viterbi
Neural CRF
Non-linear scoring function

• The only requirement for CKY and Inside-Outside was that the **global** score of a parse tree decomposes to **local** scores over rule productions:

\[ \Psi(x, y) = \prod_{r \in y} \Psi(x, r) \]

• We used a linear score for \( \psi \), but it can be a non-linear neural network, and the decoding would remain unchanged and correct.

• We will now see such a neural network.
Some re-writing

• Assume all features are conjunctions of “rule features” and “span” features

\[ \psi_{\text{sparse}}(x, A, B, C, i, j, k) = f_s(x, i, j, k)^\top W f_o(A, B, C) \]

Weight for conjunction of rule features and span feature
Learned representation

- Replace span features by a neural network
- We learn surface representations

\[ f_w(x, i, j, k) : \text{fixed-length sequence of word indicators} \]
\[ v(f_w) : \text{embedding of } f_w \]
\[ \psi_{\text{neural}}(x, A, B, C, i, j, k) = \text{relu}(H \cdot v(f_w))^\top W_{fo}(A, B, C) \]
Final representation

$$\Psi(\cdot) = \Psi_{\text{sparse}}(\cdot) + \Psi_{\text{neural}}(\cdot)$$
Features
Learning and inference

- SGD
- Can compute inside scores or feature expectations with the inside-outside algorithm in the neural network.
- Inference uses standard CKY after computing all of the local scores
- Evaluation: 91.3 F1
Missing pieces

• RNN grammars (Dyers et al.)

• Minimal span-based parser (Stern Andreas and Klein)