גנומיקה חישובית פרופ' רון שמיר, פרופ' חיים וולפסון, דר' עירית גת-ויקס ביה"ס למדעי המחשב,אוניברסיטת תל אביב

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Gene finding and regulatory motif analysis December 20, 2016



Gene Finding

Sources:

- •Lecture notes of Larry Ruzzo, UW.
- •Slides by Nir Friedman, Hebrew U.
- •Burge, Karlin: "Finding Genes in Genomic DNA", Curr. Opin. In Struct. Biol 8(3) '98
- Slides by Chuong Huynh on Gene Prediction, NCBI
- •Durbin's book, Ch. 3
- Pevzner's book, Ch. 9



Motivation

- ~3Gb human DNA in GenBank
- Only ~1.5% of human DNA is coding for proteins
- 220,731,315,250 total bases in GenBank (10/2016)
- Thousands of species have been sequenced, more to follow
- Total number of species represented in UniProtKB/Swiss-Prot (2016): 13,367
- Need to locate the genes!
- Goal: Automatic finding of genes

Reminder: The Genetic Code

				S	econd	l let	ter			
			U		с		A			
First letter		UUU Phenyl- alanine	UCU UCC	Sorino	UAU UAC	Tyrosine	UGU UGC	Cysteine	U C	
		UUA UUG	Leucine	UCA UCG	Jerme	UAA UAG	Stop codon Stop codon	UGA UGG	Stop codon Tryptophan	A G
	ç	CUU CUC	CUU CUC CUA CUG	CCU CCC	CAU CAC	CAU CAC	Histidine	CGU CGC	Arginine	U C
		CUA CUG		CCA CCG	FIQUITE	CAA CAG	Glutamine	CGA CGG	, aginine	A G
		AUU AUC	Isoleucine	ACU ACC	Thrassina	AAU AAC	Asparagine	AGU AGC	Serine	U C
		A AUA Methionine; AUG initiation codon	ACA ACG	Threomite	AAA AAG	AAA AAG Lysine		AGA AGG Arginine		
	G	G GUU GUC GUA GUG Valine GCU GCC GCA GCA	GCU GCC		GAU GAC	Aspartic acid	GGU GGC	Glyrine	U C	
	G		Aidnine	GAA GAG	Glutamic acid	GGA GGG	Giyeme	A G		

1 start, 3 stop codons

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Genes in Prokaryotes

- High gene density (e.g. 70% coding in H. Influenza)
- No introns
- → most long ORFs are likely to be genes.



Open Reading Frames

- Reading Frame: 3 possible ways to read the sequence (on each strand).
- ACCUUAGCGUA = Threonine-Leucine-Alanine
- ACCUUAGCGUA = Proline-Stop-Arginine
- ACCUUAGCGUA = Leucine-Serine-Valine
- Open Reading Frame (ORF): Reading frame with no stop codons.
- ORF is maximal if it starts right after a stop and ends in a stop
- Untranslated region (UTR): ends of the mRNA (on both sides) that are not translated to protein.

Finding long ORFs

- In random DNA, one stop codon every $64/3 \rightarrow 21$ codons on average
- Average protein is ~300 AA long
- => search long ORFs
- Problems:
 - short genes
 - many more ORFs than genes
 - In E. Coli one finds 6500 ORFs but only 1100 genes.
 - Call the remaining Non-coding ORF (NORFS)
 - Overlapping long ORFs on opposite strands



Codon Frequencies

- Coding DNA is not random:
 - In random DNA, expect
 - Leucine: Alanine: Tryptophan ratio of 6:4:1
 - In real proteins, 6.9:6.5:1
 - In some species, 3rd position of the codon, up to 90% A or T
- Different frequencies for different species.



frequency of relative freq of						Human codon										
age d don (ousa	of ead (per nd)	ch	eac sync	each codon among synonymous codons					usage							
Gly	GGG	17.08	0.23	Arg	AGG	12.09	0.22	Trp	TGG	14.74	1	Arg	CGG	10.4	0.19	
Gly	GGA	19.31	0.26	Arg	AGA	11.73	0.21	End	TGA	2.64	0.61	Arg	CGA	5.63	0.1	
Gly	GGT	13.66	0.18	Ser	AGT	10.18	0.14	Cys	TGT	9.99	0.42	Arg	CGT	5.16	0.09	
Gly	GGC	24.94	0.33	Ser	AGC	18.54	0.25	Cys	TGC	13.86	0.58	Arg	CGC	10.82	0.19	
Glu	GAG	38.82	0.59	Lys	AAG	33.79	0.6	End	TAG	0.73	0.17	GIn	CAG	32.95	0.73	
Glu	GAA	27.51	0.41	Lys	AAA	22.32	0.4	End	ΤΑΑ	0.95	0.22	GIn	CAA	11.94	0.27	
Asp	GAT	21.45	0.44	Asn	AAT	16.43	0.44	Tyr	TAT	11.8	0.42	His	САТ	9.56	0.41	
Asp	GAC	27.06	0.56	Asn	AAC	21.3	0.56	Tyr	TAC	16.48	0.58	His	CAC	14	0.59	
Val	GTG	28.6	0.48	Met	ATG	21.86	1	Leu	TTG	11.43	0.12	Leu	CTG	39.93	0.43	
Val	GTA	6.09	0.1	lle	ATA	6.05	0.14	Leu	TTA	5.55	0.06	Leu	СТА	6.42	0.07	
Val	GTT	10.3	0.17	lle	ATT	15.03	0.35	Phe	ттт	15.36	0.43	Leu	СТТ	11.24	0.12	
Val	GTC	15.01	0.25	lle	ATC	22.47	0.52	Phe	ттс	20.72	0.57	Leu	СТС	19.14	0.20	
Ala	GCG	7.27	0.1	Thr	ACG	6.8	0.12	Ser	TCG	4.38	0.06	Pro	CCG	7.02	0.11	
Ala	GCA	15.5	0.22	Thr	ACA	15.04	0.27	Ser	ТСА	10.96	0.15	Pro	CCA	17.11	0.27	
Ala	GCT	20.23	0.28	Thr	АСТ	13.24	0.23	Ser	тст	13.51	0.18	Pro	ССТ	18.03	0.29	
Ala	GCC	28.43	0.4	Thr	ACC	21.52	0.38	Ser	тсс	17.37	0.23	Pro	ccc	20.51	0.33	
	eque age d don d ousa Gly Gly Gly Glu Glu Glu Asp Val Val Val Val Val Val Val Ala Ala	equency o age of ead don (per ousand) Gly GGG Gly GGA Gly GGC Glu GAA Glu GAA Asp GAT Asp GAT Val GTG Val GTA Val GTC Val GTC Ala GCG Ala GCA	equency of age of each don (per ousand) Gly GGG 17.08 Gly GGA 19.31 Gly GGT 13.66 Gly GGC 24.94 Glu GAG 38.82 Glu GAA 27.51 Asp GAT 21.45 Asp GAT 21.45 Asp GAT 21.45 Asp GAC 27.06 Val GTG 28.6 Val GTA 6.09 Val GTT 10.3 Val GTT 10.3 Ala GCC 7.27 Ala GCA 15.5	equency of each don (per ousand) relation (per ousand) Gly GGG 17.08 0.23 Gly GGA 19.31 0.26 Gly GGA 19.31 0.26 Gly GGT 13.66 0.18 Gly GGC 24.94 0.33 Glu GAA 27.51 0.41 Asp GAC 27.06 0.56 Val GTG 28.6 0.48 Val GTA 6.09 0.1 Val GTT 10.3 0.17 Val GTC 15.01 0.25 Ala GCG 7.27 0.1 Ala GCA 15.5 0.22 Ala GCC 28.43 0.4	equercy of age of each consumeration of each and and any of each any of ea	equency of age of each don (per ousand)relative freq each codon an synonymus of aynonymus of<	relative freq of each codon any 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.



http://genome.imim.es/courses/Lisboa01/slide3.8.html

First Order Markov Model

- Use two Markov models (similar to CpG islands) to discriminate genes from NORFs
- Given a sequence of nucleotides X_1, \dots, X_n we compute the log-odds ratio:

$$\log \frac{P(X_1, \dots, X_n \mid \mathbf{G})}{P(X_1, \dots, X_n \mid \mathbf{R})} = \sum_i \log \frac{A^G_{X_i X_{i+1}}}{A^R_{X_i X_{i+1}}}$$

Bit= unit when log base 2 is used

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First Order Markov Model



Figure 3.11 Histograms of the log-odds per nucleotide for all NORFs (grey) and genes (black line) according to a first order Markov chain. Because of the large number of NORFs, the histogram bin size is five times smaller for the NORFs.

Test on E. Coli data Durbin et al pp.74

- Average log-odds per nucleotide
 - in genes : 0.018
 - in NORFs: 0.009
- But the variance makes it useless for discrimination (similar results for 2nd-order MM)
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Using codons

- Translate each ORF into a sequence of codons
- Form a 64-state Markov chain

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- Codon is more informative than its translation
- Estimate probabilities in coding regions and NORFs



Using Codon Frequencies

- Assume each codon is iid
- For codon abc calculate frequency f_{abc} in coding region
- Given coding sequence $a_1b_1c_1, \dots, a_{n+1}b_{n+1}c_{n+1}$
- Calculate

$$p_{1} = f_{a_{1}b_{1}c_{1}} * f_{a_{2}b_{2}c_{2}} * \dots * f_{a_{n}b_{n}c_{n}}$$

$$p_{2} = f_{b_{1}c_{1}a_{2}} * f_{b_{2}c_{2}a_{3}} * \dots * f_{b_{n}c_{n}a_{n+1}}$$

$$p_{3} = f_{c_{1}a_{2}b_{2}} * f_{c_{2}a_{3}b_{3}} * \dots * f_{c_{n}a_{n+1}b_{n+1}}$$

The probability that the *i*-th reading frame is the coding region:

CodonPreference

CODONPREFERENCE of: gb_ba:EcoOmpa City 778, 1 to 2270 October 24, 1996 16:12 Codon Table: GenRunData:ecohigh.cod PrefWindow: 25 Rare Codon Threshold: 0.10



eptmoneterence_1.ffoure (ettber 24, 1996).

RNA Transcription

- Not all ORFs are expressed.
- Transcription depends on regulatory signals
- Minimal regulatory region core promoter to which RNA polymerase and initiation factors bind to start transcription.
- At the termination signal the polymerase releases the RNA and disconnects from the DNA.



E. coli promoters



- "TATA box" (or Pribnow Box)
- Not exact



Positional Weight Matrix (PWM)

- $F_{b,j}$: frequency of base b in position j.
- Assumes independence btw positions
- For TATA box:

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pos:	1	2	3	4	5	6
А	2	95	26	59	51	1
С	9	2	14	13	20	3
G	10	1	16	15	13	0
Т	79	3	44	13	17	96

• f_b : background frequency.

Scoring Function

• For sequence $S=B_1B_2B_3B_4B_5B_6$

 $P(S \mid \text{promoter}) = \prod_{i=1}^{6} f_{B_i,i}$ $P(S \mid \text{non - promoter}) = \prod_{i=1}^{6} f_{B_i}$

Log-likelihood ratio score:

$$\log\left(\frac{P(S \mid \text{promoter})}{P(S \mid \text{non - promoter})}\right) = \log\left(\frac{\prod_{i=1}^{6} f_{B_i,i}}{\prod_{i=1}^{6} f_{B_i}}\right) = \sum_{i=1}^{6} \log\left(\frac{f_{B_i,i}}{f_{B_i}}\right)$$



Gene finding: coding density

As the coding/non-coding length ratio decreases, exon prediction becomes more complex





Eukaryote gene structure





Typical figures: verterbrates

- S' Untranslated region (UTR) Promoter Transcription start site Internal exon Internal exon
- Promoter: 2-5kb upstream of TSS
- 5' UTR: ~750 bp, 3' UTR: ~450bp
- Ave gene length: 30kb, coding region: 1-2kb
- Average of 6 exons, 150bp long
- Huge variance!
 - dystrophin: 2.4Mb long
 - TTN: 363 exons, longest: 17,106bp
 - Blood coagulation factor: 26 exons, 69bp to 3106bp; intron 22 contains another unrelated gene

Splicing

- Splicing: the removal of the introns.
- Performed by the spliceosome complex, containing both proteins and snRNA.
- The snRNA recognizes the splice sites through RNA-RNA base-pairing
- Recognition must be precise: a 1nt error shifts the reading frame making nonsense of its message.
- Many genes have alternative splicing, which changes the protein created.





- 1st modeling approach: positional weight matrices
 - Problematic with weak/short signals
 - Does not exploit all info (reading frames, intron/exon stats...)
- → try integrated approaches!

Length Distribution

Suppose we use HMM for gene structure



•The length of each exon (intron) has a geometric distribution:

 $P(\text{exon of length } k) = p^k(1-p)$

HMM is a memory-less process, so the only length distribution that can be modeled is geometric.



Exon and Intron Length Distribution



Generalized HMM

(Burge & Karlin, J. Mol. Bio. 97 268 78-94)

- Hidden Markov states **q**₁,...**q**_n
- State q_i has output length distribution f_i
- Output of each state can have a different probabilistic model (weight matrix, codon freq, ...)
- Initial state probability distribution $\boldsymbol{\pi}$
- State transition probabilities T_{ij}



GenScan Model



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GenScan model



- states = functional units along a gené
- The allowed transitions ensure the order is biologically consistent

ACCUUAGCGUA ← ...intron.... → ACCUUAGCGUA

ACCUUAGCGUA ← ...intron.... → ACCUUAGCGUA

 The index of the intron model = the phase of the exons before and after it

In terms of output and length, I₀, I₁, I₂₉
 Coore identical

Signal Models

- Genscan uses different models to model the different biological signals
 - Weight Matrix Model
 - Position specific distribution.
 - Columns are independent
 - Used for
 - Translation initiation signal
 - Translation termination signal
 - promoters
 - polyadenylation signals



Splice Sites

- Correct recognition of these sites greatly enhances ability to predict correct exon boundaries.
- Used Weighted Array Model: a generalization of PWM that allows for dependencies between adjacent positions
- Accurate modeling of these sites led to substantial improvement in performance.



GenScan Performance

Accuracy of GENSCAN for different signal and exon types.

(a) Prediction of individual splice sites and translational signals.

Type of signal	Type of exon	Anr	lotated exons	Predicted exons		
	• ·	Number	% Correctly predicted	Number	% Correctly predicted	
Initiation	Initial only	570	66	450	84	
Termination	Terminal only	570	78	487	91	
5' splice site	Initial only	570	88	450	89	
5' splice site	Internal only	1510	93	1682	89	
5' splice site	Initial and internal	2080	91	2132	89	
3' splice site	Terminal only	570	81	487	92	
3' splice site	Internal only	1510	92	1682	83	
3' splice site	Internal and terminal	2080	89	2169	85	

(b) Accuracy for initial, internal and terminal exons.

Exon type		A	nnotated exor		Predicted exons				
	Number	% Exactly	% Partially	% Missed	Number	% Exactly	% Partially	% Wrong	
Initial	570	65	25	9	457	81	9	10	
Internal	1510	90	5	4	1707	80	11	8	
Terminal	570	76	8	15	509	84	6	8	
All types	2650	81	10	8	2678	81	10	9	

Predicts correctly 80% of exons

Prediction accuracy per bp > 90%



Precision and Recall

Accuracy of GENSCAN for different signal and exon types.

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selected elements



GenScan Output





Sam Karlin, Chris Burge











Finding Genes via mRNA-DNA alignment Gelfand, Mironov, Pevzner PNAS '93 9061-6

Idea: If we have mature (spliced) mRNA seq, we can align it to the genomic DNA, skipping over introns



"Spliced alignment" problem



Transcript based prediction using NGS (2009+ style)

 Extract mRNA; break randomly into short segments (~100bp)

100**M**

- Sequence 100K M segments
- Align segments to the known gene sequences (
 stringology here!)
- Obtain counts how many copies of each gene were found















Yassour M, et al. Ab initio Construction of a Eukaryotic Transcriptome 40 correction of a Eukaryotic Transcriptome 40





Regulatory sequence analysis

Slides with Chaim Linhart



Regulation of Transcription

- A gene's ranscription regulation is mainly encoded in the DNA in a region called the promoter
- Each promoter contains several short DNA subsequences, called binding sites (BSs) that are bound by specific proteins called transcription factors (TFs)



Regulation of Transcription (II)

Assumption:

Co-expression ↓ Transcriptional co-regulation ↓ Common BSs



WH-questions

- V Why are we looking for common BSs?
- What exactly are we trying to find?
- Where should we look for it?
- How can we find it?



Promoter Region (Where?)

What is the promoter region?

- Upstream Transcription Start Site (TSS)
 - Too short \rightarrow miss many real BSs (false negatives)
 - Too long \rightarrow lots of wrong hits (false positives)
 - Length is species dependent (e.g., yeast ~600bp, thousands in human)
 - Common practice: ~ 500-2000bp
- Consider both strands?
 - Common practice: Yes



What: Models for Binding Sites

(I) Exact string(s)

Example: BS = TACACC , TACGGC

CAATGCAGGATACACCGATCGGTA

GGAGTACGGCAAGTCCCCATGTGA

AGGCTGGACCAGACTCTACACCTA



(II) String with mismatches

Example: BS = TACACC + 1 mismatch

CAATGCAGGATTCACCGATCGGTA GGAGTACAGCAAGTCCCCATGTGA AGGCTGGACCAGACTCTACACCTA



(III) Degenerate string $\underbrace{\text{Example:}}_{BS = \text{TASDAC}} (S=\{C,G\} D=\{A,G,T\})$

CAATGCAGGATACAACGATCGGTA GGAG<mark>TAGTAC</mark>AAGTCCCCATGTGA AGGCTGGACCAGACTC<mark>TACGAC</mark>TA



(IV) Position Weight Matrix (PWM)

a.k.a Position Specific Scoring Matrix (PSSM)

Example:

Score: product of base probabilities. Need to set score threshold for hits.

A	0.1	0.8	0	0.7	0.2	0
С	0	0.1	0.5	0.1	0.4	0.6
G	0	0	0.5	0.1	0.4	0.1
Т	0.9	0.1	0	0.1	0	0.3

ATGCAGGATACACCGATCGGTA 0.0605 GGAGTAGAGCAAGTCCCGTGA 0.0605 AAGACTCTACAATTATGGCGT 0.0151

How: Experimental techniques

Protein Binding Microarrays

Berger et al, Nat. Biotech 2006

- Generate an array of double-stranded
 DNA with all
 possible k-mers
- Detect TF binding to specific k-mers





Chromatin Immunoprecipitation (ChIP)



Isolate the chromatin. Shear DNA along with bound proteins into small fragments.

Bind antibodies specific to the DNA-binding protein to isolate the complex by precipitation. Reverse the cross-linking to release the DNA and digest the proteins.

Identify bound DNA via microarray hybriziation or sequencing

http://www.bio.brandeis.edu/haberlab/jehsite/chip.html

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How: I. Analyzing known motifs



PRomoter Integration in Microarray Analysis (Elkon et al. '03)

- Goal: Identify enriched TFs = TF motifs over-represented in promoters of co-regulated genes
 - Input: TF motif(s), target and background sets of promoter sequences
 - Find motif hits in all promoters

Motif:

- Compute enrichment of hits in the target set compared to the background set



Computation of Motif Hits

Computing the threshold for a PWM:

- Compute 2nd-order Markov model of background sequences
- Generate random sequences using the model (e.g., 1,000 sequences of length 1,000)
- Set threshold s.t. PWM has $\sim 5\%$ hits at random.

This "ensures" a pre-defined false-positive rate, but no guarantee on false-negative rate.

Motif Enrichment

Each promoter is hit or not.

- Let: B = total # of promoters (BG)
 - T = # of target-set promoters
 - b =total # of promoters that are hit

t = # of target-set promoters that are hit Then (hypergeometric distribution assumption): Prob. for t hits in target-set: $P(t) = {\binom{b}{t} \binom{B-b}{T-t}} / {\binom{B}{T}}$

Prob. for at least *t* hits:

$$p - value = \sum_{i=t}^{\min\{b,T\}} P(i) \qquad 59$$

R

b

TF Synergism

Find pairs of TFs that tend to occur in the same promoters

Let: T = # of promoters in target-set

 t_1 , $t_2 = #$ of promoters hit by TF 1,2

 t_{12} = # of promoters hit by *both* TFs (w/o overlaps!)

Then:

Prob. for co-occurrence of at least t_{12} :

synergism
$$p-value = \frac{\sum_{i \ge t_{12}} {\binom{t_1}{i} {\binom{T-t_1}{t_2-i}}}}{{\binom{T}{t_2}}}$$

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PRIMA: Human Cell Cycle

Whitfield et al. ('02) identified 568 genes that are periodically expressed in the human cell-cycle and partitioned them into the 5 phases of the cell-cycle



PRIMA: results on HCC

PRIMA found 8 enriched TFs in the 568 HCC genes (w.r.t. 13K BG promoters):



Results on HCC (III)

Co-occurring pairs of TFs:



How: II Motif discovery

Bailey & Elkan ZOOPS model

- *n* sequences, *m* possible motif positions per sequence.
- <u>Assumption:</u> Zero Or One occurrence of the motif Per Sequence.
- Prior probability for one occurrence : γ
- Prior probability for motif in position $j: \lambda = \gamma/m$
- What is the hidden data?
- What is the Q function?

Bailey & Elkan ZOOPS (cont.)

- Z_{ii} indicator for motif at sequence *i*, position *j*.
- Q_i indicator for motif in sequence *i*.

$$\log Pr(X, Z | \theta, \gamma) = \sum_{i=1}^{n} \sum_{j=1}^{m} Z_{i,j} \log Pr(X_i | Z_{i,j} = 1, \theta) + \sum_{i=1}^{n} (1 - Q_i) \log Pr(X_i | Q_i = 0, \theta) + \sum_{i=1}^{n} (1 - Q_i) \log(1 - \gamma) + \sum_{i=1}^{n} Q_i \log(1$$

$$Z_{i,j}^{(t)} = \frac{f_i}{f_0 + \sum_{k=1}^m f_k}$$
, where

$$f_0 = Pr(X_i | Q_i = 0, \theta^{(t)}) (1 - \gamma^{(t)}), \text{ and} f_j = Pr(X_i | Z_{i,j} = 1, \theta^{(t)}) \lambda^{(t)}, \ 1 \le j \le m$$

(ex.)

The MEME Suite

Motif-based sequence analysis tools



Tim Bailey, Charles Elkan



Research Professor Department of Pharmacology School of Medicine University of Nevada, Reno

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Professor
 Department of
 Computer Science and
 Engineering University
 of California, San
 Diego